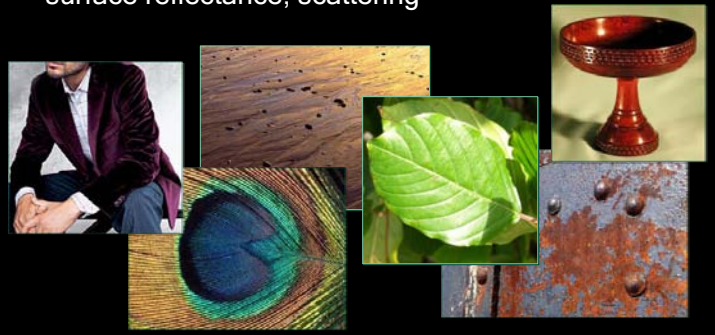


Radiometry and Appearance Models

Szymon Rusinkiewicz
Princeton University

The Visual World

Rich variety of **materials**: characterized by surface reflectance, scattering

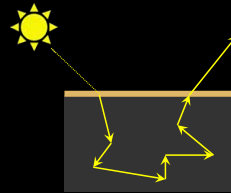


Understanding Reflectance



for each position:
for each direction of incident light:
for each reflected direction:
how much light is reflected?

Understanding Scattering



for each incident position:
for each exitant position:
how much light is scattered?

Motivation

- Understanding appearance models aids in:
 - Photorealistic image synthesis
 - Image-based view and lighting interpolation
 - 3D reconstruction from images
 - Image interpretation
 - Understanding human material perception

Overview

- Radiometry and Radiometric Units
- BRDF properties and common BRDFs
- Subsurface scattering
- Taxonomy of reflection and scattering functions

Radiometric Units

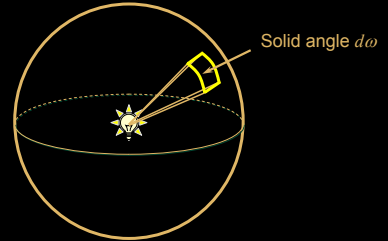


- Light is a form of energy - measured in Joules (J)
- Power: energy per unit time
 - Measured in Joules/sec = Watts (W)
 - Also called Radiant Flux (Φ)

Point Light in a Direction



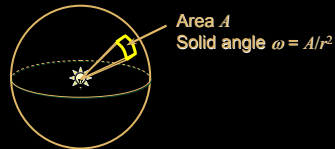
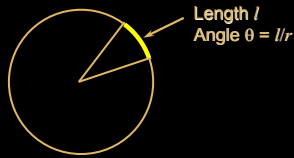
- Total radiant flux in Watts
- How to define angular dependence?
 - Solid angle



Digression – Solid Angle



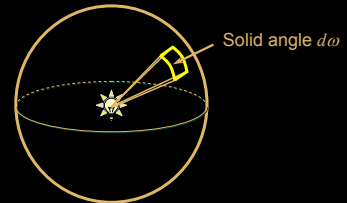
- Angle in radians
- Solid angle in steradians



Point Light in a Direction



- Total radiant flux in Watts
- How to define angular dependence?
 - Solid angle



- Radiant flux per unit solid angle
 - Measured in Watts per steradian (W/sr)

Light Falling on a Surface



- Power per unit area - Irradiance (E)
 - Measured in W/m²
- Move surface away from light
 - Inverse square law: $E \sim 1/r^2$



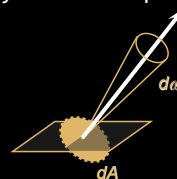
- Tilt surface away from light
 - Cosine law: $E \sim \mathbf{n} \cdot \mathbf{l}$



Light Emitted from a Surface in a Direction



- Power per unit area per unit solid angle - Radiance (L)
 - Measured in W/m²/sr
 - Projected area - perpendicular to given direction



$$L = \frac{d\Phi}{dA d\omega}$$

- Cameras (and our eyes) “see” radiance

Surface Reflectance – BRDF



- Bidirectional Reflectance Distribution Function

$$f_r(\omega_i \rightarrow \omega_o) = \frac{dL_o(\omega_o)}{dE_i(\omega_i)}$$

- 4-dimensional function: also written as

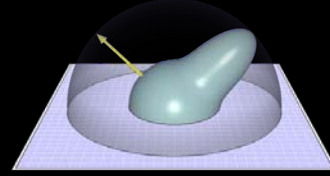
$$f_r(\theta_i, \phi_i, \theta_o, \phi_o) = \frac{dL_o(\omega_o)}{dE_i(\omega_i)}$$

F. E. Nicodemus, J. C. Richmond, J. J. Hsia, and I. W. Ginsberg,
Geometrical Considerations and Nomenclature for Reflectance,
Boulder CO: National Bureau of Standards, 1977.

BRDF



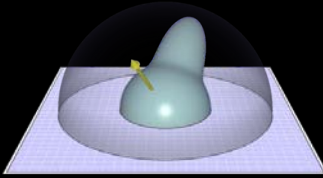
- Radiance/irradiance ratio
 - Directional exitant radiance distribution
 - For each direction of incident irradiance



BRDF



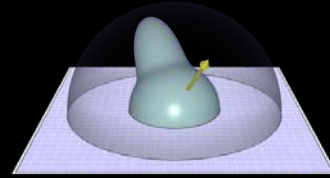
- Radiance/irradiance ratio
 - Directional exitant radiance distribution
 - For each direction of incident irradiance



BRDF



- Radiance/irradiance ratio
 - Directional exitant radiance distribution
 - For each direction of incident irradiance



Properties of the BRDF



- Energy conservation:

$$\int_{\Omega} f_r \cos \theta_o d\omega_o \leq 1$$

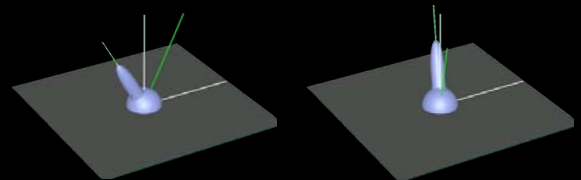
- Helmholtz reciprocity:

$$f_r(\omega_i \rightarrow \omega_o) = f_r(\omega_o \rightarrow \omega_i)$$

Isotropy



- A BRDF is isotropic if it stays the same when surface is rotated around normal



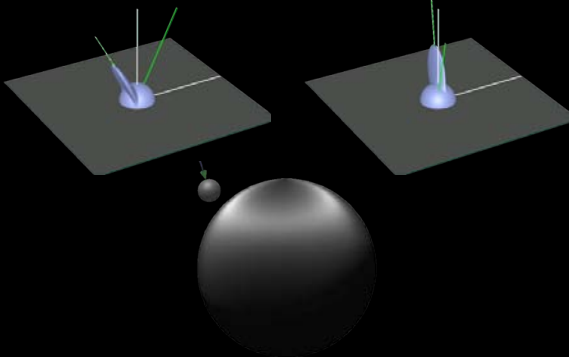
- Isotropic BRDFs are 3-dimensional functions:

$$f_r(\theta_i, \theta_o, \phi_i - \phi_o)$$

Anisotropy



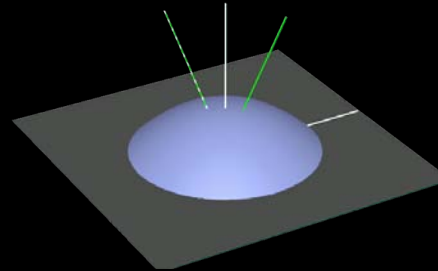
- Anisotropic BRDFs do depend on surface rotation



Other BRDF Features



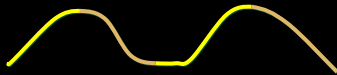
- BRDFs for dusty surfaces scatter light towards grazing angles



Other BRDF Features



- Retroreflection: strong reflection back towards the light source
- Can arise from bumpy diffuse surfaces



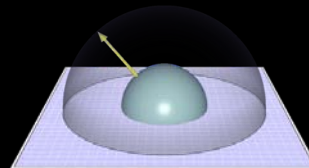
- ... or from corner reflectors



Lambertian BRDF



- Constant BRDF: ideal diffuse reflectance



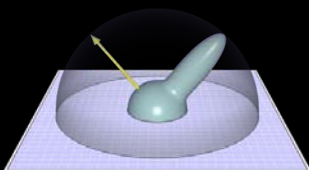
$$f_r = \text{const.} = \frac{\rho}{\pi}$$



Blinn-Phong BRDF



- Simple BRDF describing specular reflection



$$f_r = \frac{\rho}{\pi} + k_s (n \cdot h)^\alpha$$



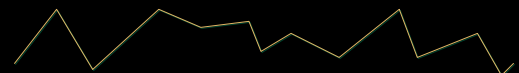
Torrance-Sparrow BRDF



- Physically-based BRDF model
 - Originally used in the physics community

$$f_r = \frac{DGF}{\pi \cos \theta_i \cos \theta_o}$$

- Assume surface consists of tiny "microfacets" with mirror reflection off each



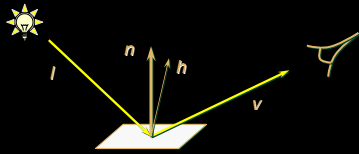
Torrance-Sparrow BRDF



- D term is distribution of microfacets (i.e., how many are pointing in each direction)
- Beckmann distribution

$$D = \frac{e^{-[(\tan \beta)/m]^2}}{4m^2 \cos^4 \beta}$$

β is angle between n and h
 h is halfway between l and v
 m is "roughness" parameter

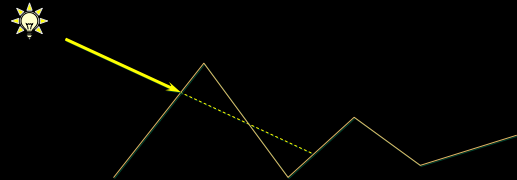


Torrance-Sparrow BRDF



- G term accounts for self-shadowing

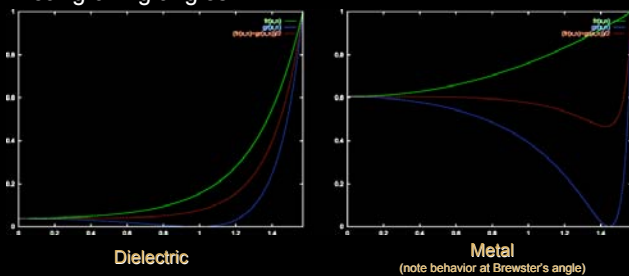
$$G = \min \left\{ 1, \frac{2(n \cdot h)(n \cdot v)}{(v \cdot h)}, \frac{2(n \cdot h)(n \cdot l)}{(v \cdot h)} \right\}$$



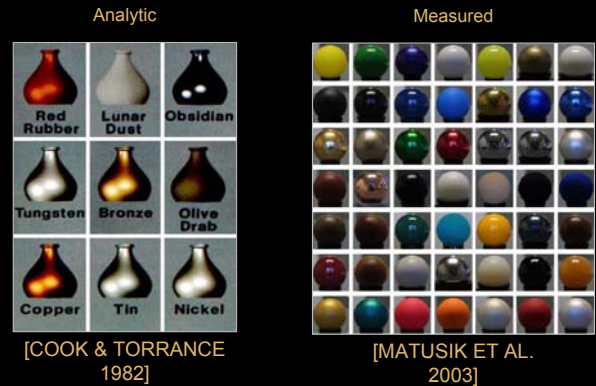
Torrance-Sparrow BRDF



- F is Fresnel term - reflection from an ideal smooth surface (solution of Maxwell's equations)
- Consequence: most surfaces reflect (much) more strongly near grazing angles



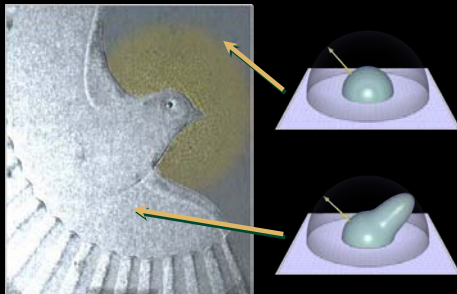
Complex BRDF Models



The SVBRDF: 6D



Spatially-Varying
 Bi-Directional
 Reflectance
 Distribution
 Function



Bidirectional Texture Functions



- For non-flat samples, datasets include effects due to occlusion, shadowing
 - Often called *Bidirectional Texture Functions* - BTFs



Translucent Materials



Surface reflection only



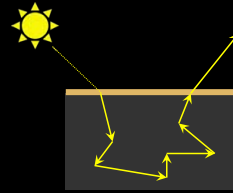
With subsurface scattering

[PEERS ET AL. 2004]

Subsurface Scattering



- Translucency: light no longer leaves surface at point of incidence
 - Not a BRDF!



