

# Inverse Shade Trees for Non-Parametric Material Representation and Editing

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MERL

# Complex Appearance



# Appearance Acquisition



- 2,000 Images
- 6 GB

•  
•  
•

# Challenge

- Given: dense set of measurements of light transport function.
- Provide: intuitive representation that is **compact** and allows **editing**.

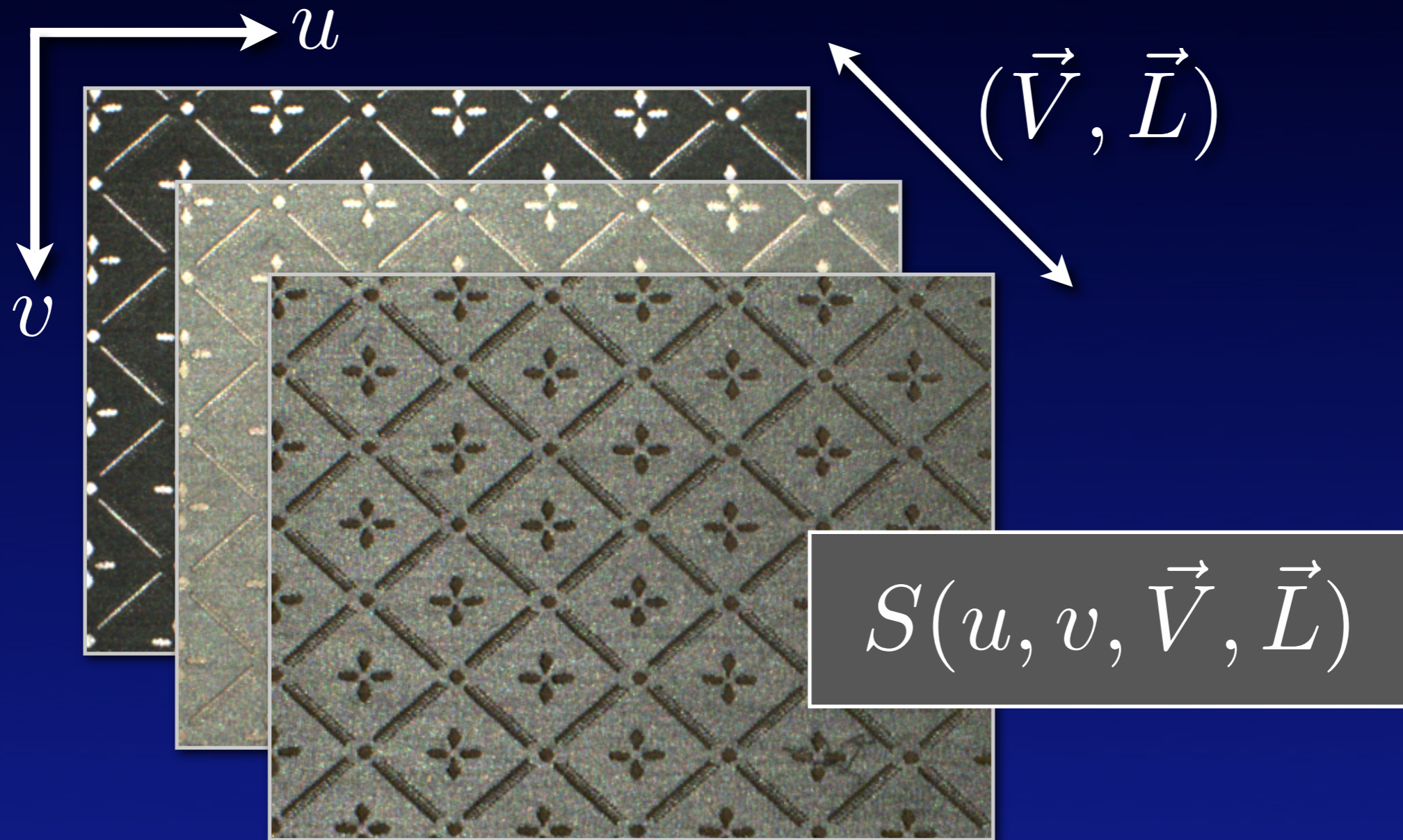


Original Measured  
Appearance



Result of Editing  
Material Properties

# Spatially-Varying Reflectance

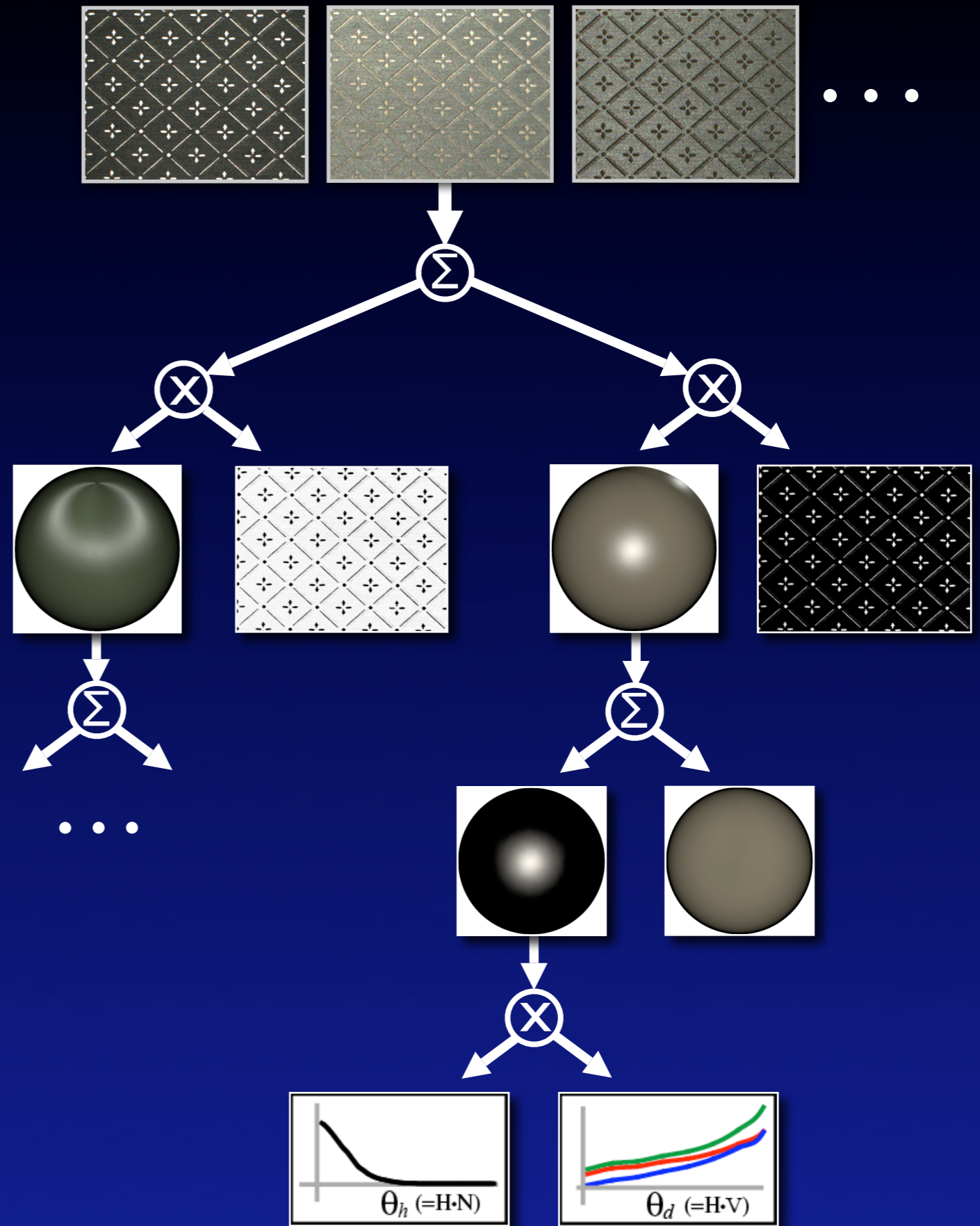


Spatially-Varying Bidirectional Reflectance Distribution Function

Observation #1:  
Represent high-dimensional  
measured function as  
tree-structured collection of  
lower-dimensional parts.

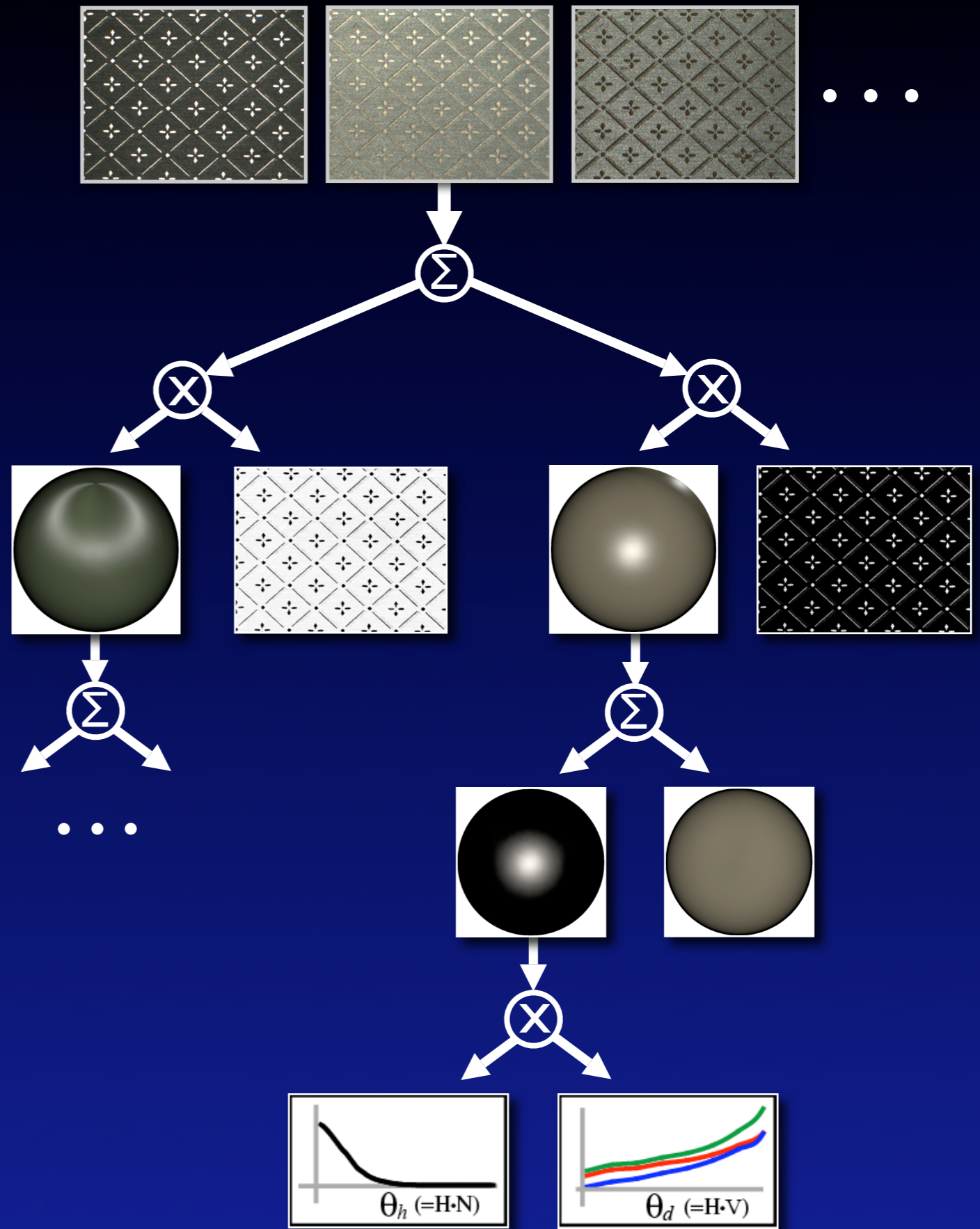
Observation #2:  
Decomposition at each level  
is matrix factorization.

Observation #3:  
Intuitive decomposition  
achieved using constrained  
factorization.



Shade Trees  
Cook 1984

Inverse  
Shade Trees



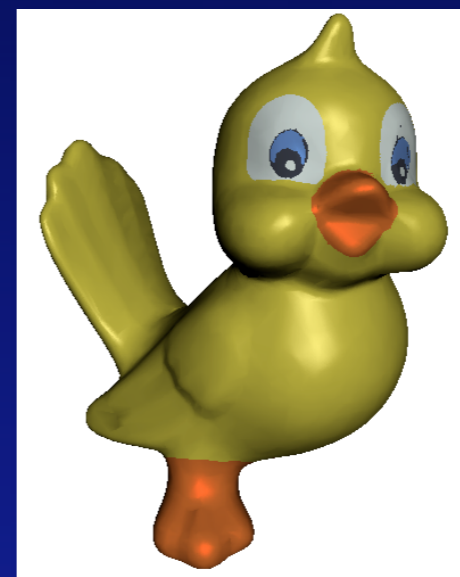
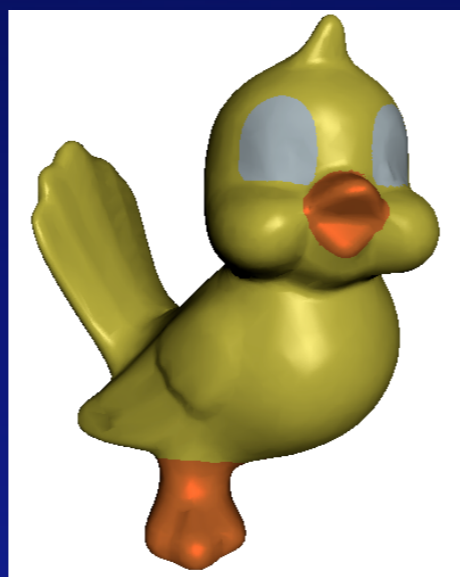
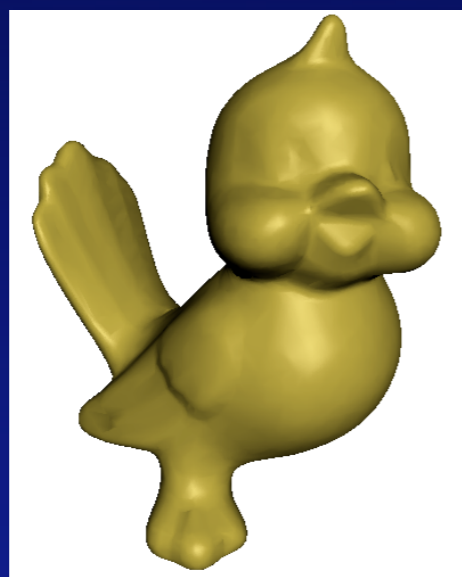
# Outline