The BSSRDF



- The Bidirectional Scattering-Surface Reflection Distribution Function

$$S(x_i, y_i, \theta_i, \phi_i, x_o, y_o, \theta_o, \phi_o)$$

- Generalization of spatially-varying BRDF

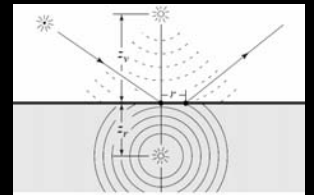
BSSRDF Simplification



- BSSRDF often dominated by multiple scattering
- Accurately modeled by **diffusion** approximation

$$S = F(\theta_i) R(\|x_i - x_o\|) F'(\theta_o)$$

- Angular behavior described by Fresnel equations
- Spatial behavior equivalent to a dipole



BSSRDF Dipole Model



Surface reflection only



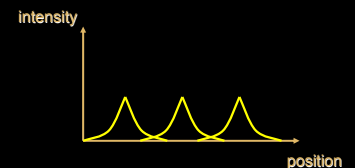
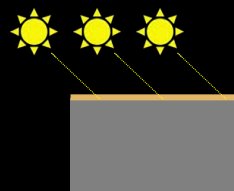
With subsurface scattering

[WANN JENSEN ET AL. 2004]

BSSRDF: Homogeneous



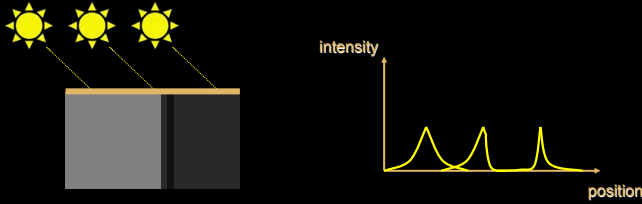
- Homogeneous: uniform material



BSSRDF: Heterogeneous



- Homogeneous: uniform material
- Heterogeneous: spatially-varying materials



Heterogeneous Scattering



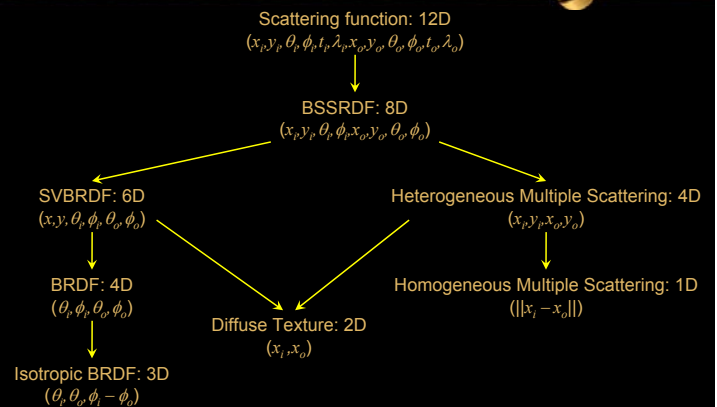
[PEERS ET AL. 2006]

Generalizing Further



- Many additional effects could be incorporated into appearance functions: add 1 dimension for each
 - Wavelength
 - Fluorescence
 - Time dependence
 - Phosphorescence

Appearance Taxonomy



Rest of This Tutorial



- A Review of Radiometry & Physical Models – *Rusinkiewicz*
- Principles of Acquisition – *Zickler*
- (Spatially Varying) BRDF Models – *Lawrence*
- From BSSRDFs to 8D Reflectance Fields – *Lensch*
- The Human Face Scanner Project – *Weyrich*
- Future Directions / Q&A

Principles of Acquisition

Todd Zickler
Harvard University

Outline

1. 5D: Homogeneous Reflectance (BRDF)
2. 7D: Spatially-varying Reflectance (SV-BRDF)
3. 9D: Subsurface Scattering (BSSRDF)
4. Calibration
5. Open problems

Balancing Needs

1. (Per-object) Acquisition Time
2. Accuracy and Precision
3. Cost
4. Generality: how broad is the class of surfaces being considered?

Homogeneous Reflectance

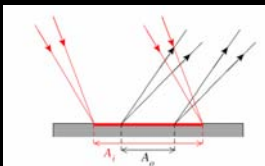
- BRDF: Five dimensional domain

$$f(\lambda, \vec{\omega}_i, \vec{\omega}_o) = f(\lambda, \theta_i, \phi_i, \theta_o, \phi_o)$$
- Isotropic BRDF: Four dimensional domain

$$f(\lambda, \theta_i, \theta_o, |\phi_i - \phi_o|)$$

BRDF: Measurement Scale

- One measures *averages* of the BRDF over finite intervals of surface area and solid angle.
- The measurement scale must be appropriate for the BRDF model to be valid (more on this later).



The Gonioreflectometer

Four-axis gonioreflectometer

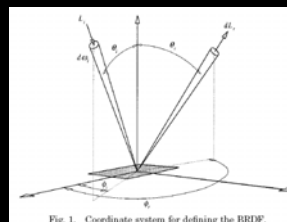
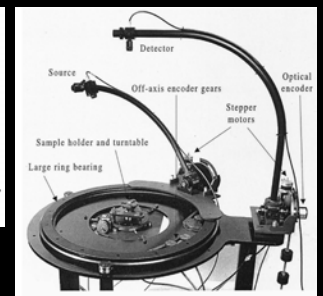


Fig. 1. Coordinate system for defining the BRDF.



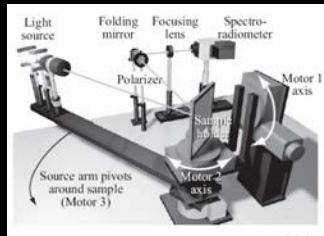
[White et al., 1998]

The Gonioreflectometer



Three-axis gonioreflectometer

- Isotropic BRDF
- 1000 angular samples
- 31 spectral samples
- ~10 hours per BRDF

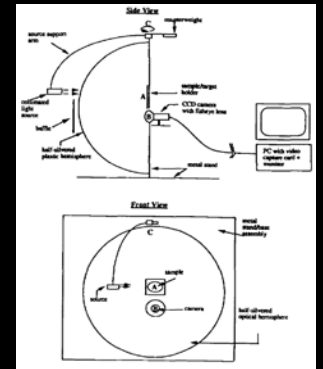


[Li et al., 2005]

Image-based measurement: planar

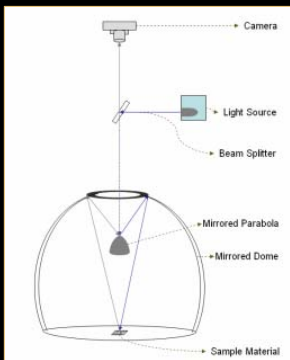


- Camera: Observe multiple output angles simultaneously
- Trade precision (and accuracy?) for efficiency



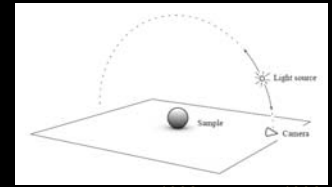
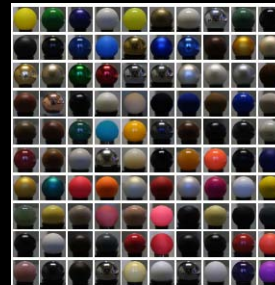
[Ward, 1992]

Image-based measurement: planar



[Ghosh et al., 2007]

Image-based measurement: curved

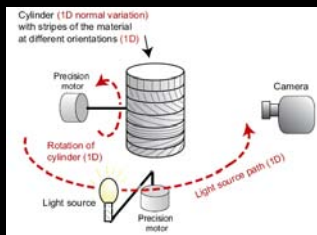


[Marschner, 1998; Lu et al., 1998]

[Matusik et al., 2003]

[<http://www.merl.com/brdf/>]

Image-based measurement: curved



[Ngan et al., 2005]

Image-based measurement: general



[Marschner et al., 1999]

Outline



1. 5D: Homogeneous Reflectance (BRDF)
2. 7D: Spatially-varying Reflectance (SV-BRDF)
3. 9D: Subsurface Scattering (BSSRDF)
4. Calibration
5. Open problems

Spatially-varying Reflectance

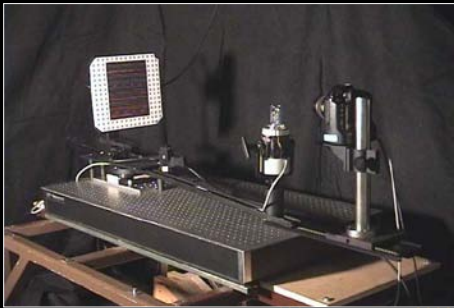


- SV-BRDF: Seven dimensional domain
$$f(\lambda, \vec{x}, \vec{\omega}_i, \vec{\omega}_o) = f(\lambda, x, y, \theta_i, \phi_i, \theta_o, \phi_o)$$
- Isotropic SV-BRDF: Six dimensional domain
$$f(\lambda, x, y, \theta_i, \theta_o, |\phi_i - \phi_o|)$$

Planar Surfaces: The Spatial Gonioreflectometer



Three-axis spatial gonioreflectometer

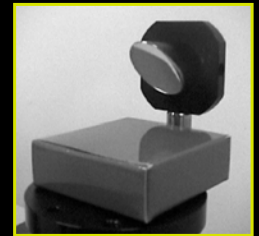
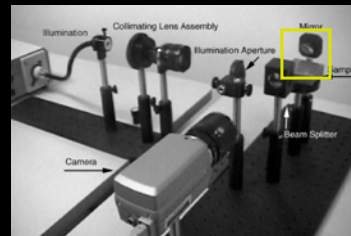


[Dana et al., 1997; McAllister, 2002]

Planar Surfaces: Another Spatial Gonioreflectometer



- Can use catadioptrics to re-sort light rays and exchange spatial and angular resolution.