- Introduction
- **Prior Work**
- Factorization
- Editing
- Conclusions and Future Work



# Fitting Parametric Models

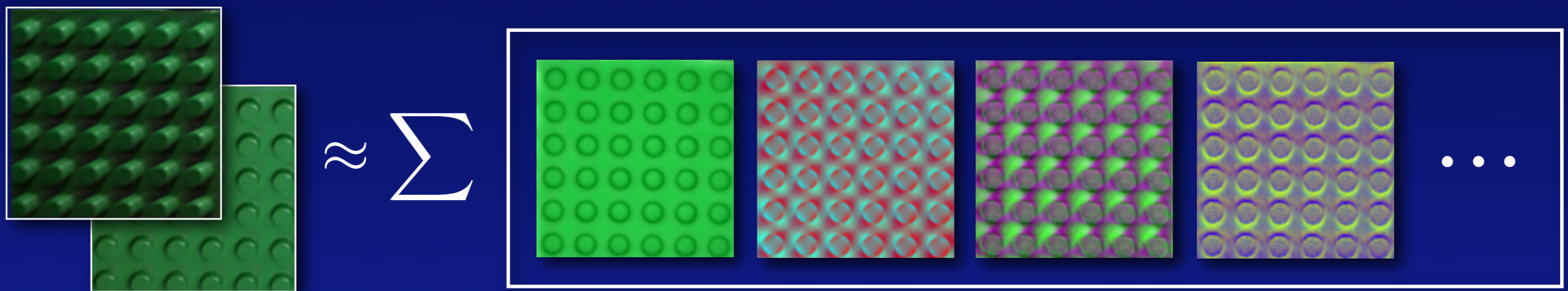
- Cluster fits of parametric BRDF:  
[Lensch et al. 03], [Goldman et al. 05].
- Editable **if** nice clusters
- Single analytic BRDF limits accuracy



Lensch et al. 2003

# Dimensionality Reduction

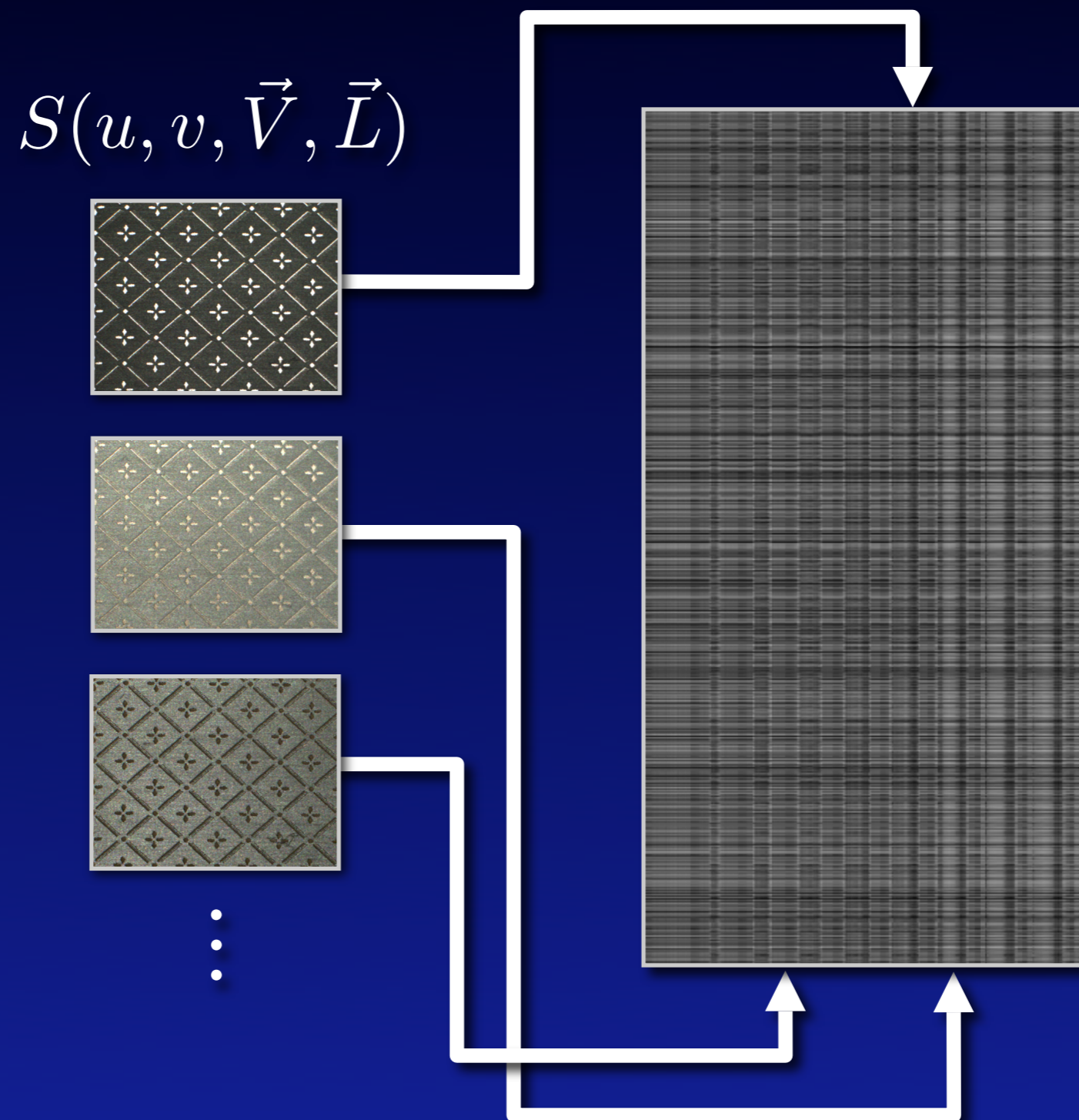
- Apply rank-reduction algorithms to data matrix:  
[Dana et al. 99], [Chen et al. 02], [Tsumura et al. 03]
- Compact and accurate
- Cannot be directly edited



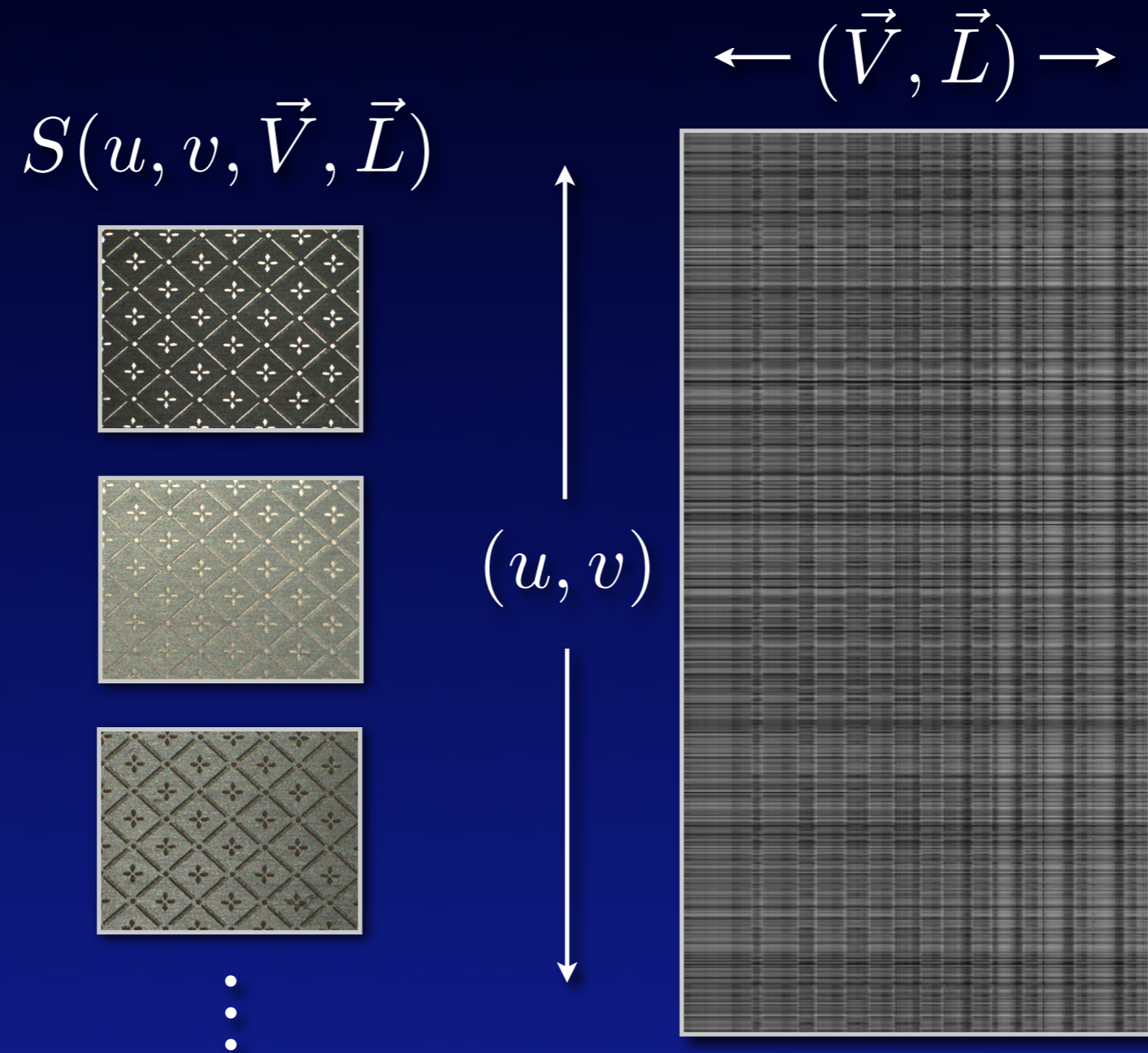
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- **Factorization**
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- Conclusions and Future Work

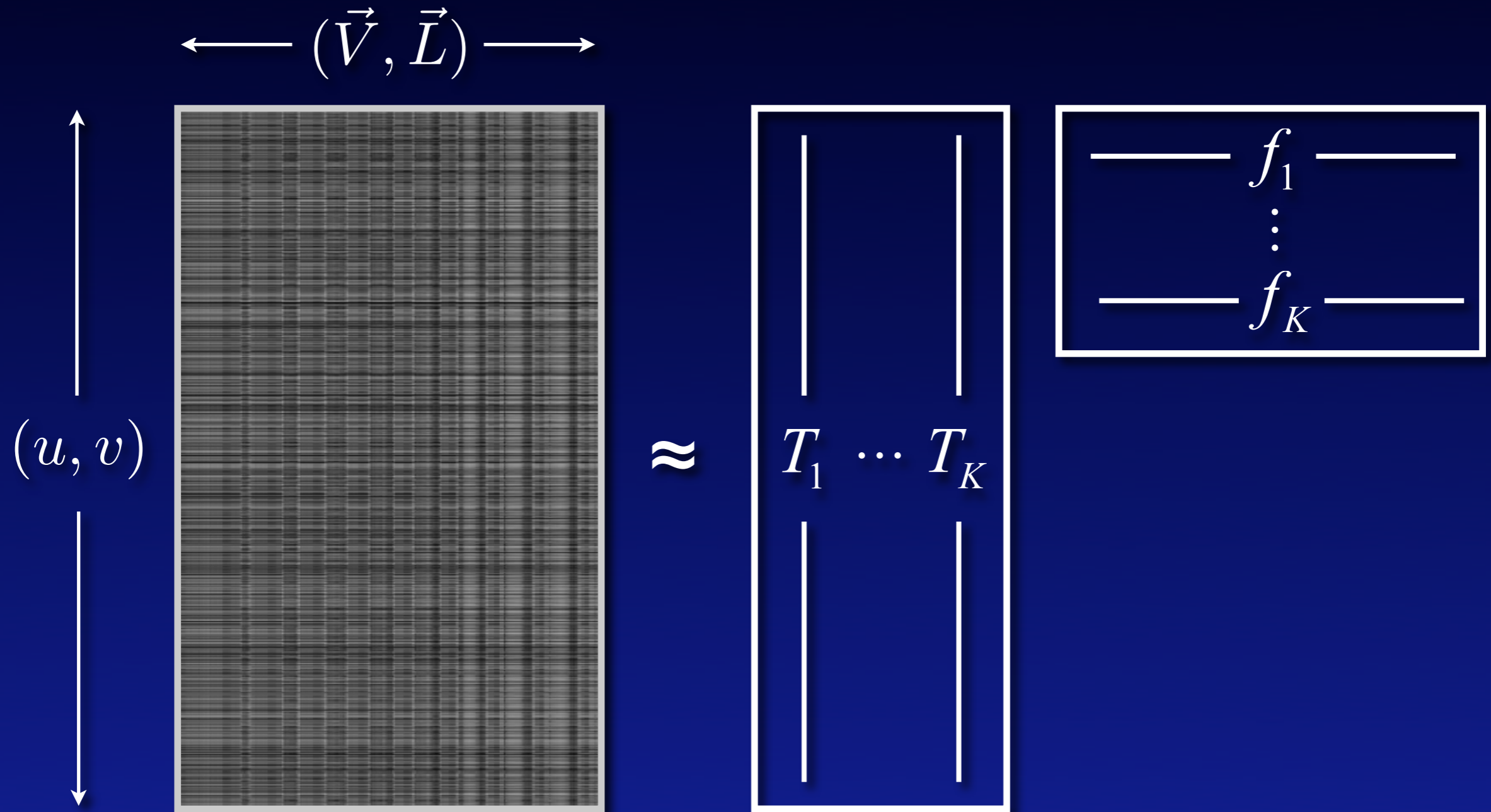
# Tabulate Raw Data



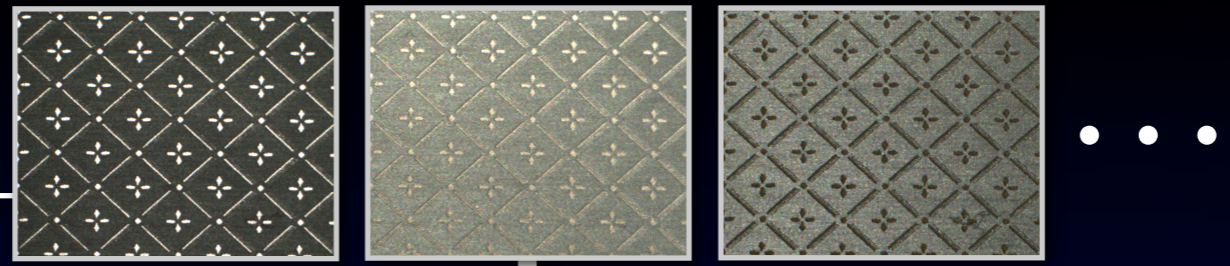
# Tabulate Raw Data



# Factorization of SVBRDF



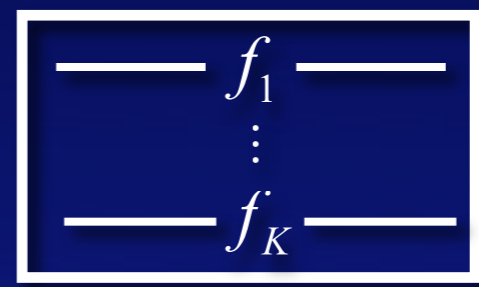
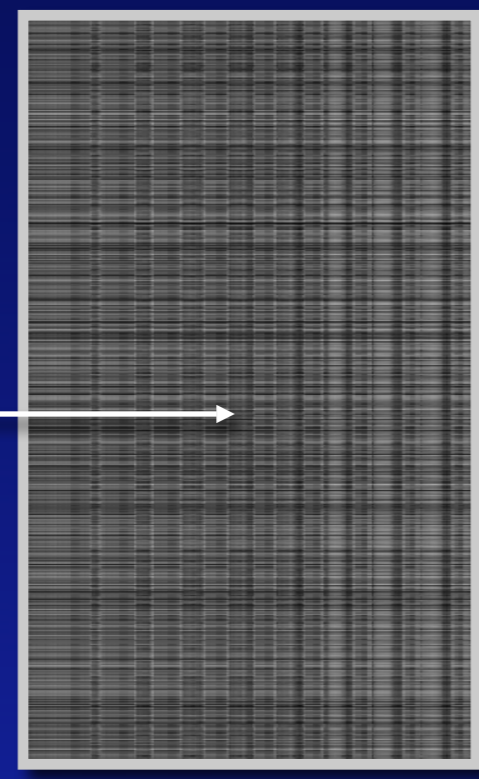
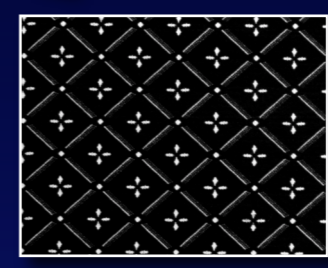
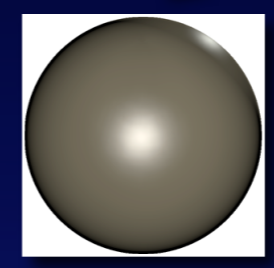
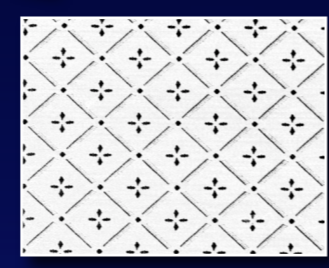
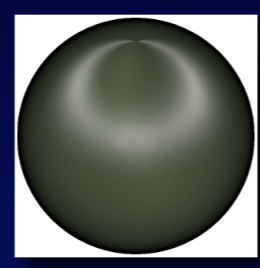
6D SVBRDF



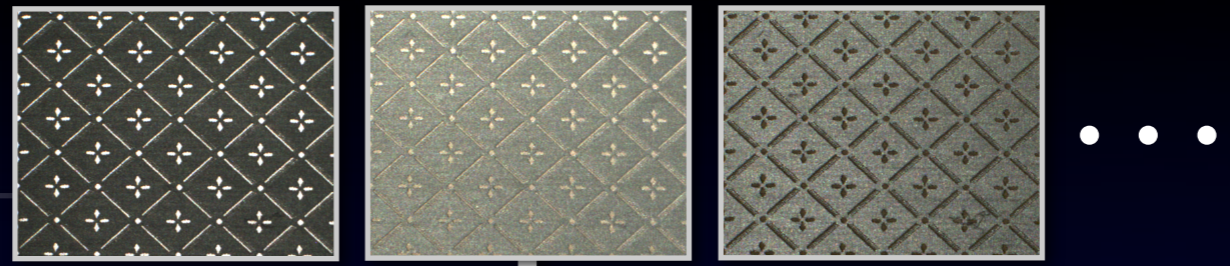
$\Sigma$

$\otimes$

$\otimes$



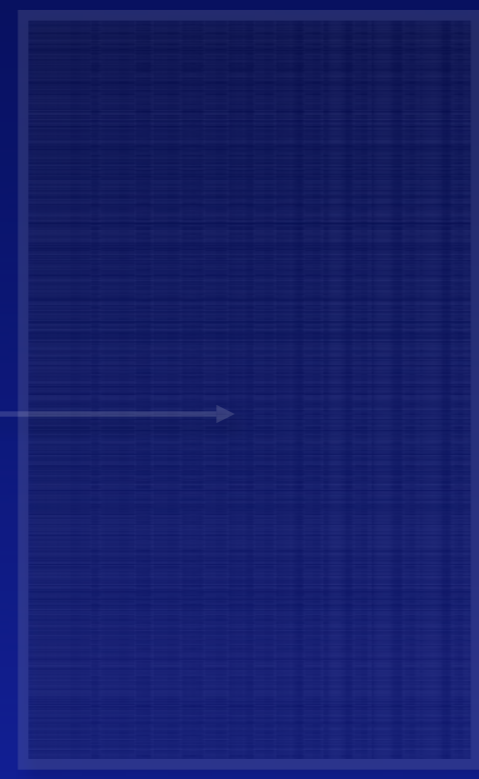
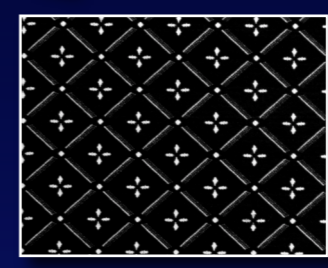
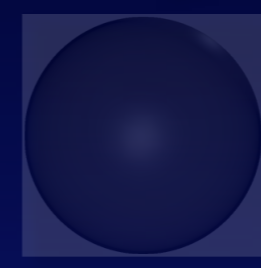
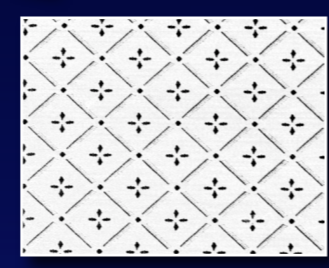
6D SVBRDF



$\Sigma$

$\otimes$

$\otimes$



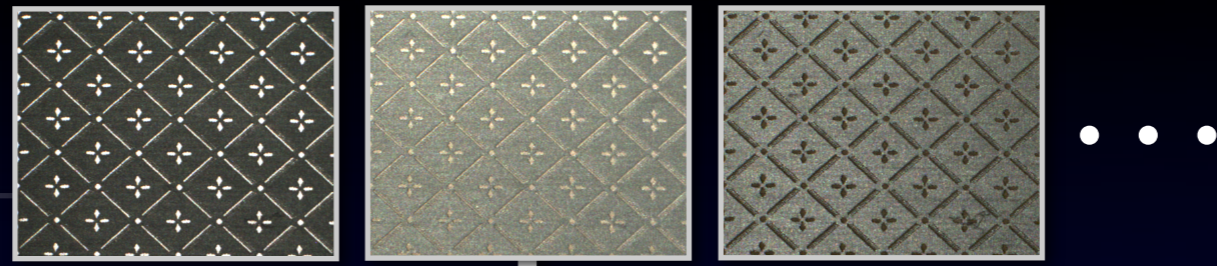
$T_1 \dots T_K$

$f_1$   
 $\vdots$   
 $f_K$

2D Spatial Blending Weights



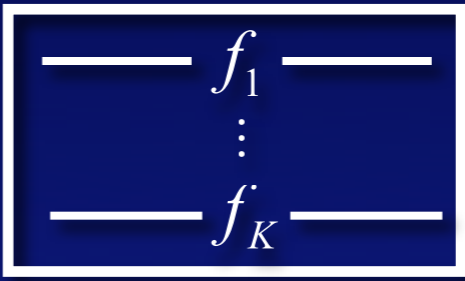
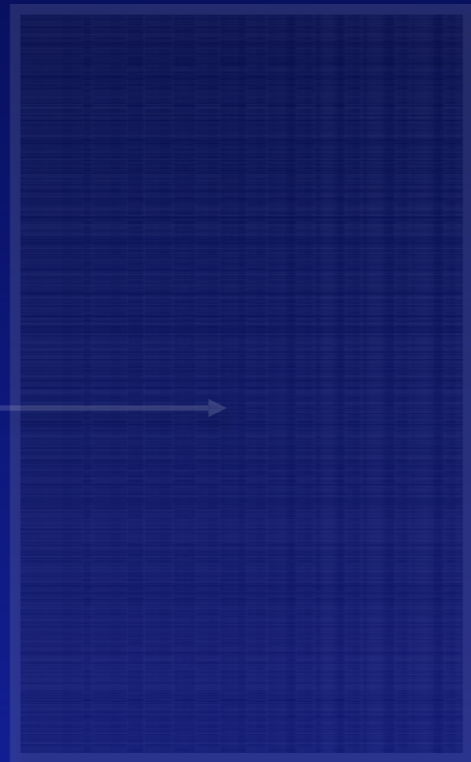
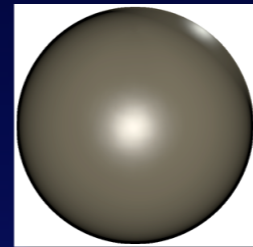
6D SVBRDF