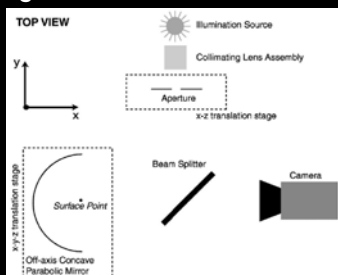
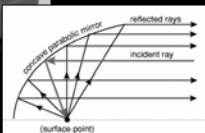


[Dana et al., 2004]

Planar Surfaces: Another Spatial Gonioreflectometer



- Can use catadioptrics to re-sort light rays and exchange spatial and angular resolution.



[Dana et al., 2004]

Curved Surfaces

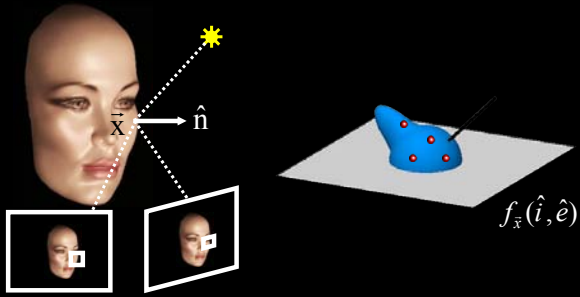


- Many interesting surfaces are not planar.
- Non-planar shapes can be used, provided the shape is known.



[Stanford Spherical Gantry]
(also Cornell, UVA, UCSD,...)

Counting Images



5° sampling: 1,000,000 images >10⁶ MB
 1° sampling: 625,000,000 images >10⁹ MB

Counting Images

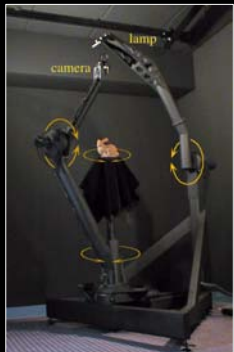


Reduce acquisition time by:

1. Designing efficient acquisition systems
2. Using parametric BRDF models
3. Exploiting common reflectance phenomena

5° sampling: 1,000,000 images >10⁶ MB
 1° sampling: 625,000,000 images >10⁹ MB

Acquisition Systems



[Stanford Graphics]



[USC-ICT]

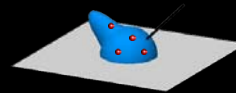


[MERL]

Parametric Approaches



- Pro: requires estimating only a handful of parameters at each surface point.
- Con: requires choice of specific parametric family (Oren-Nayar, Cook-Torrance, Phong,...)



$$f_{\vec{x}}(\hat{i}, \hat{e}) \leftarrow f_{\vec{x}}(\vec{\alpha}_{\vec{x}}; \hat{i}, \hat{e})$$

Parametric Approaches



- Some parametric approaches:
 - [Sato, Wheeler, Ikeuchi, 1997]
 - [Yu et al., 1999]
 - [Boivin, Gagalowicz, 2001]
 - [Lensch, et al., 2001]
 - [McAllister, Lastra, Heidrich, 2002]
 - [Georghades, 2003]
 - [Goldman et al., 2005]
 - ...

General Reflectance Properties



- Isotropy: from a 6D domain to 5D
- Reciprocity: cuts the angular domain in half
- Compressibility: BRDF is slowly varying over much of its angular domain
- Separability: distinct diffuse and specular components
- Spatial smoothness: slow variation from point to point
- Spatial regularity: a common per-object BRDF basis

General Reflectance Properties



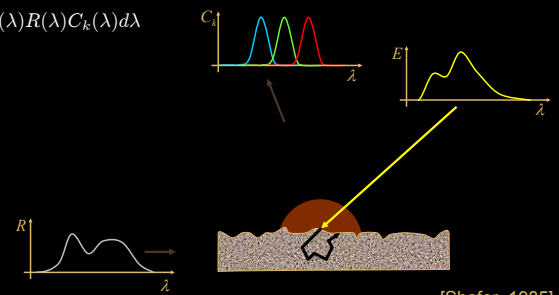
- Isotropy, reciprocity, separability are commonly exploited
- Compressibility
 - Implicit in parametric approaches; used in non-parametric approaches as well
- Spatial smoothness
 - Exploited in parametric (e.g., [Sato, Wheeler, Ikeuchi, 1997]) and non-parametric (e.g., [Zickler et al., 2006]) approaches
- Spatial regularity
 - Exploited in parametric (e.g., [Lensch et al., 2001], [Goldman et al. 2005]) and non-parametric (e.g., [Lawrence et al., 2006]) approaches

Separability (Dichromatic Model)



$$\mathbf{I}_{RGB} = (\hat{\mathbf{n}} \cdot \hat{\mathbf{i}})\mathbf{D}$$

$$D_k = \int E(\lambda)R(\lambda)C_k(\lambda)d\lambda$$



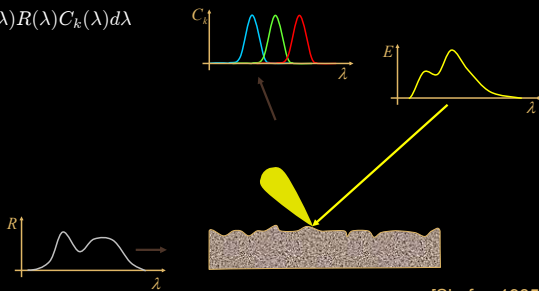
[Shafer, 1985]

Separability (Dichromatic Model)



$$\mathbf{I}_{RGB} = (\hat{\mathbf{n}} \cdot \hat{\mathbf{i}})\mathbf{D}$$

$$D_k = \int E(\lambda)R(\lambda)C_k(\lambda)d\lambda$$



[Shafer, 1985]

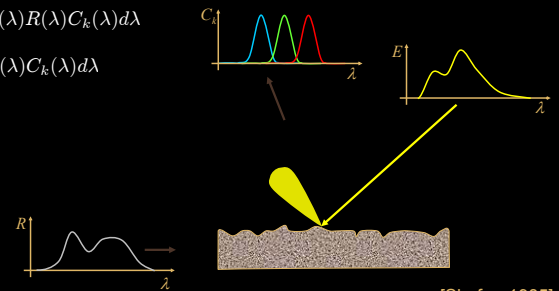
Separability (Dichromatic Model)



$$\mathbf{I}_{RGB} = (\hat{\mathbf{n}} \cdot \hat{\mathbf{i}})\mathbf{D} + f(\hat{\mathbf{n}}, \hat{\mathbf{i}}, \hat{\mathbf{v}})\mathbf{S}$$

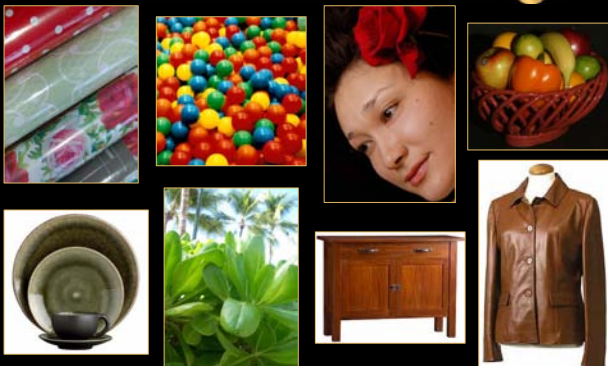
$$D_k = \int E(\lambda)R(\lambda)C_k(\lambda)d\lambda$$

$$S_k = \int E(\lambda)C_k(\lambda)d\lambda$$



[Shafer, 1985]

"Separable" Materials



[Tominga and Wandell, 1989; Healey, 1989; Lee et al., 1990]

Implications for Acquisition



DIFFUSE

SPECULAR

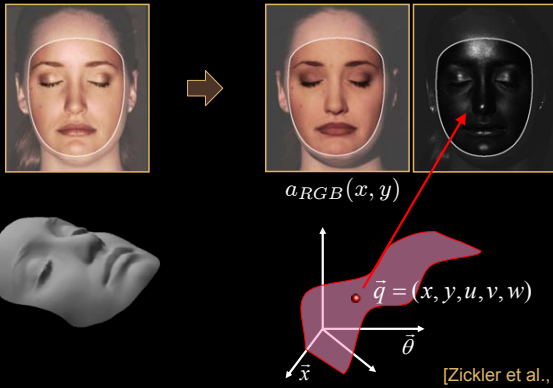
= +

DIFFUSE

SPECULAR

- Approx. Lambertian
- Rapid spatial variation
- Randomly polarized
- Non-Lambertian
- Slow spatial variation
- Monochromatic
- Partially polarized

Example: Reflectance Sharing

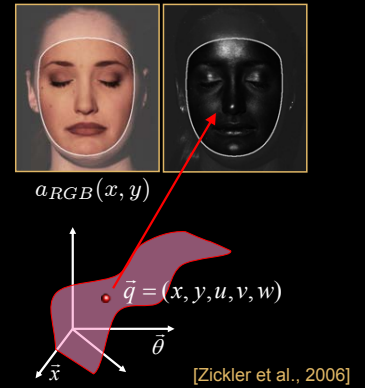


Example: Reflectance Sharing

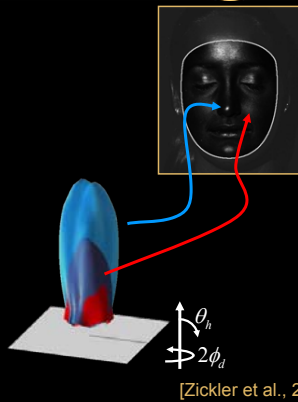


Exploits:

- Separability
- Isotropy/Reciprocity
- Compressibility
- Slow spatial variation



Example: Reflectance Sharing



Outline



1. 5D: Homogeneous Reflectance (BRDF)
2. 7D: Spatially-varying Reflectance (SV-BRDF)
3. 9D: Subsurface Scattering (BSSRDF)
4. Calibration
5. Open problems

Subsurface Scattering

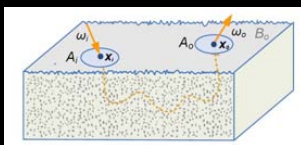


- BSSRDF:

$$S(\lambda, \vec{x}_i, \vec{\omega}_i, \vec{x}_o, \vec{\omega}_o)$$

- Homogeneous, multiple scattering:

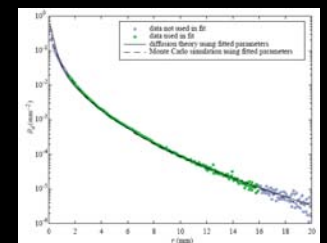
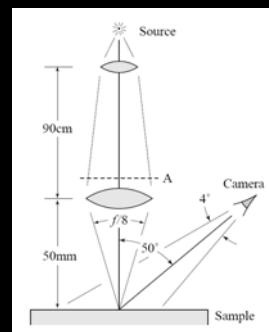
$$F_t(\eta, \vec{\omega}_i)R(\lambda, \|\vec{x}_i - \vec{x}_o\|)F_t(\eta, \vec{\omega}_o)$$



BSSRDF



$$F_t(\eta, \vec{\omega}_i)R(\lambda, \|\vec{x}_i - \vec{x}_o\|)F_t(\eta, \vec{\omega}_o)$$

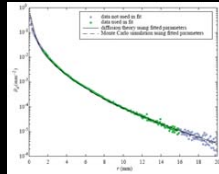


[Jensen et al., 2001]