$\Sigma$

$\otimes$

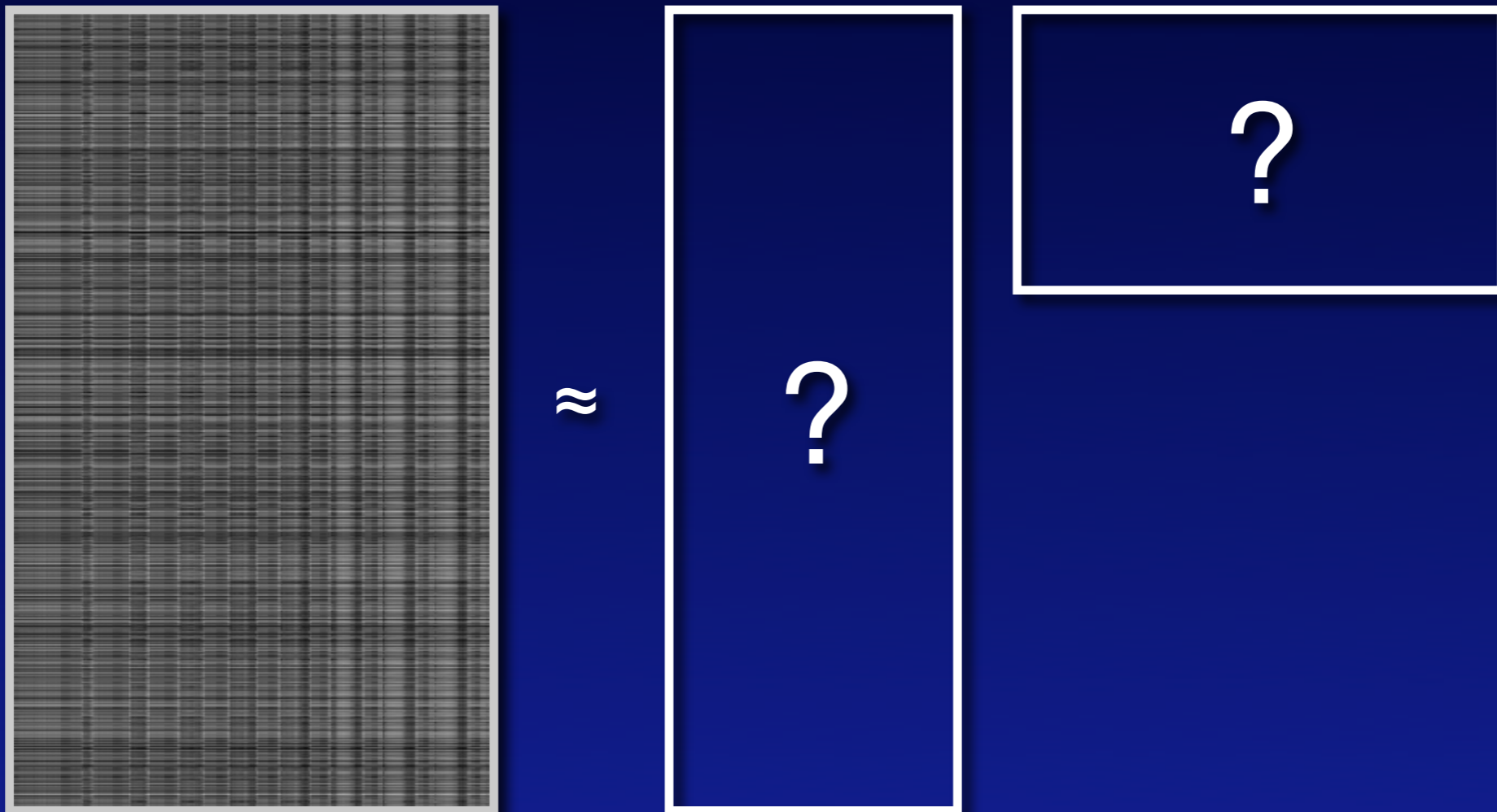
$\otimes$



4D Basis BRDFs

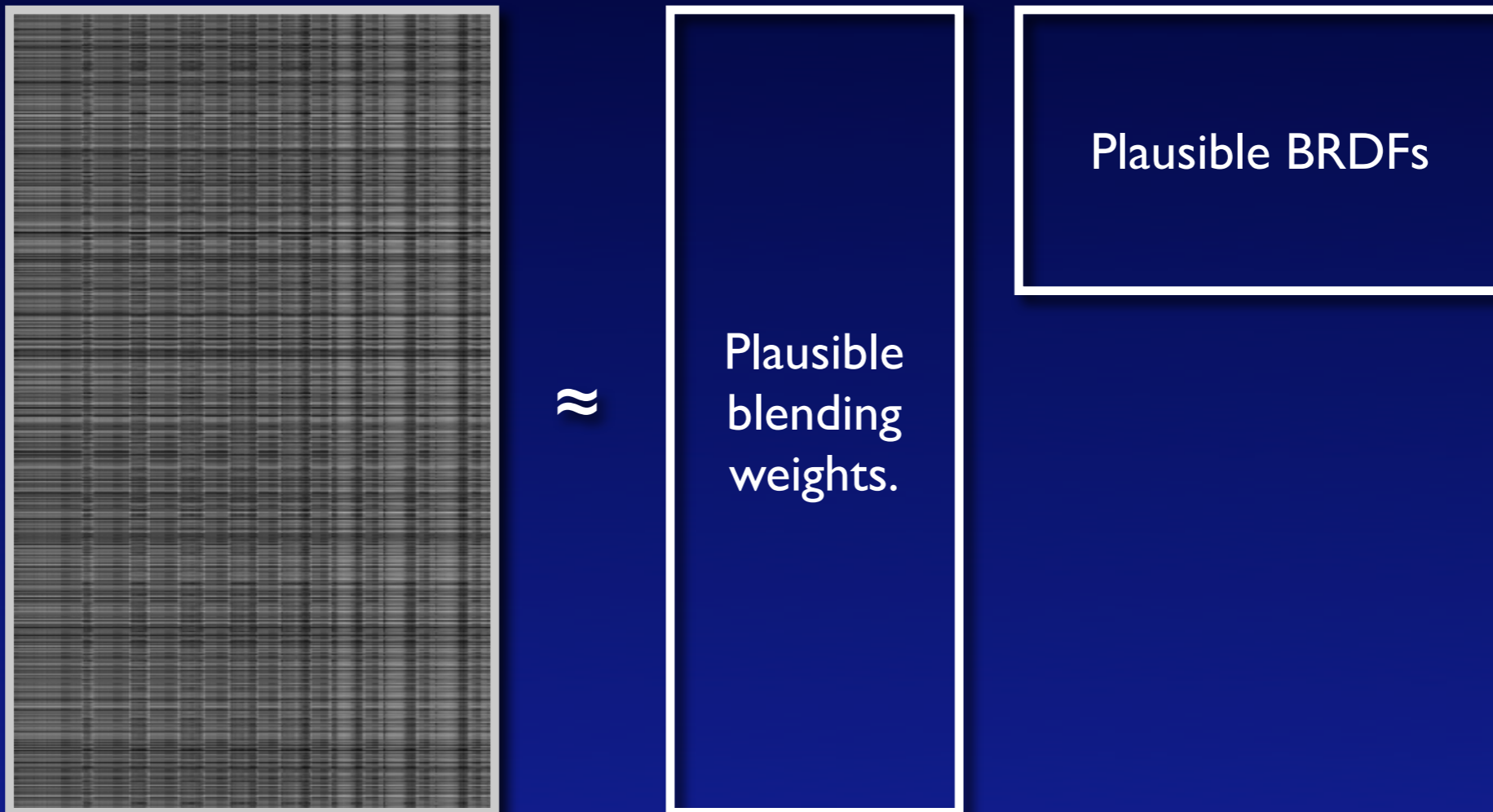
# Research Challenge

Providing an intuitive factorization:



# Key Idea

Incorporate domain-specific knowledge as constraints of factorization:



# Factorization Constraints

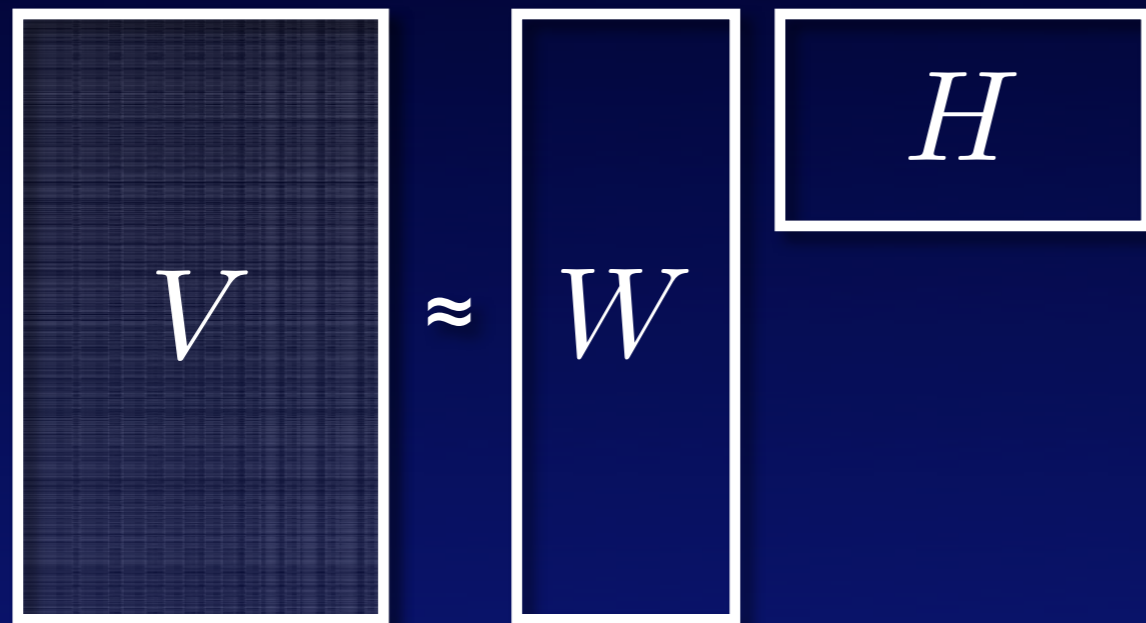
- Non-negativity:  
Reflectance functions are non-negative
- Sparsity:  
Few BRDFs at each position
- Domain-specific:  
Energy-conservation, monotonicity, etc.

# Factorization Algorithms

Algorithm Groups	Properties			
	Linear	Positive	Sparse	Domain
PCA	✓	✗	✗	✗
Clustering	✗	✓	✓	✗
NMF	✓	✓	✗	✗
<b>Our Method</b>	✓	✓	✓	✓

# Our Method

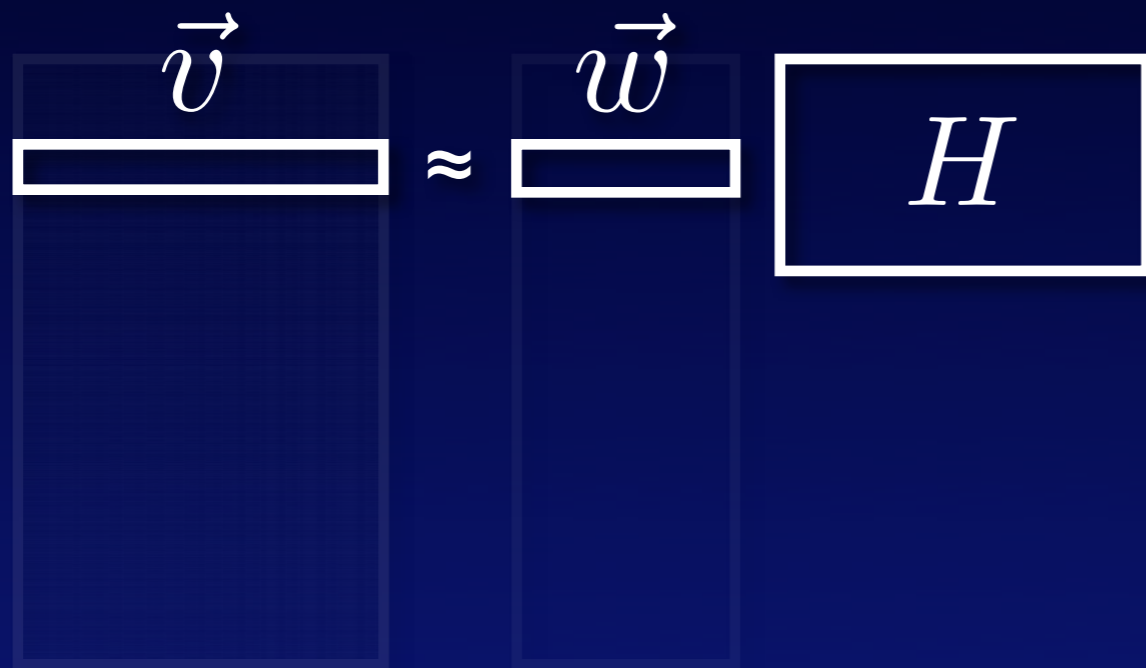
Alternating Constrained Least Squares (ACLS)



1. Initialize  $W$  and  $H$
2. Update  $W$
3. Update  $H$
4. Iterate until convergence

# Our Method

## Alternating Constrained Least Squares (ACLS)



## Convex QP Problem

$$\min_{\vec{w}} \|\vec{v} - \vec{w}H\|^2$$

$$\vec{l} \leq \begin{Bmatrix} \vec{w}^T \\ A\vec{w}^T \end{Bmatrix} \leq \vec{u}$$

1. Initialize  $W$  and  $H$
2. Update  $W$
3. Update  $H$
4. Iterate until convergence

# Appearance Constraints

- Non-negativity  
Value constraint
- Energy conservation  
Constraint on sum
- Monotonicity  
Constraint on derivative

$$\vec{l} \leq \left\{ \begin{array}{c} \vec{w}^T \\ A\vec{w}^T \end{array} \right\} \leq \vec{u}$$



# Appearance Constraints

- Non-negativity


Value constraint

- Energy conservation

Constraint on sum


- Monotonicity

Constraint on derivative


$$\vec{l} \leq \begin{Bmatrix} \vec{w}^T \\ A\vec{w}^T \end{Bmatrix} \leq \vec{u}$$

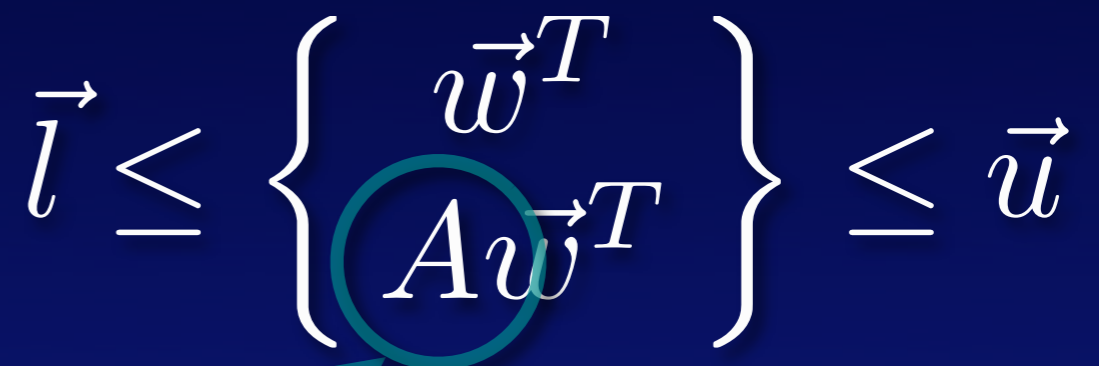
# Appearance Constraints

- Non-negativity  
Value constraint
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Constraint on sum
- Monotonicity  
Constraint on derivative

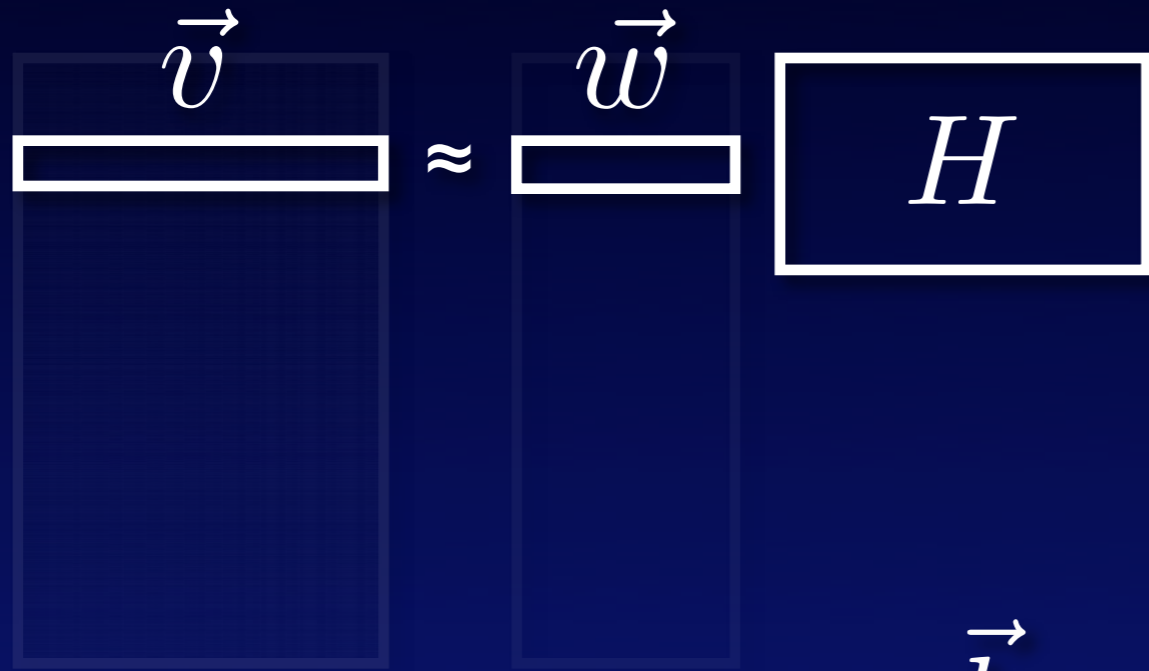
$$\vec{l} \leq \left\{ \begin{array}{c} \vec{w}^T \\ A\vec{w}^T \end{array} \right\} \leq \vec{u}$$


# Appearance Constraints

- Non-negativity  
Value constraint
- Energy conservation  
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Constraint on derivative

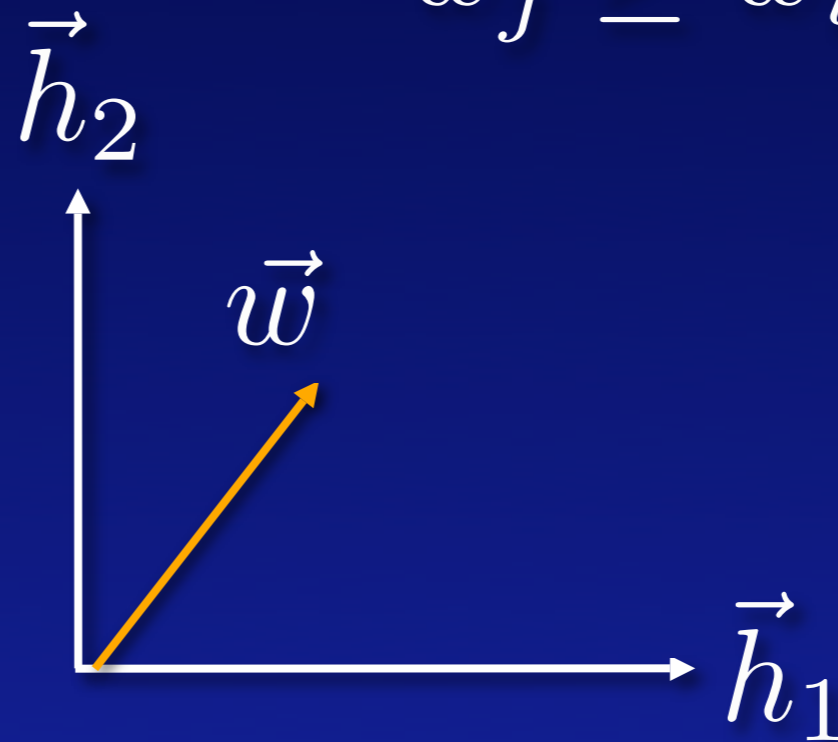
$$\vec{l} \leq \left\{ \begin{array}{c} \vec{w}^T \\ A\vec{w}^T \end{array} \right\} \leq \vec{u}$$


# Measure of Sparsity

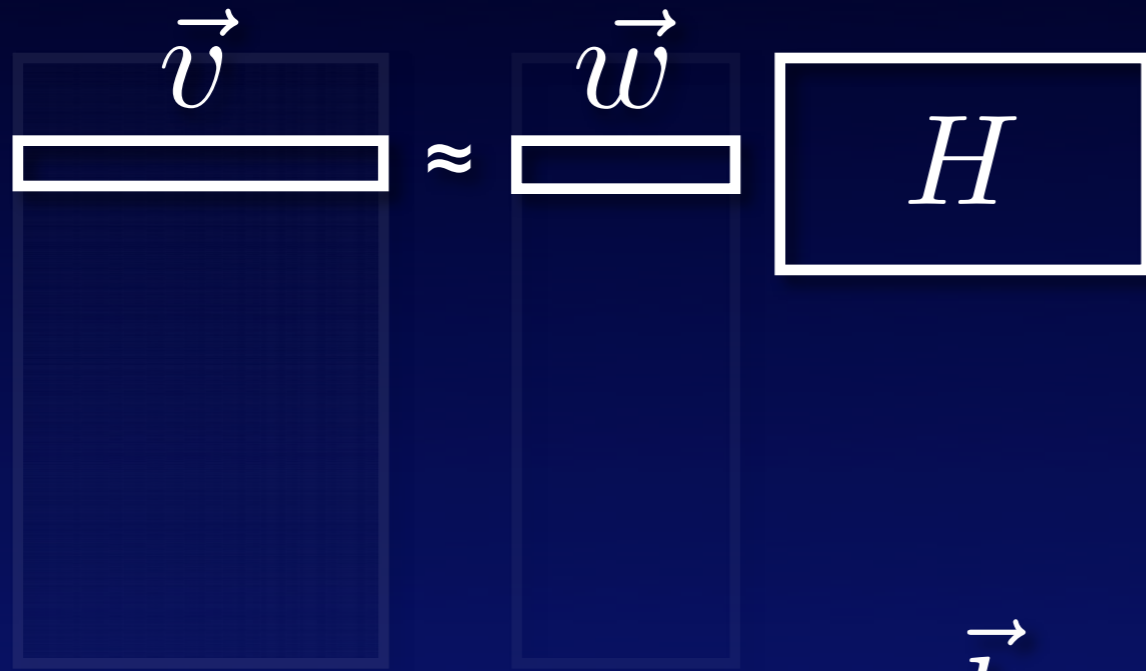


$$E_{sparse} = \sum_{i \neq j} w_i$$

$$w_j \geq w_i, i = 1 \dots K$$

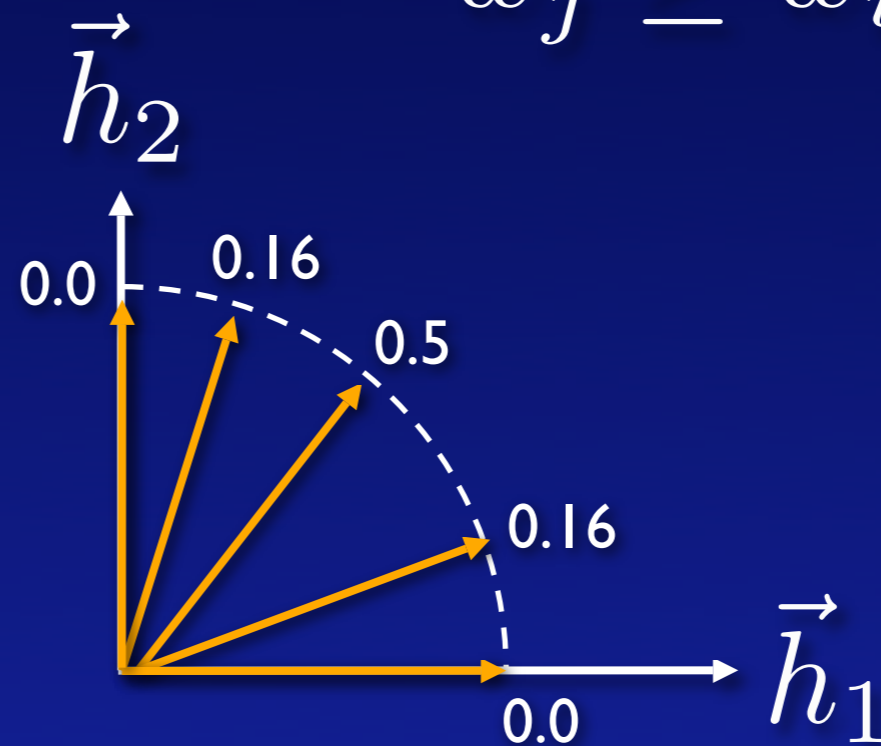


# Measure of Sparsity



$$E_{sparse} = \sum_{i \neq j} w_i$$

$$w_j \geq w_i, i = 1 \dots K$$



# Season's Greetings Dataset

5 Camera Positions 5 Camera Positions ~ 1,750 Images



Gold Foil

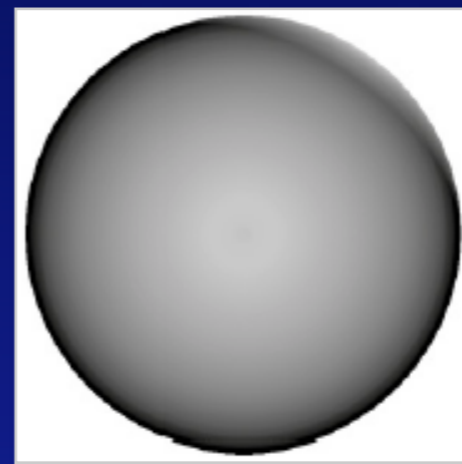
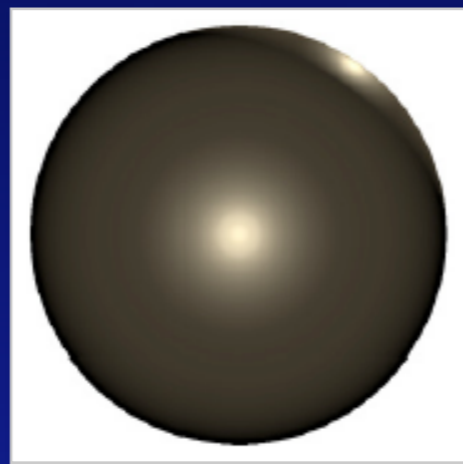
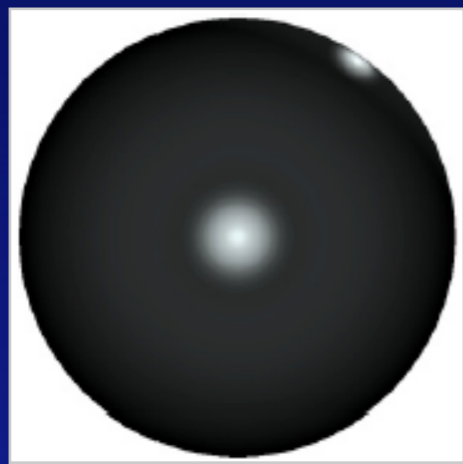
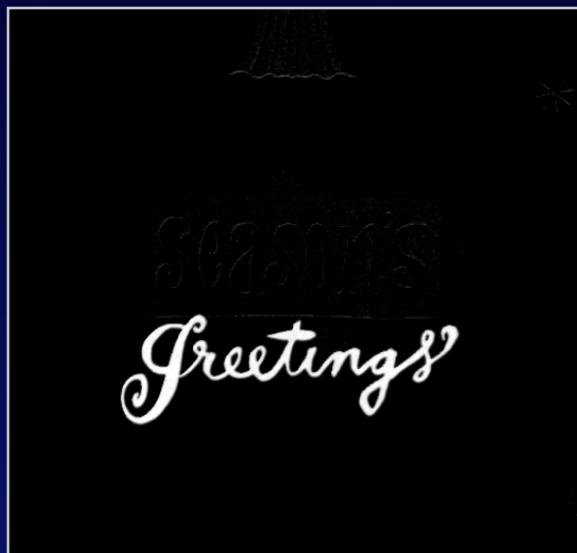
Silver Foil

White Paper

Blue Paper

# Season's Greetings Dataset

Factorization Computed with **ACLS** (4 Terms)



Silver Foil

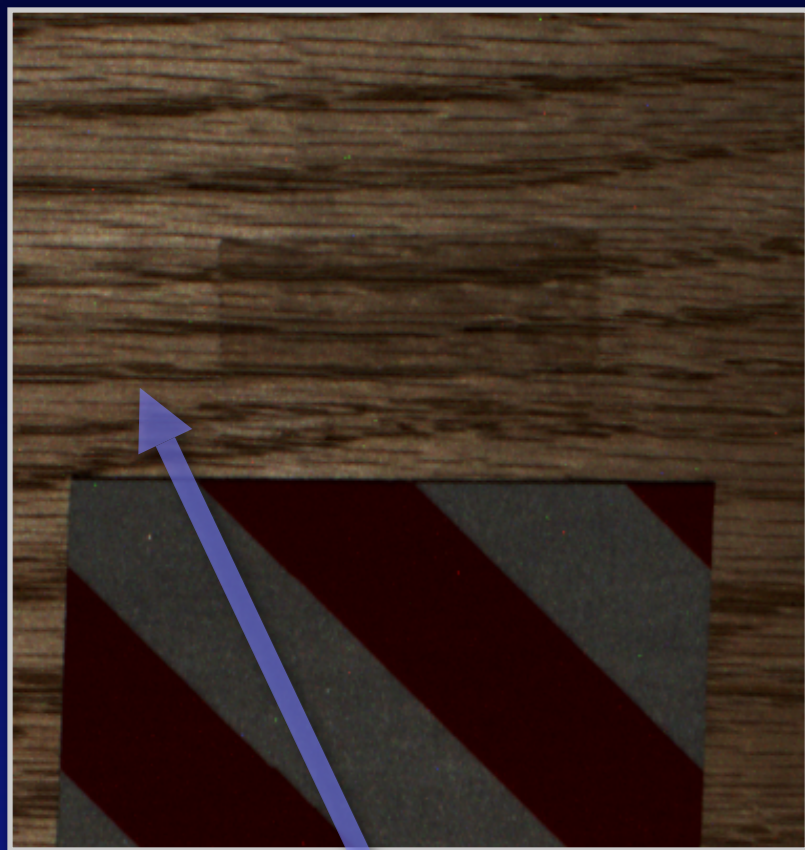
Gold Foil

White Paper

Blue Paper

# Wood+Tape Dataset

12 Camera Positions x 480 Light Positions = 6,000 Images



Oak Wood  
(Anisotropic)