BSSRDF



Material	σ_s (mm ⁻¹)			σ_a (mm ⁻¹)			Diffuse Reflectance			η
	R	G	B	R	G	B	R	G	B	
Apple	2.29	2.39	1.97	0.0030	0.0034	0.046	0.85	0.84	0.53	1.3
Chicken1	0.15	0.21	0.38	0.015	0.077	0.19	0.31	0.15	0.10	1.3
Chicken2	0.19	0.25	0.32	0.018	0.088	0.20	0.32	0.16	0.10	1.3
Cream	7.38	5.47	3.15	0.0002	0.0028	0.0163	0.98	0.90	0.73	1.3
Ketchup	0.18	0.07	0.03	0.061	0.97	1.45	0.16	0.01	0.00	1.3
Marble	2.19	2.62	3.00	0.0021	0.0041	0.0071	0.83	0.79	0.75	1.5
Potato	0.68	0.70	0.55	0.0024	0.0090	0.12	0.77	0.62	0.21	1.3
Skinmilk	0.70	1.22	1.90	0.0014	0.0025	0.0142	0.81	0.81	0.69	1.3
Skin1	0.74	0.88	1.01	0.032	0.17	0.48	0.44	0.22	0.13	1.3
Skin2	1.09	1.59	1.79	0.013	0.070	0.145	0.63	0.44	0.34	1.3
Spectralon	11.6	20.4	14.9	0.00	0.00	0.00	1.00	1.00	1.00	1.3
Wholemilk	2.55	3.21	3.77	0.0011	0.0024	0.014	0.91	0.88	0.76	1.3

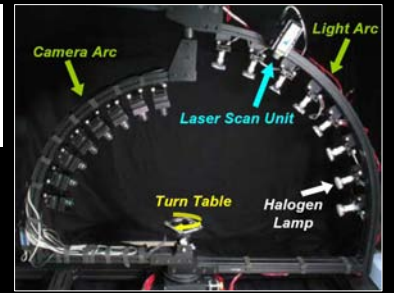
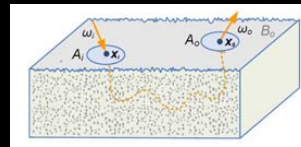


[Jensen et al., 2001]

BSSRDF

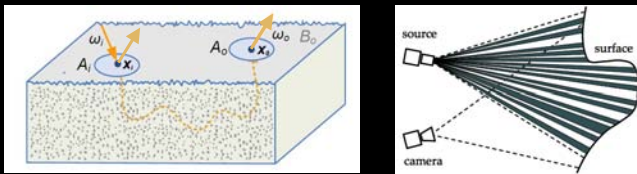


$$S(\lambda, \vec{x}_i, \vec{\omega}_i, \vec{x}_o, \vec{\omega}_o) = f_i(\vec{\omega}_i) R_d(\vec{x}_i, \vec{x}_o) f_o(\vec{x}_o, \vec{\omega}_o)$$



[Tong et al., 2005]

Direct/Sub-surface Separation



[Nayar et al., 2006]

Outline

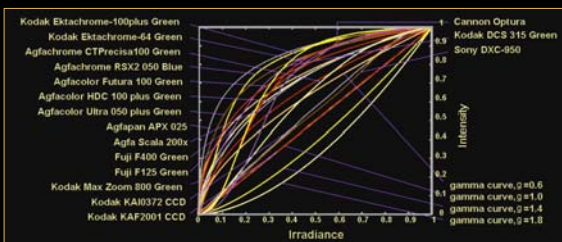


1. 5D: Homogeneous Reflectance (BRDF)
2. 7D: Spatially-varying Reflectance (SV-BRDF)
3. 9D: Subsurface Scattering (BSSRDF)
4. Calibration
5. Open problems

Radiometric Calibration



- Camera:
 - Response function and high dynamic range (HDR) imaging



[Grossberg and Nayar, 2003]

Radiometric Calibration



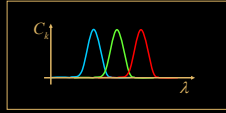
- Camera:
 - Response function and high dynamic range (HDR)
 - Optical fall-off



Radiometric Calibration



- Camera:
 - Response function and high dynamic range (HDR)
 - Optical fall-off
 - Spectral filters



Radiometric Calibration



- Camera:
 - Response function and high dynamic range (HDR)
 - Optical fall-off
 - Spectral filters
 - Thermal noise (at least)

Radiometric Calibration



- Light source(s):
 - Temporal variation
 - Angular non-uniformity
 - Spectral power distribution
- Projector(s):
 - Optical fall-off
 - Spectral filters

Geometric Calibration



- Camera/projector parameters (intrinsic/extrinsic)
- Source direction
- Surface Shape. Ideally:
 - Surface normals (Photometric stereo; Helmholtz stereo)
 - Independent of reflectance
 - Same images used for shape and reflectance



[Debevec et al., 2007]

Some Open Problems



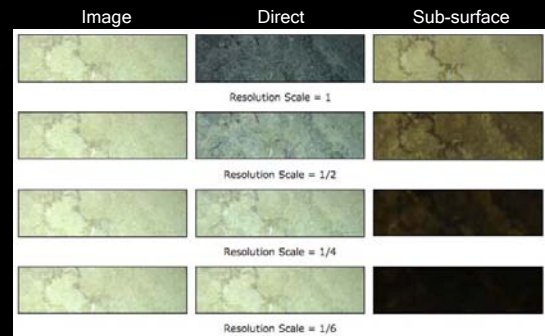
- Automatic scale selection



Some Open Problems



- Automatic scale selection

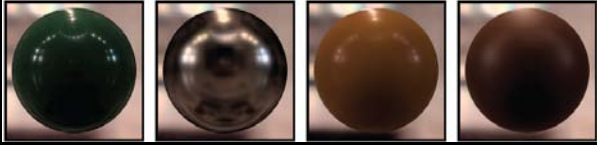


[Nayar et al., 2006]

Some Open Problems



- Automatic scale selection
- Acquisition (inference) in complex lighting environments. [Dror 2001, Ramamoorthi and Hanrahan 2001]



Some Open Problems



- Automatic scale selection
- Acquisition (inference) in complex lighting environments. [Dror 2001, Ramamoorthi and Hanrahan 2001]
- SV-BRDF acquisition as an inference problem. What are the priors?
- Increased spectral resolution
- Combined shape and reflectance acquisition

Spatially-Varying BRDF Models

Jason Lawrence
University of Virginia

A Spatially-Varying BRDF



$$S(u, v, \omega_i, \omega_o)$$

A Spatially-Varying BRDF



$$S(u_1, v_1, \omega_i, \omega_o)$$



$$S(u_0, v_0, \omega_i, \omega_o)$$

Talk Outline

- acquisition
- representations
- future directions

Acquisition



Acquisition



Outline



- acquisition
- representations
- future directions

Representation



- goals
 - compact
 - editable
 - sampling
- challenges
 - scattered data
 - dimensionality
 - massive datasets

Representation



- goals
 - compact
 - editable
 - sampling
- challenges
 - scattered data
 - dimensionality
 - massive datasets

Goal



- input: large set of reflectance measurements
- representation that is compact and editable



input measurements
(1000s of images)



result of editing
material properties

Strategy: Basis Decomposition



$$S(u, v, \omega_i, \omega_o, \lambda) \approx \sum_{k=1}^K T_k(u, v) \rho_k(\omega_i, \omega_o, \lambda)$$

Strategy: Basis Decomposition



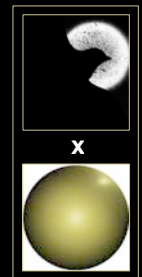
≈



+

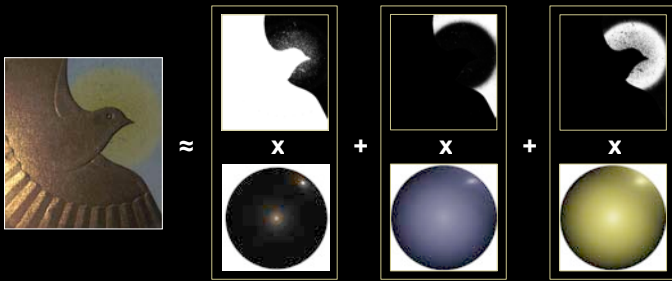


+



$$S(u, v, \omega_i, \omega_o, \lambda) \approx \sum_{k=1}^K T_k(u, v) \rho_k(\omega_i, \omega_o, \lambda)$$

Strategy: Basis Decomposition



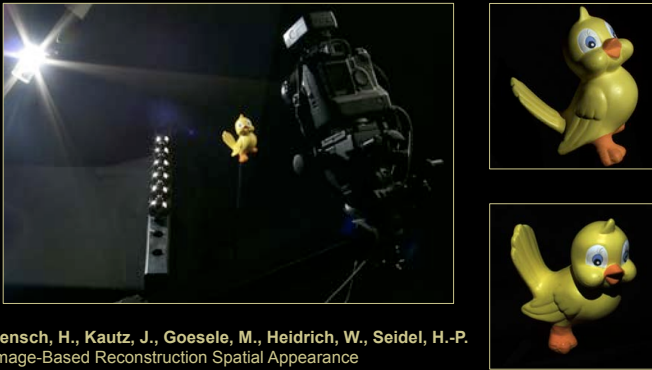
$$S(u, v, \omega_i, \omega_o, \lambda) \approx \sum_{k=1}^K T_k(u, v) \rho_k(\omega_i, \omega_o, \lambda)$$

General Strategy



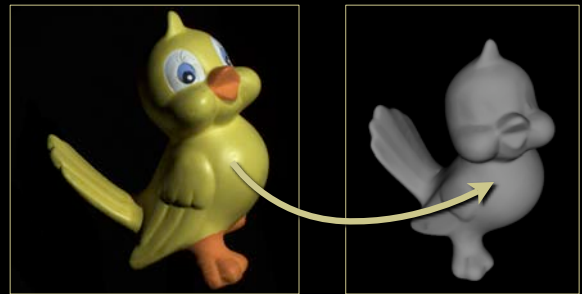
- parametric
 - fit parametric BRDF model
 - cluster
 - reproject onto basis
- non-parametric
 - tabulate the reflectance data
 - cast as matrix factorization
 - place constraints on factors

Acquisition



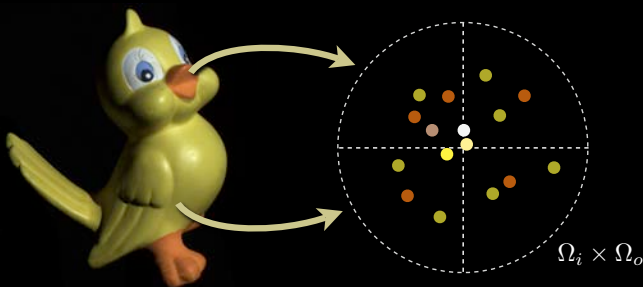
Lensch, H., Kautz, J., Goesele, M., Heidrich, W., Seidel, H.-P.
Image-Based Reconstruction Spatial Appearance
ACM Transactions on Graphics 22(3), 2003

Registration



silhouette-based alignment procedure

Fitting Lafortune Parameters



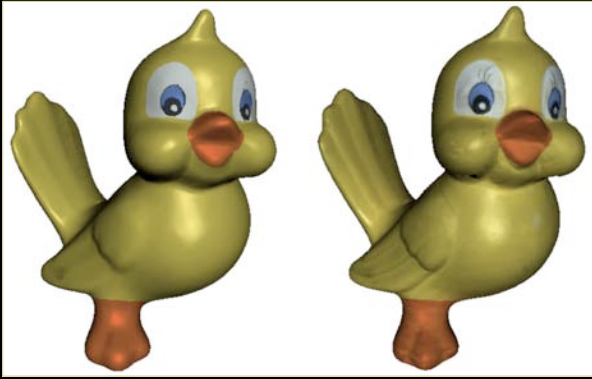
$$\rho(\vec{l}, \vec{v}) = k_d + \sum_i [C_{x,i}(l_x v_x + l_y v_y) + C_{z,i} l_z v_z]^{N_i}$$

Clustering



split / refine

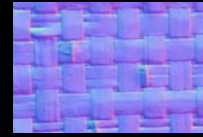
Reprojection



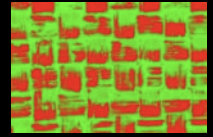
Goldman et al. 2005



one input image



normal map



blending weights +
basis BRDFs (Ward)



reconstruction

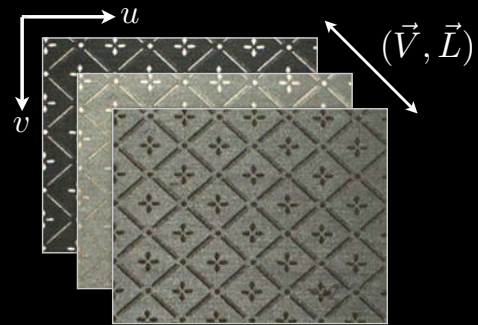
Goldman, D., Curless, B., Hertzmann, A., Seitz, S.
Shape and Spatially Varying BRDFs from Photometric Stereo
Proceedings of ICCV 2005.

General Strategy

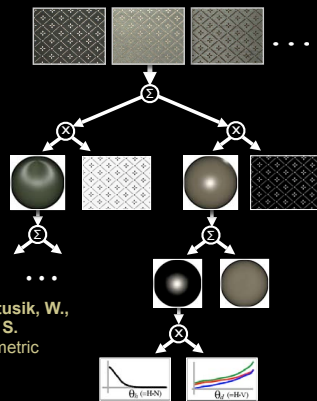


- parametric
 - fit parametric BRDF model
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 - tabulate the reflectance data
 - cast as matrix factorization
 - place constraints on factors

Wallpaper Dataset

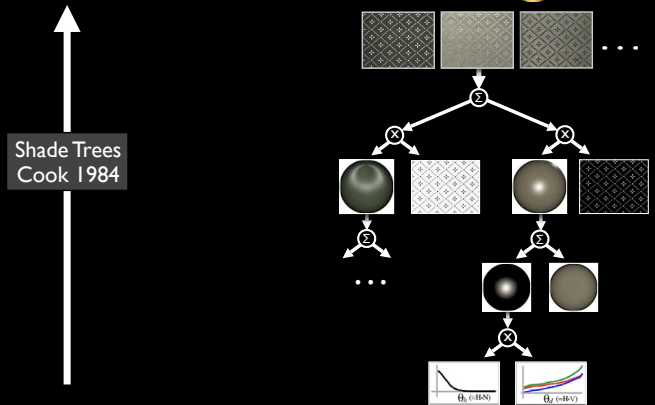


Inverse Shade Trees



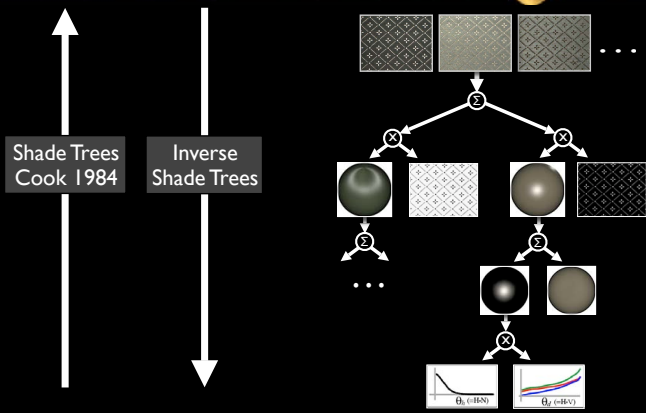
Lawrence, J., Ben-Artzi, A., DeCoro, C., Matusik, W., Pfister, H., Ramamoorthi, R., Rusinkiewicz, S.
Inverse Shade Tree Framework for Non-Parametric Material Representation and Editing
Proceedings of SIGGRAPH 2006.

Inverse Shade Tree Framework



Shade Trees
Cook 1984

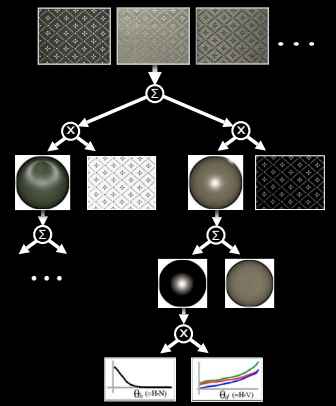
Inverse Shade Tree Framework



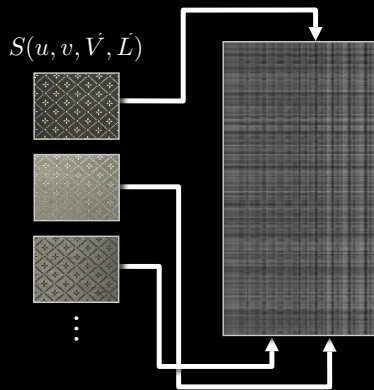
Inverse Shade Tree Framework



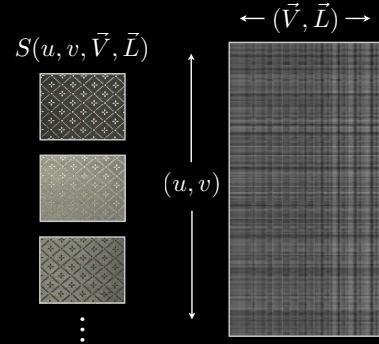
decomposition at each level is cast as matrix factorization



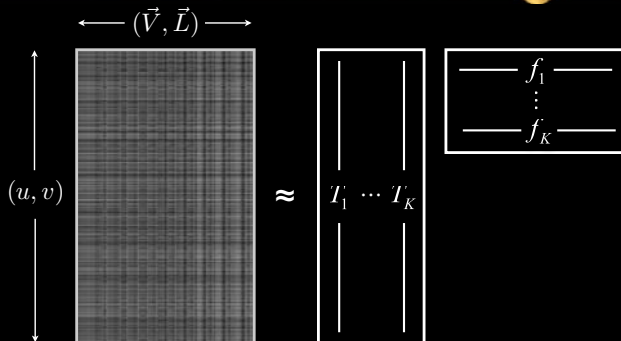
Tabulate Raw Data



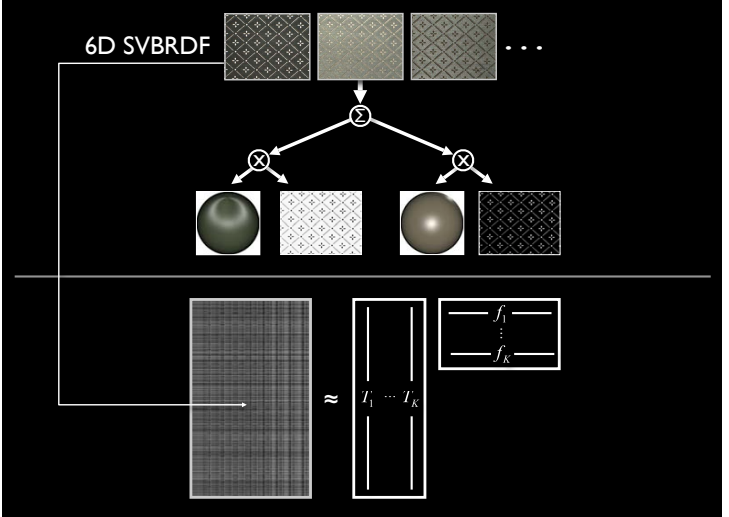
Tabulate Raw Data

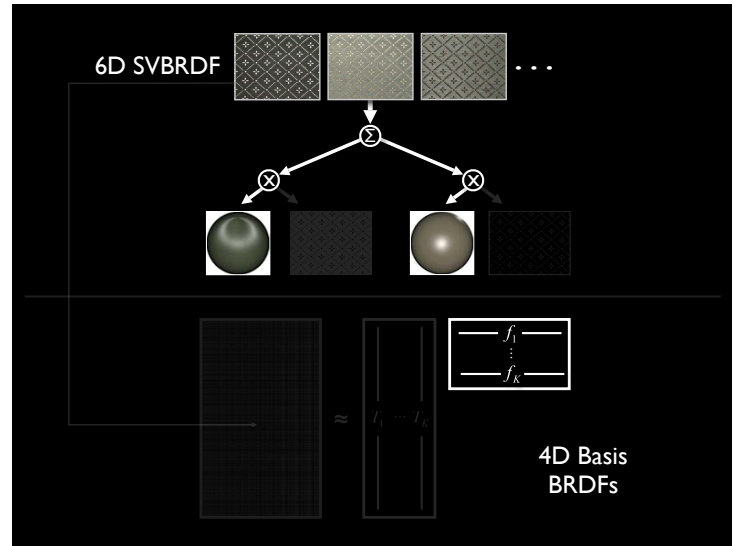
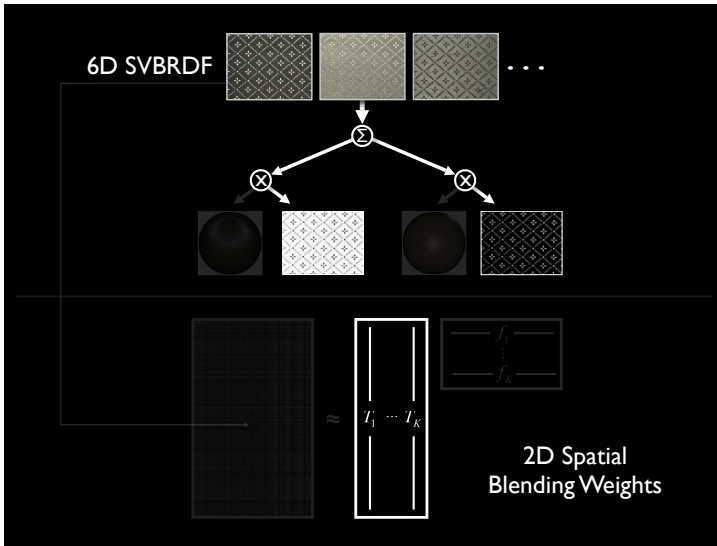


Factor SBRDF



6D SVBRDF





Research Challenge

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providing an intuitive factorization:

The diagram shows a grid of 6D SVBRDFs being factorized into a grid of 2D Spatial Blending Weights and a grid of 4D Basis BRDFs. The 2D Spatial Blending Weights and 4D Basis BRDFs are represented by grids with question marks, indicating the challenge of providing an intuitive factorization.

Key Idea

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incorporate domain-specific knowledge as constraints of factorization:

The diagram shows a grid of 6D SVBRDFs being factorized into a grid of 2D Spatial Blending Weights and a grid of 4D Basis BRDFs. The 4D Basis BRDFs are labeled as "plausible BRDFs", indicating that domain-specific knowledge is used as constraints of factorization.

Factorization Constraints

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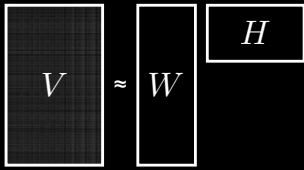
- non-negativity: reflectance functions are non-negative
- sparsity: few BRDFs at each position
- domain-specific:
 - energy conservation, monotonicity, etc.