Semi-Transparent  
Tape



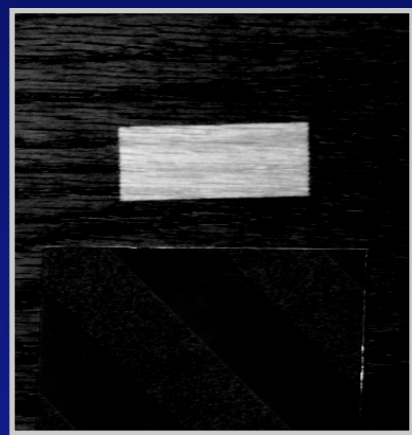
Retroreflective  
Bicycle Tape



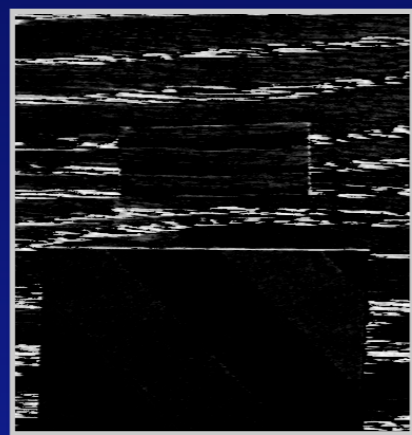
# Wood+Tape Dataset



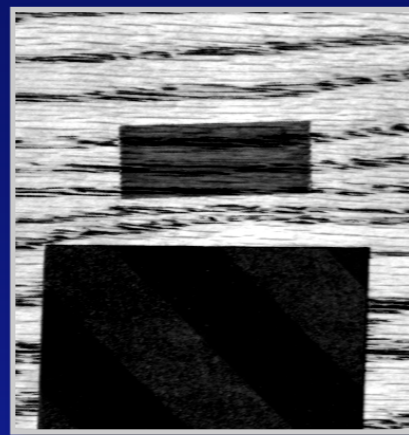
Blending Weights from **ACLS** (5 Terms)



Scotch Tape



Dark Grain



Light Grain

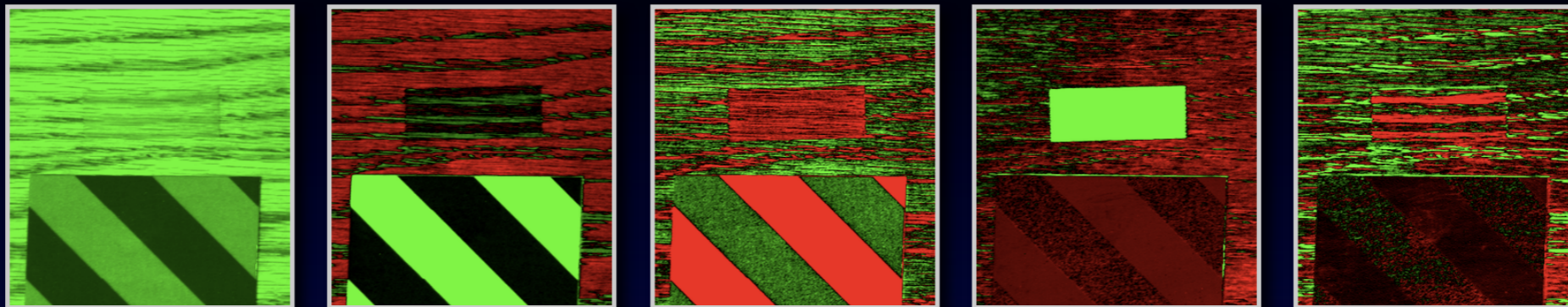


Red Bicycle



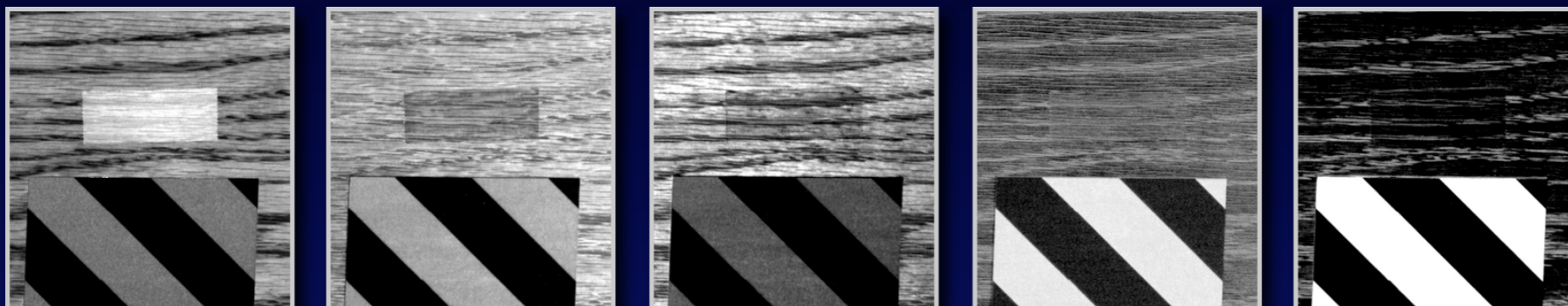
White Bicycle

SVD



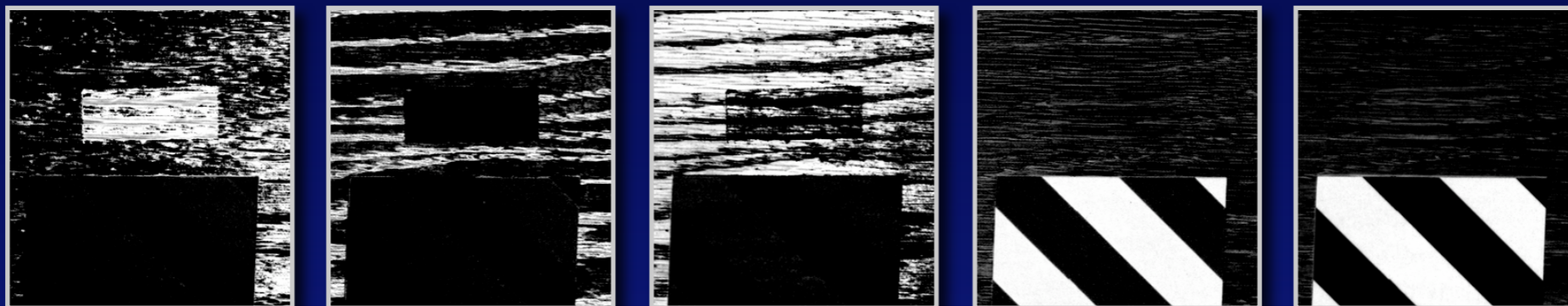
0.014  
(RMS)

NMF



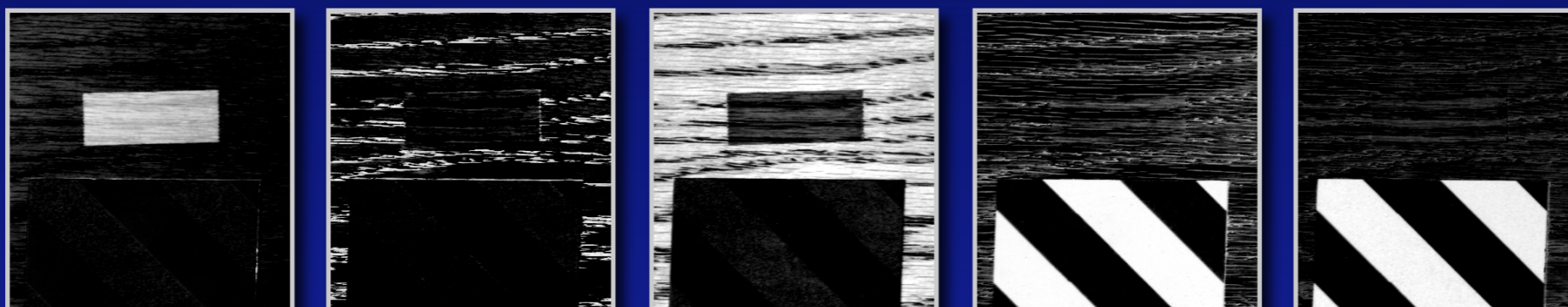
0.015

k-means



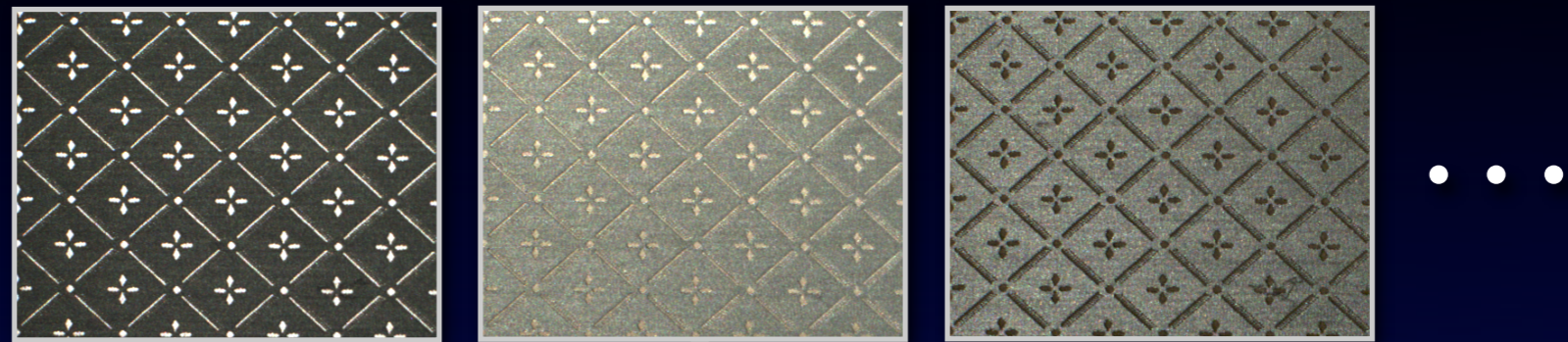
0.029

ACLS



0.022

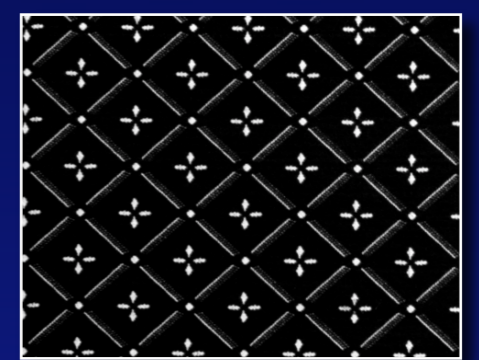
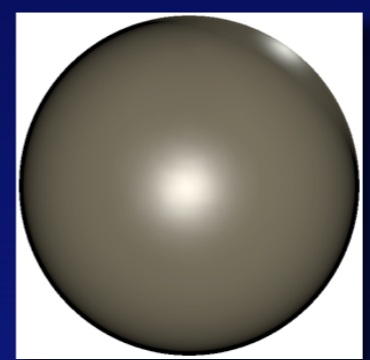
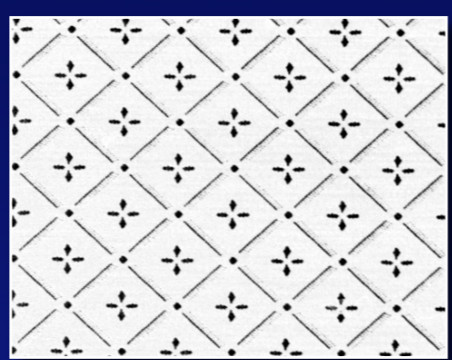
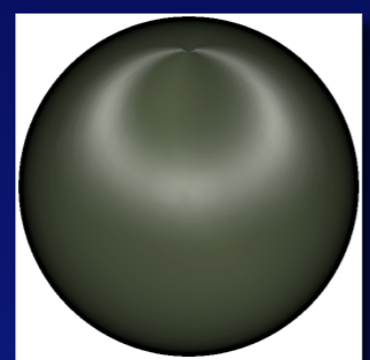
6D SVBRDF



$\Sigma$

$\times$

$\times$



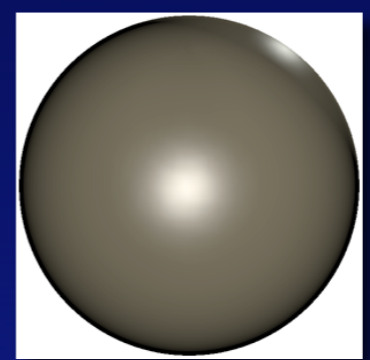
2D Blending  
Weights

4D Basis  
BRDFs

6D SVBRDF

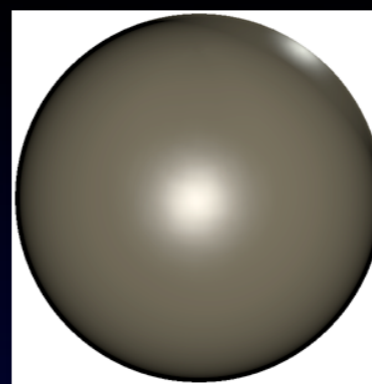


2D Blending  
Weights

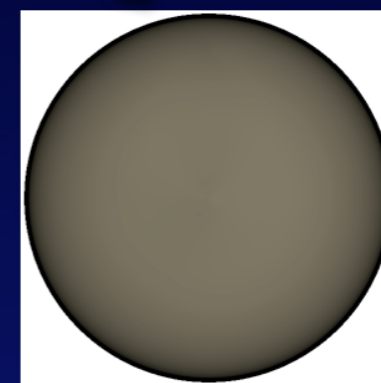
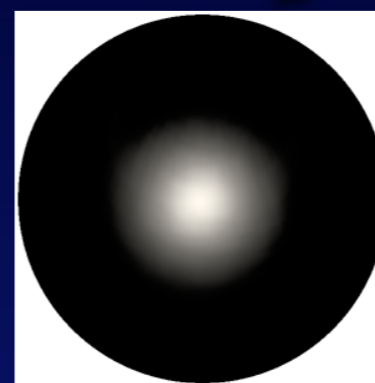


4D Basis  
BRDFs

BRDF  
4D

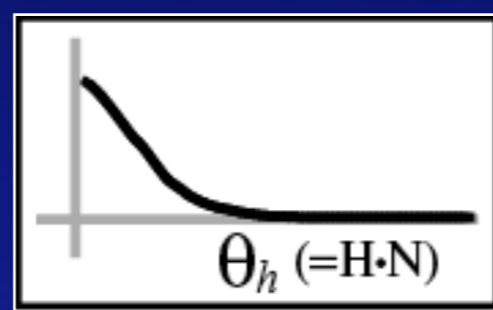
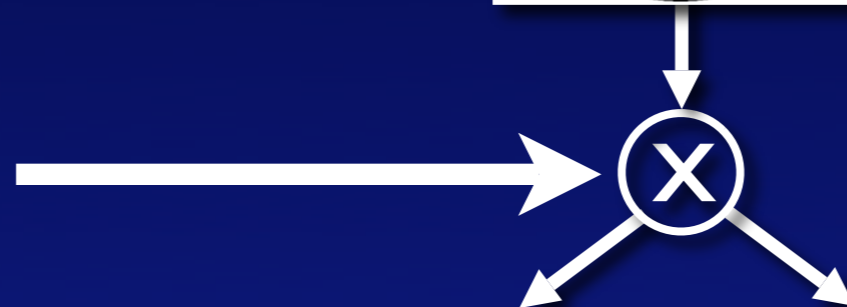