Factorization Algorithms

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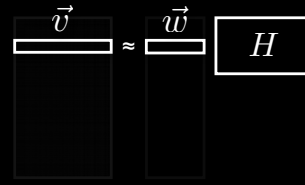
algorithm	properties			
	linear	positive	sparse	domain
PCA	✓	✗	✗	✗
clustering	✗	✓	✓	✗
NMF	✓	✓	✓	✗
ACLS	✓	✓	✓	✓

Alternating Constrained LS



1. Initialize W and H
2. Update W
3. Update H
4. Iterate until convergence

Alternating Constrained LS



convex QP problem

$$\min_{\vec{w}} \|\vec{v} - \vec{w}H\|^2$$

$$\vec{l} \leq \begin{Bmatrix} \vec{w}^T \\ A\vec{w}^T \end{Bmatrix} \leq \vec{u}$$

1. Initialize W and H
2. Update W
3. Update H
4. Iterate until convergence

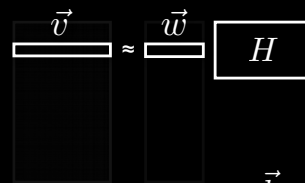
Reflectance Constraints



- non-negativity
 - constraint on value
- energy conservation
 - constraint on sum
- monotonicity
 - constraint on derivative

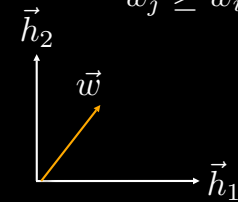
$$\vec{l} \leq \begin{Bmatrix} \vec{w}^T \\ A\vec{w}^T \end{Bmatrix} \leq \vec{u}$$

Measure of Sparsity

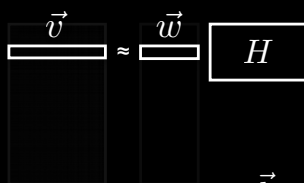


$$E_{sparse} = \sum_{i \neq j} w_i$$

$$w_j \geq w_i, i = 1 \dots K$$

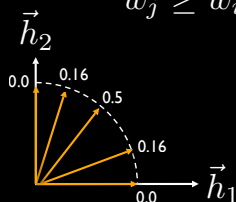


Measure of Sparsity



$$E_{sparse} = \sum_{i \neq j} w_i$$

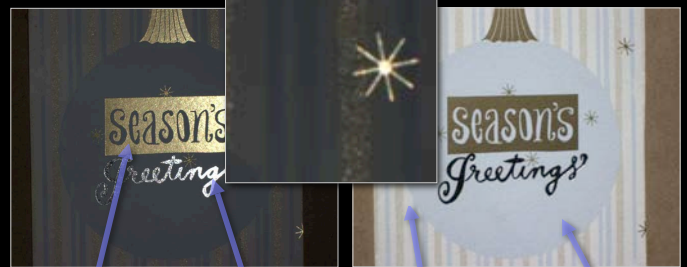
$$w_j \geq w_i, i = 1 \dots K$$



Season's Greetings Dataset



5 Camera Positions ~ 1,750 Images

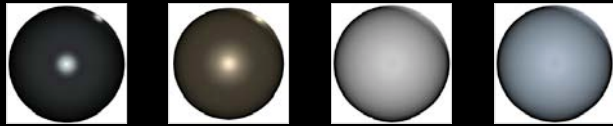


Gold Foil Silver Foil White Paper Blue Paper

Season's Greetings Dataset



Factorization Computed with **ACLS** (4 Terms)



Silver Foil Gold Foil White Paper Blue Paper

Wood+Tape Dataset



12 Camera Positions x 480 Light Positions = 6,000 Images

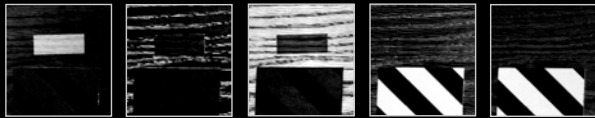


Oak Wood (Anisotropic) Semi-Transparent Tape Retroreflective Bicycle Tape

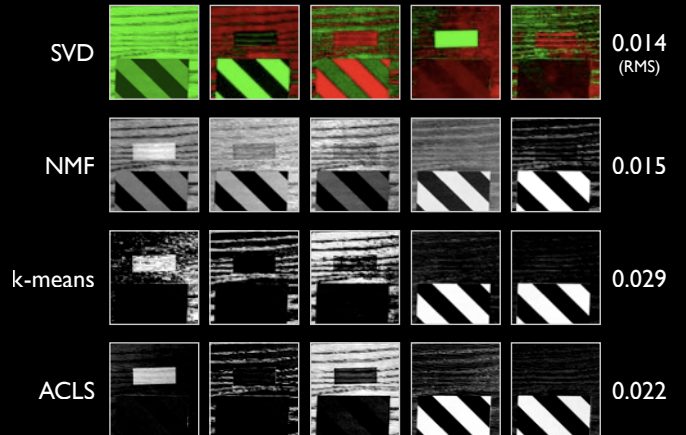
Wood+Tape Dataset



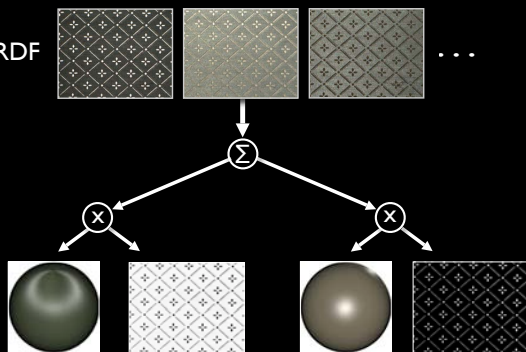
Blending Weights from **ACLS** (5 Terms)



Scotch Tape Dark Grain Light Grain Red Bicycle White Bicycle



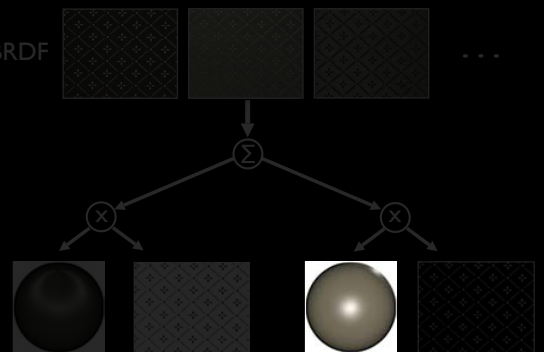
6D SVBRDF



2D blending weights

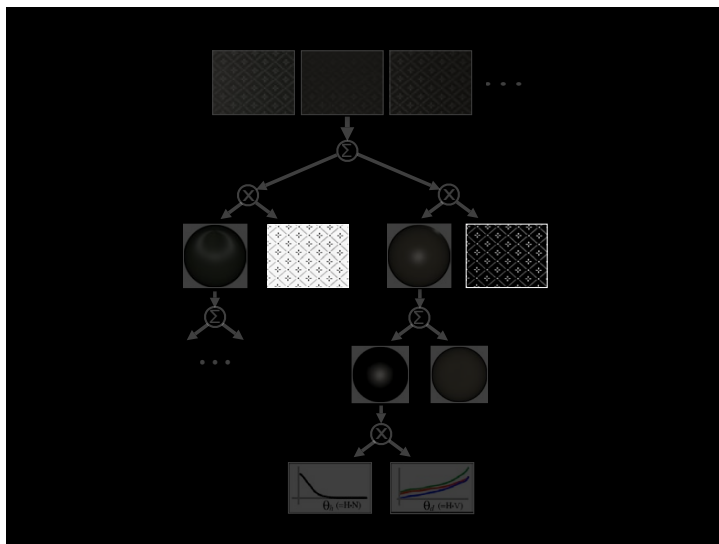
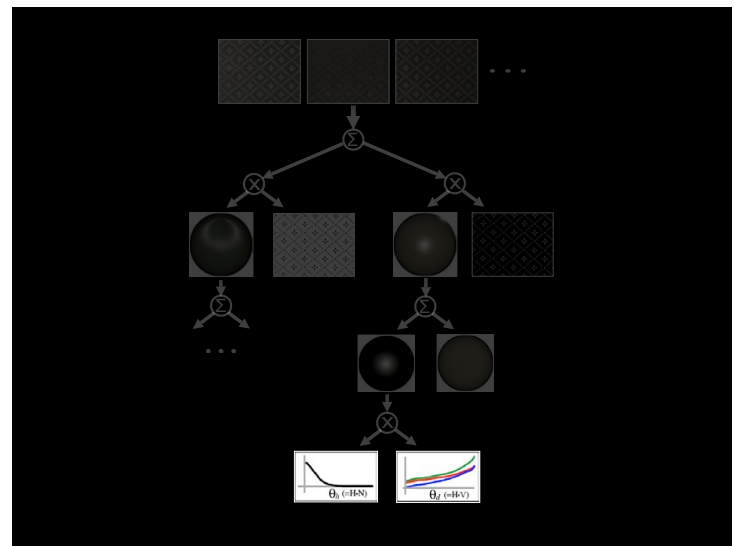
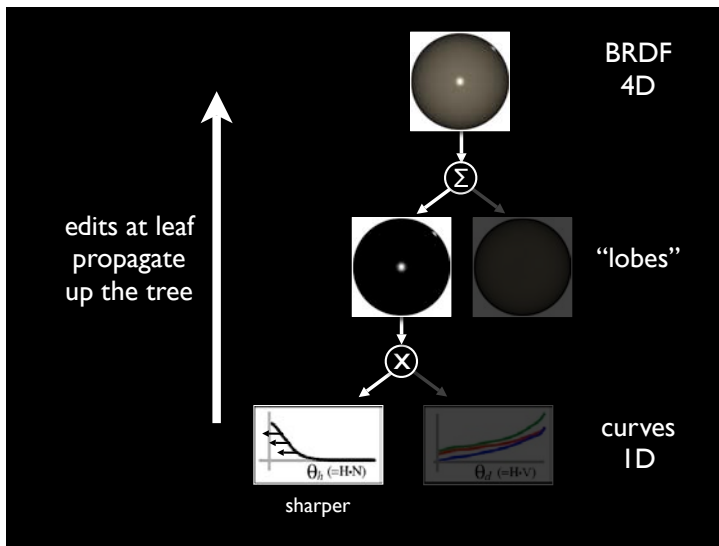
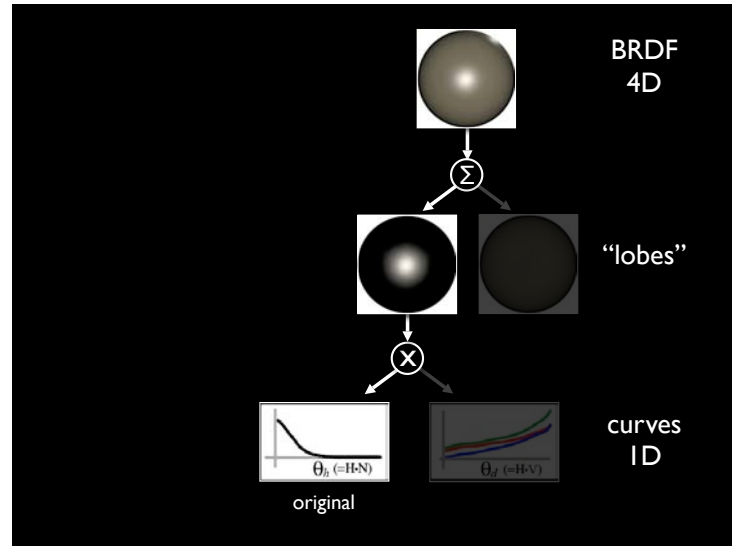
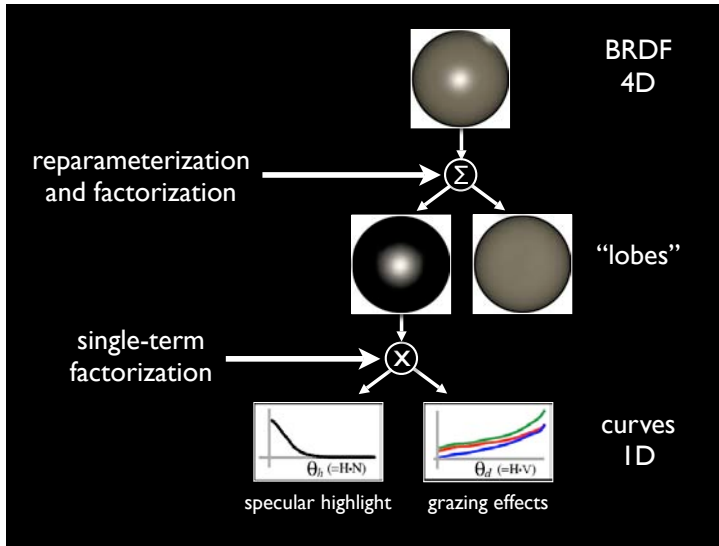
4D basis BRDFs

6D SVBRDF



2D blending weights

4D basis BRDFs



Summary

- representation goals:
 - compact
 - editable
 - supports rendering
- basis decomposition
 - parametric
 - non-parametric

Summary



- sparse/scattered data
- interpolation
- flexibility
- local minima

Summary



- sparse/scattered data
- interpolation
- flexibility
- local minima

Summary



- sparse/scattered data
- interpolation
- flexibility/accuracy
- local minima

Summary



- sparse/scattered data
- interpolation
- flexibility
- local minima

Future Directions



- higher-dimensional datasets
 - subsurface scattering / reflectance field
 - time-varying properties
 - etc.
- rigorous probabilistic framework
- measurement
 - synchronous shape + appearance
 - lowering calibration burden

Future Directions



- higher-dimensional datasets
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Future Directions



- higher-dimensional datasets
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Future Directions



- higher-dimensional datasets
 - subsurface scattering / reflectance field
 - time-varying properties
 - etc.
- **rigorous probabilistic framework**
- **measurement**
 - synchronous shape + appearance
 - lowering calibration burden

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From BSSRDFs to 8D Reflectance Fields

Hendrik P. A. Lensch
MPI Informatik

SIGGRAPH 2008 Class Los Angeles, August, 2008

Digitizing Real World Objects

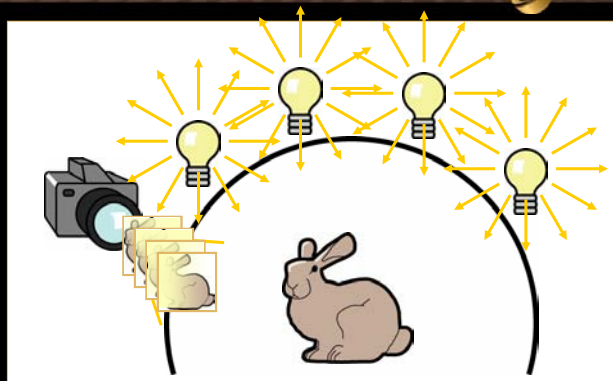
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relighting with arbitrary illumination patterns

Relighting

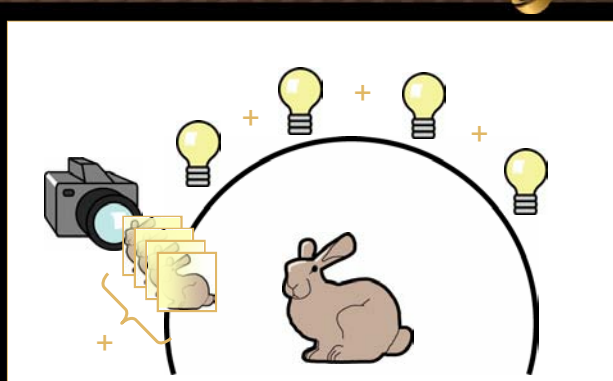
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one image for each light direction

Relighting

SIGGRAPH2008

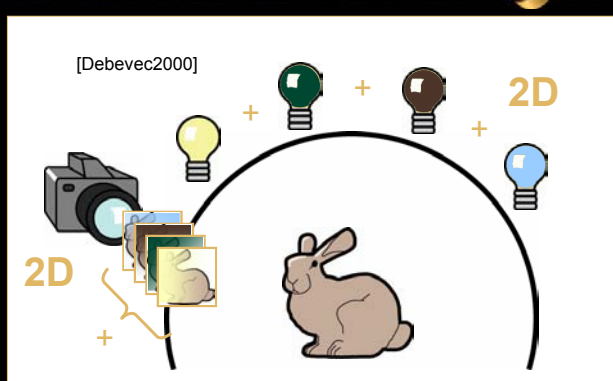


superposition

Reflectance Fields

SIGGRAPH2008

[Debevec2000]

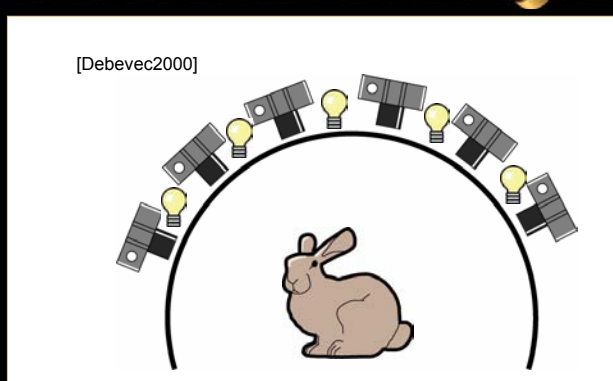


arbitrary materials, but single view point

Reflectance Field – 6D

SIGGRAPH2008

[Debevec2000]

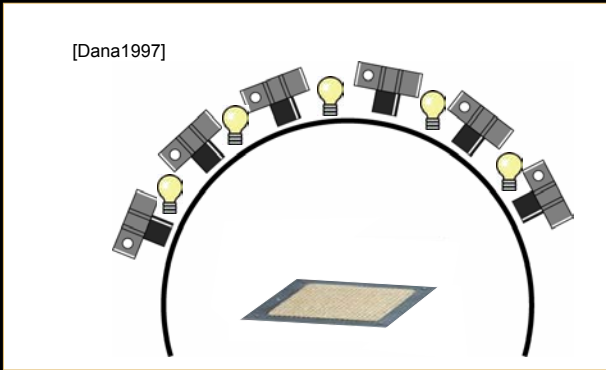


arbitrary materials, arbitrary geometry

Bidirectional Texture Functions

SIGGRAPH2008

[Dana1997]



arbitrary materials, surface patch

BTF Acquisition Devices

SIGGRAPH2008



[Sattler2003]

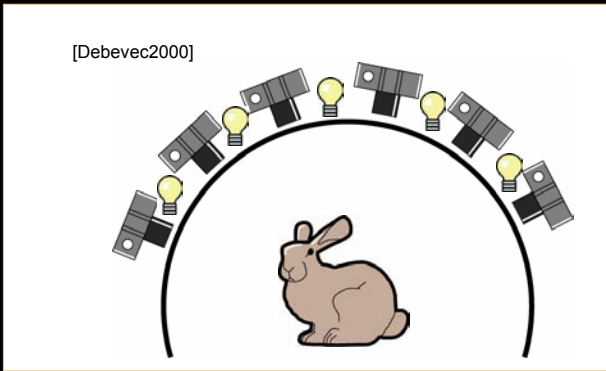


[Mueller2005]

Far-Field Reflectance Fields

SIGGRAPH2008

[Debevec2000]



arbitrary materials, but distant light sources only

Far- vs. Near-Field Illumination

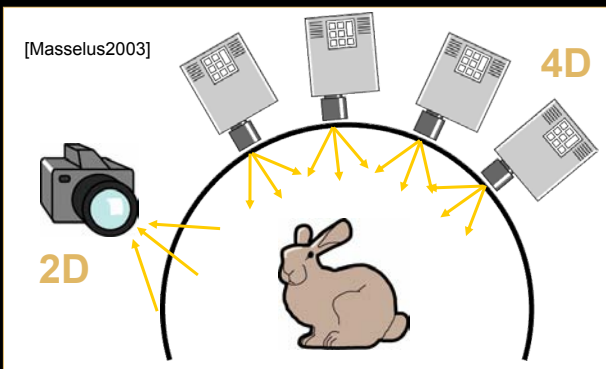
SIGGRAPH2008



6D Reflectance Fields

SIGGRAPH2008

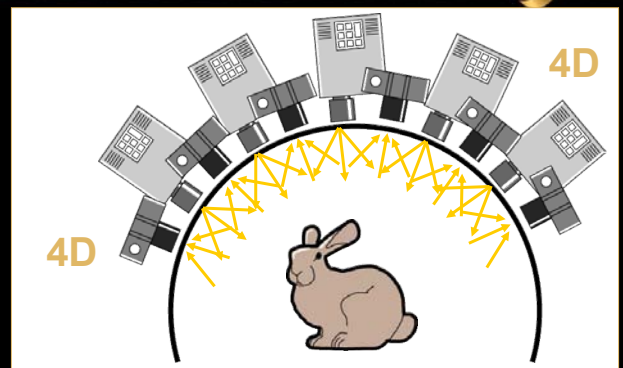
[Masselus2003]



relighting with 4D incident light fields

8D Reflectance Fields

SIGGRAPH2008



arbitrary materials +
arbitrary view point + arbitrary illumination

Definition – Reflectance Field



8D function = BSSRDF

$$f_r((\vec{x}_i, \vec{\omega}_i) \rightarrow (\vec{x}_o, \vec{\omega}_o))$$

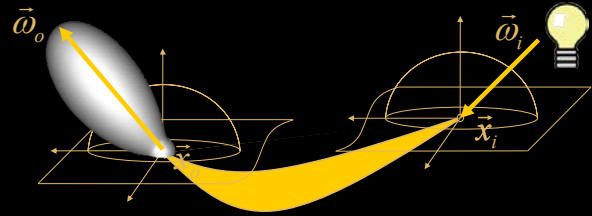


Definition – Reflectance Field



ratio of reflected radiance to incident flux

$$f_r((\vec{x}_i, \vec{\omega}_i) \rightarrow (\vec{x}_o, \vec{\omega}_o)) = \frac{dL_o(\vec{x}_o, \vec{\omega}_o)}{d\phi_i(\vec{x}_i, \vec{\omega}_i)}$$



Main Problem



- sampling an *8D function*
 - spending 100 samples/dimension
→ 10^{16} samples
 - hi-res 3D geometry: 10^8 vertices
- coherence in reflectance fields
→ reduced data complexity
- no complete solution yet



Approaches



- limited reflectance model
- limited reproduction
 - viewer position
 - incident illumination
- adaptive parallel acquisition
- advanced interpolation