Reparamaterization  
and Constrained  
Factorization

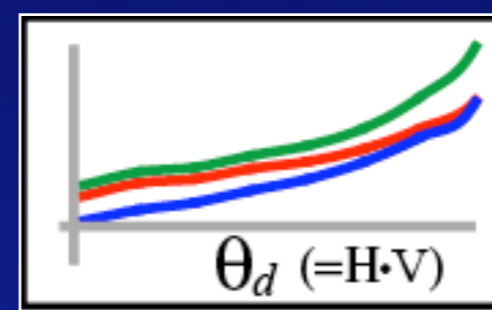


“Lobes”

Single Term  
Factorization



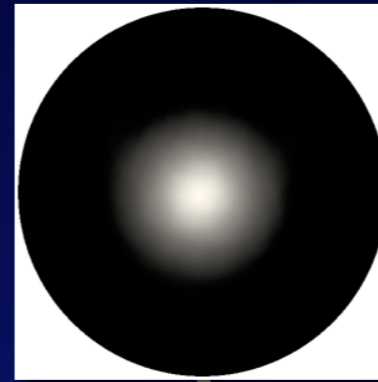
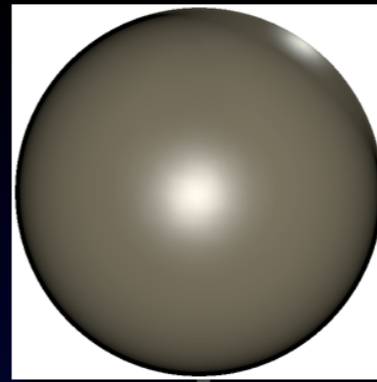
Specular Highlight



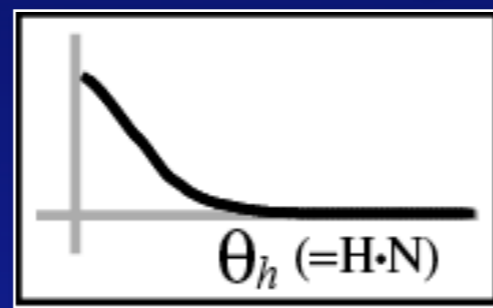
Grazing Effects

Curves  
ID

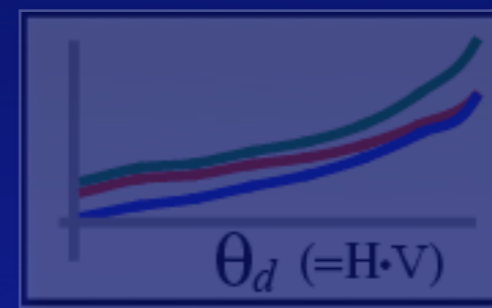
BRDF  
4D



“Lobes”

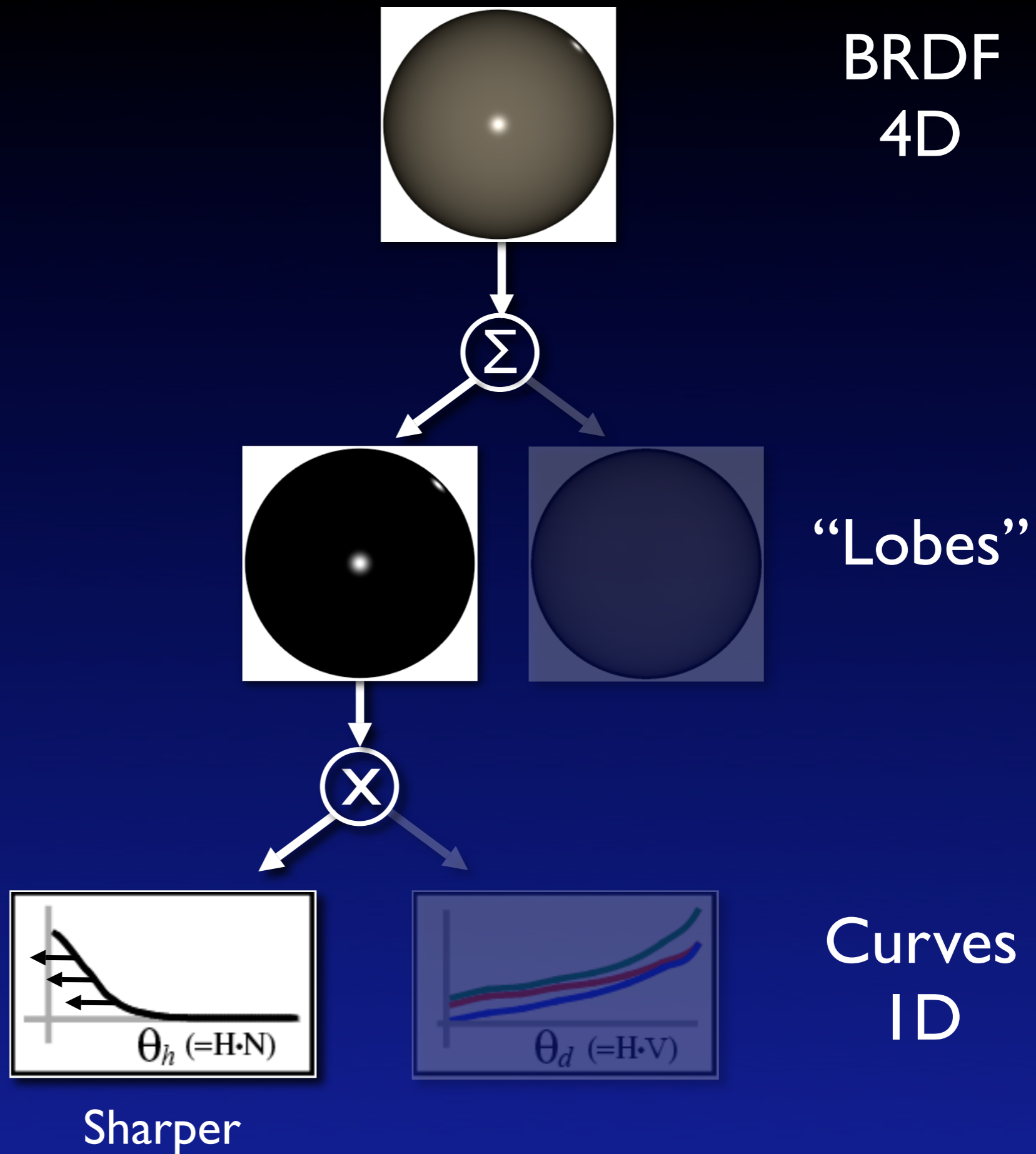


Original



Curves  
ID

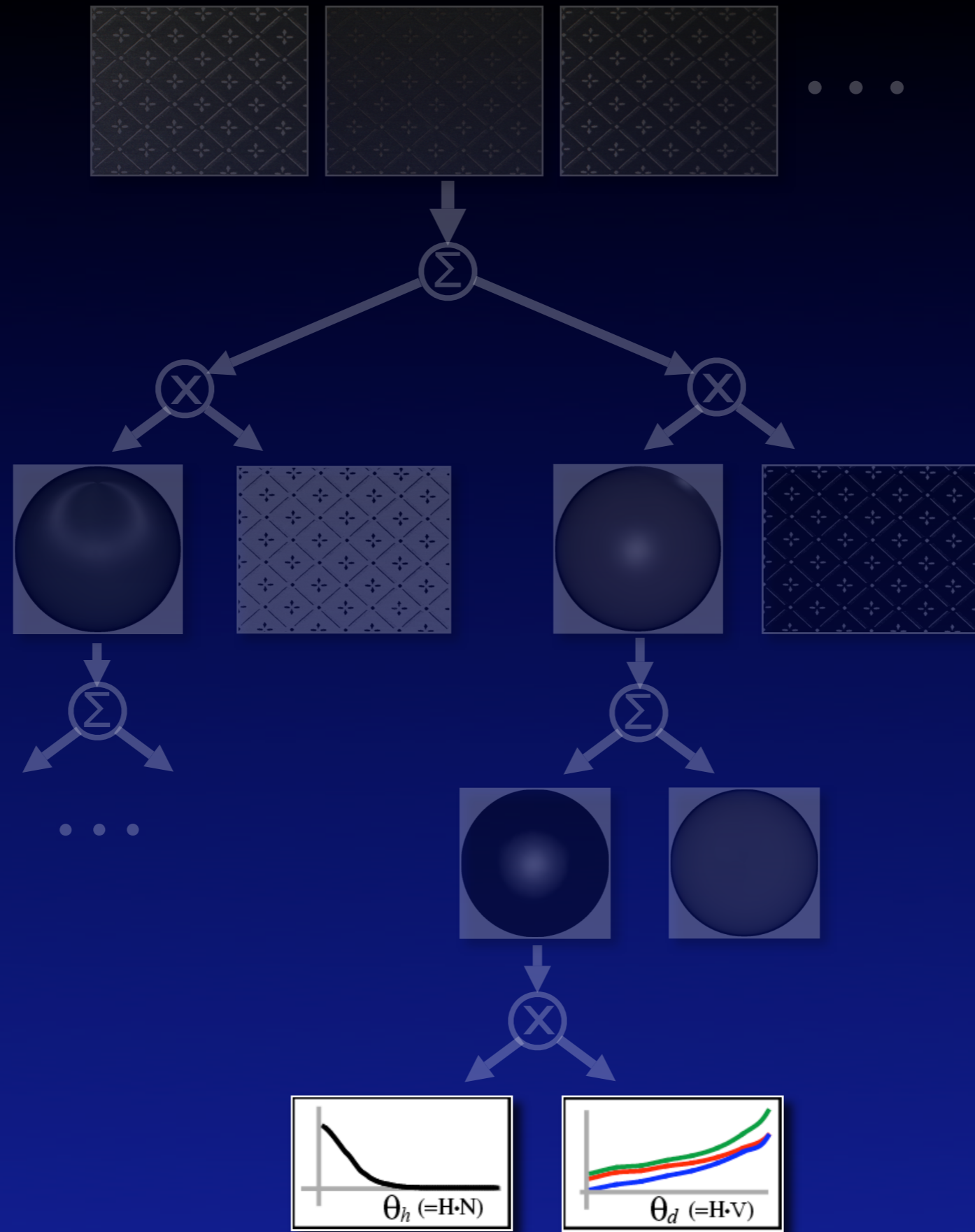
Edits at leaf  
propagate  
up the tree.



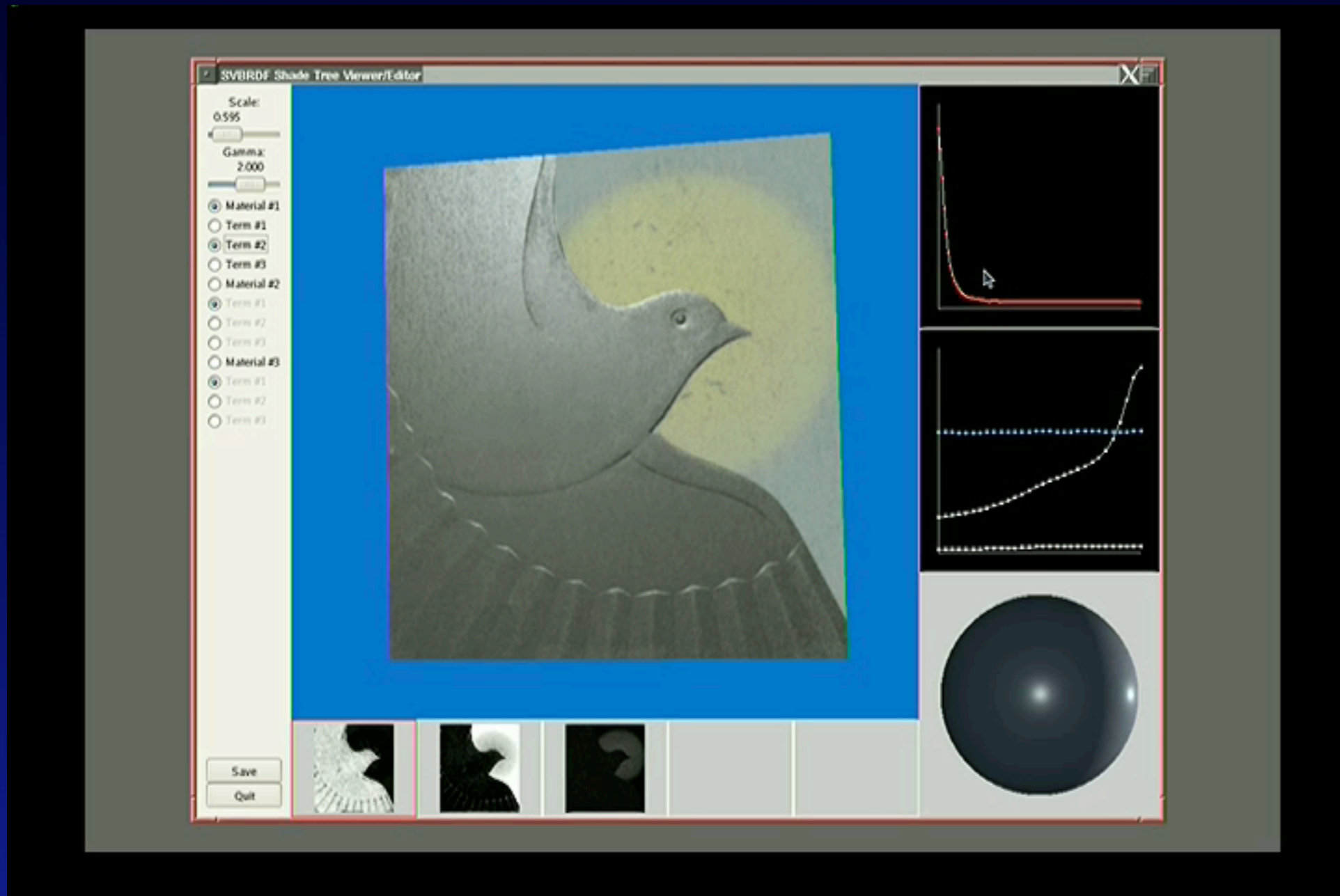
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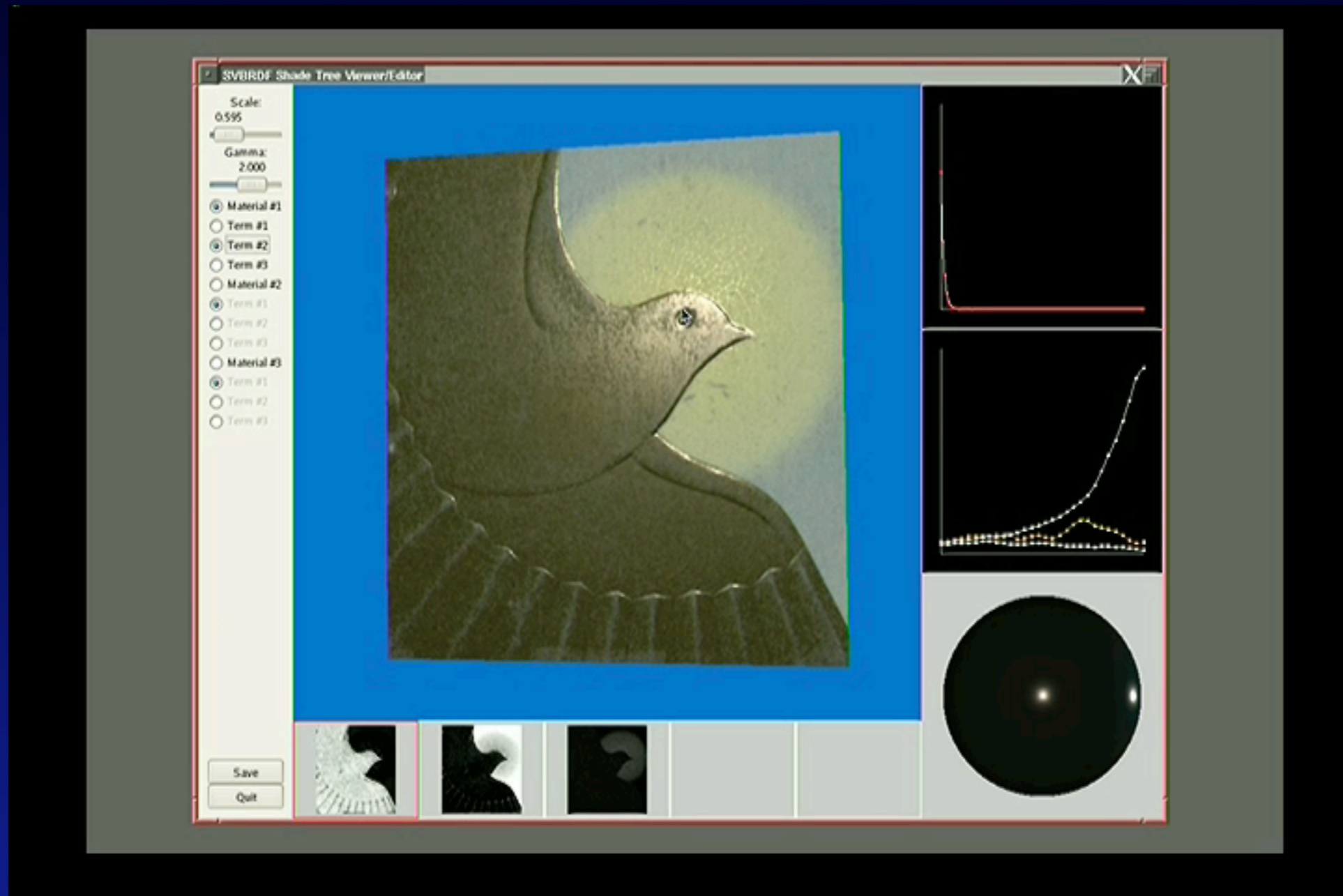


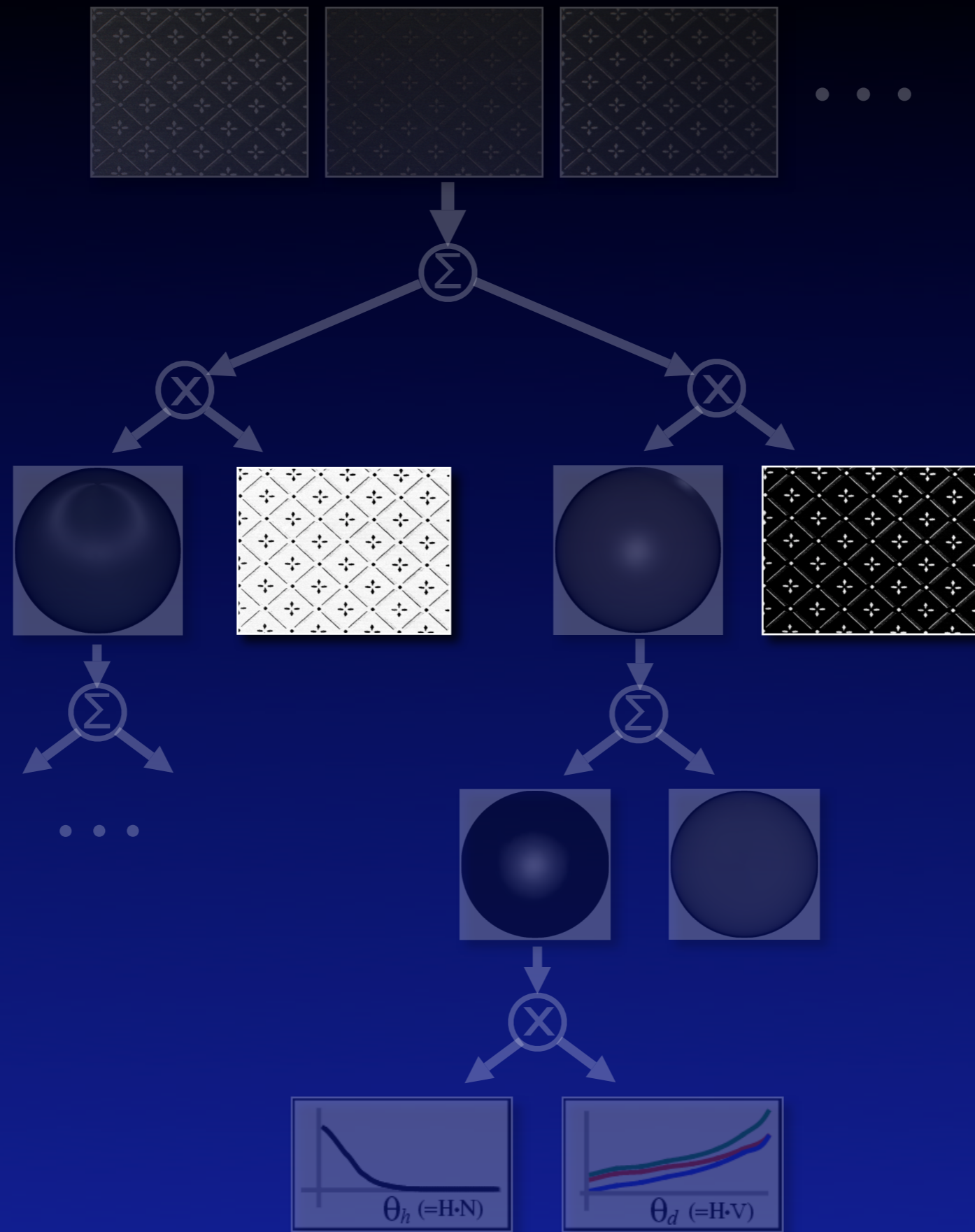


# Specular Highlight Edit

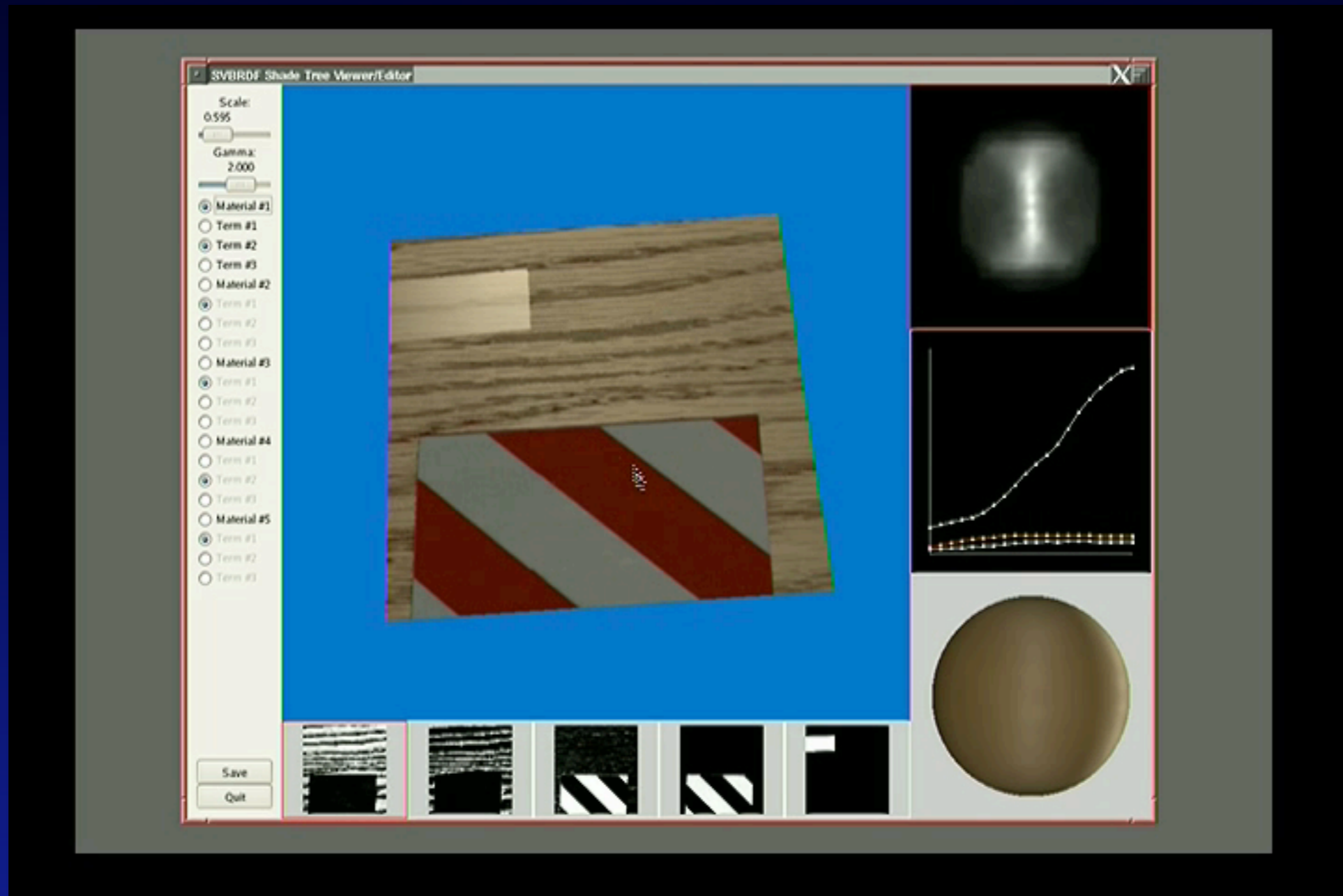


# Material Replacement





# Blending Weights Edit



# Outline

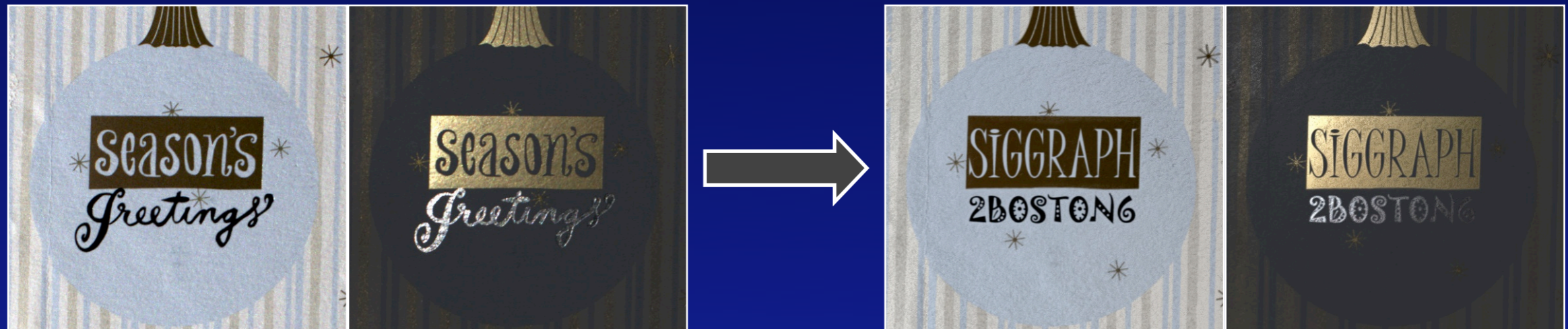
- Introduction
- Prior Work
- Factorization
- Editing
- **Conclusions and Future Work**

# Conclusion

Inverse Shade Trees enable applications with measured appearance data:

Compression for interactive rendering

Editing of texture and reflectance



# Concurrent Work



Translucent  
[Peers et al. 06]



Time-Varying  
[Gu et al. 06]



# Future Work

- Automatic selection of tree topology
- Additional composition nodes:  
(e.g. over operators, masks, etc.)
- Higher-dimensional light transport functions
- Other linear decomposition problems

# Acknowledgements

- Funding:
  - NSF grants CCF-0347427, CCF-0305322 and CCF-0446916
  - Sloan Foundation
- Data:
  - Steve Marschner and the Cornell Graphics Laboratory
  - Tim Weyrich
- Discussions:
  - Marc Levoy
  - Steve Marschner
  - SIGGRAPH reviewers
  - TIGGRAPH reviewers

# Thank You

<http://ist.cs.princeton.edu>