Relighting with 4D Incident Light Fields



- goal: relighting with spatially varying illumination, e.g. spot lights



Acquisition with Large Blocks



- fixed camera perspective
- rotating illumination

Relighting Results



Translucent Objects



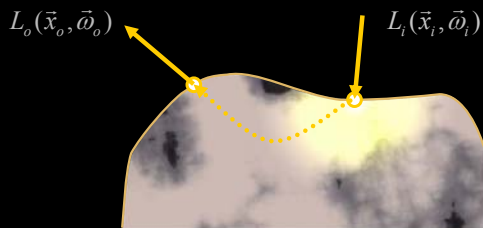
- light transport through the object
- scattering dampens high frequencies

BSSRDF - 8D



bidirectional scattering-surface reflectance distribution function [Nicolodemus77]

$$f_r((\vec{x}_i, \vec{\omega}_i) \rightarrow (\vec{x}_o, \vec{\omega}_o))$$

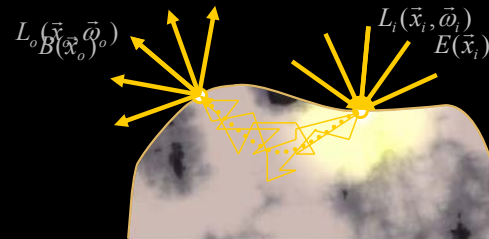


Diffuse Approximation



neglect directional dependency [Jensen 2001]

- multiple scattering leads to diffuse light transport



4D - Diffuse Approximation



⇒ diffuse reflectance function $R_d(\vec{x}_i, \vec{x}_o)$

- four dimensions only
- dense sampling is possible



Diffuse Reflectance Function R_d



- discretize the surface
 - enumerate all surface points
 - vectors for irradiance E and radiosity B

- matrix R_d

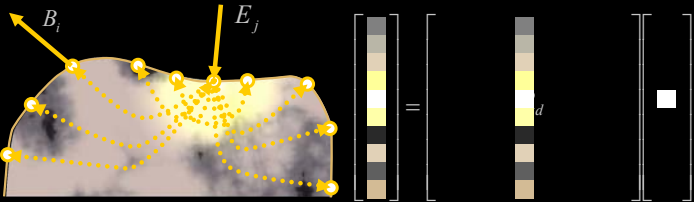
- linear point-to-point transport

$$\begin{bmatrix} B_i \end{bmatrix} = \begin{bmatrix} R_d \end{bmatrix} \begin{bmatrix} E_j \end{bmatrix}$$

Basic Idea



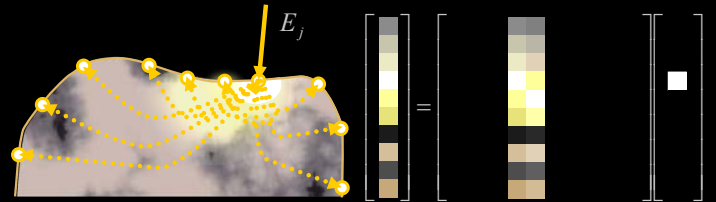
- direct measurement of R_d
 - illuminate individual surface points
 - capture impulse response function



Basic Idea



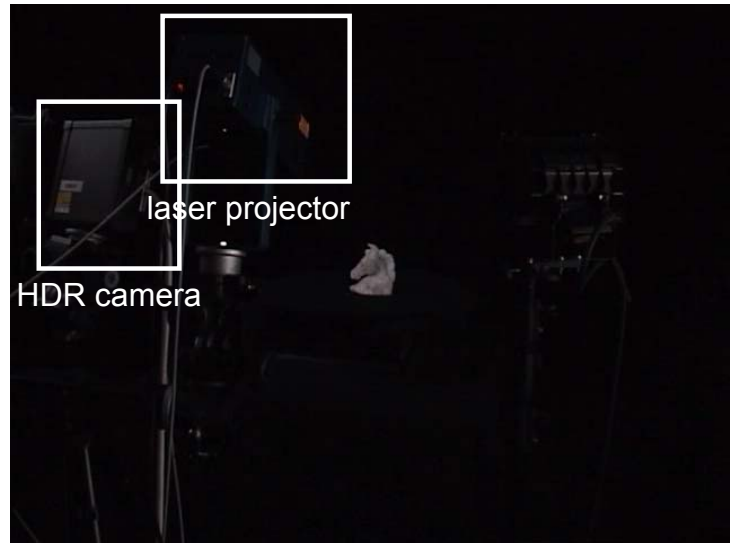
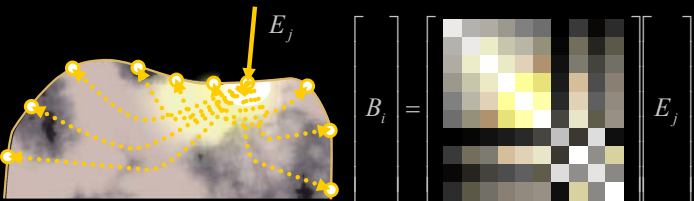
- direct measurement of R_d
 - illuminate individual surface points
 - capture impulse response function



Basic Idea



- direct measurement of R_d
 - illuminate individual surface points
 - capture impulse response function



Matrix Representation



- 500.000 - 1.000.000 input images
⇒ $\sim 100.000^2$ entries
- fill up holes (inpainting)
- hierarchical representation
- hardware assisted rendering
 - analysis
 - real-time rendering

[Lensch, Goesele, Bekaert, Magnor, Lang, Seidel – PG2003]

Video

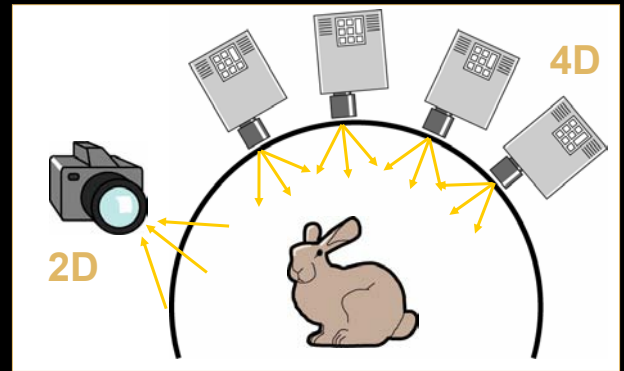


1.000.000 images, 22 hours → model - 800MB

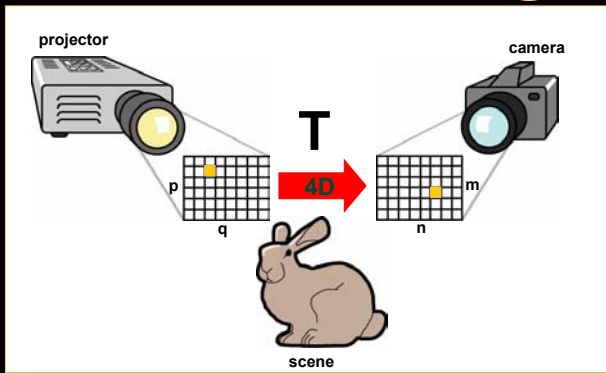


[Goesele, Lensch, Lang, Fuchs, Seidel - SIGGRAPH 2004]

Fixed Perspective + Arbitrary Illumination



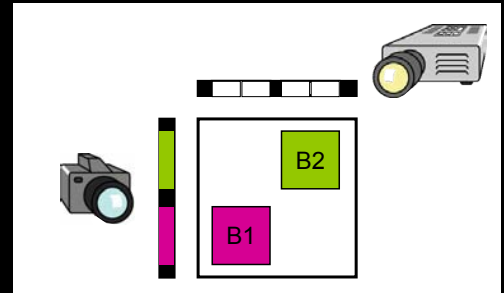
Pixel-to-Pixel Transport



Adaptive Parallel Acquisition



- assumption: sparse matrix
- radiometrically independent blocks can be sensed in parallel



Adaptive Parallel Acquisition



parallelized acquisition of regions which do not overlap in the camera image



projector pattern



camera image

Adaptive Parallel Acquisition



parallelized acquisition of regions which do not overlap in the camera image



Relighting with Arbitrary Patterns



1.200 images. 2 hours → model - 220MB



Captured Global Light Transport



Helmholtz Reciprocity

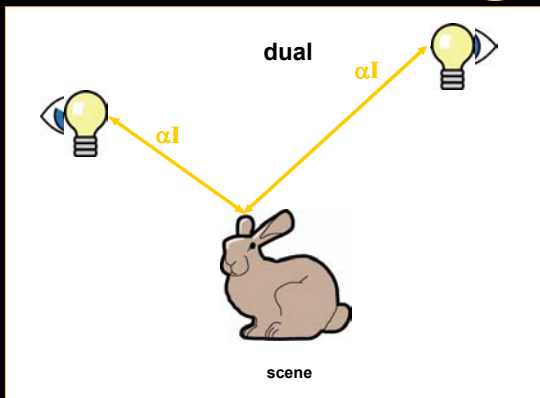


Image Acquisition without a Camera

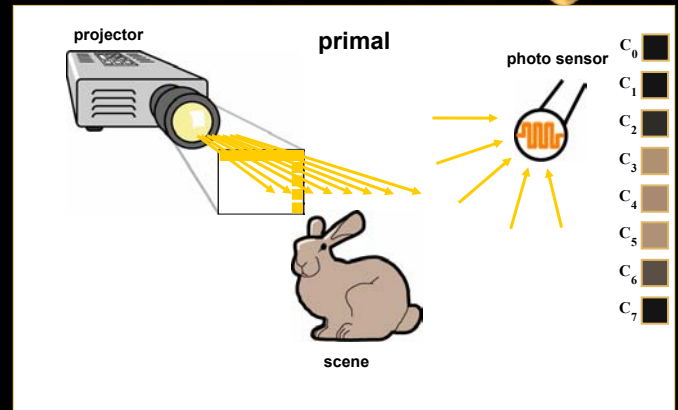
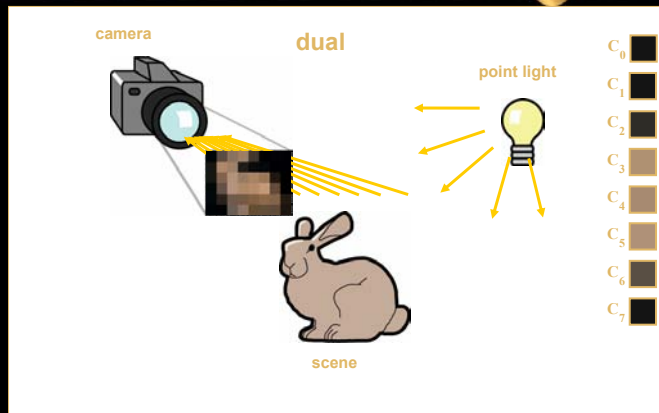
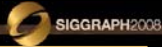


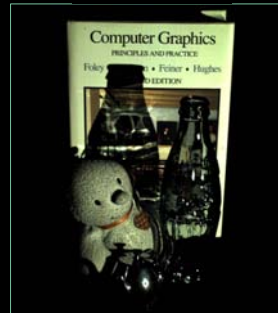
Image Acquisition without a Camera



Dual Photography



photograph
from camera



dual image
from projector



[Sen, Chen, Garg, Marschner, Horowitz, Levoy, Lensch - SIGGRAPH 2005]

Examples



primal

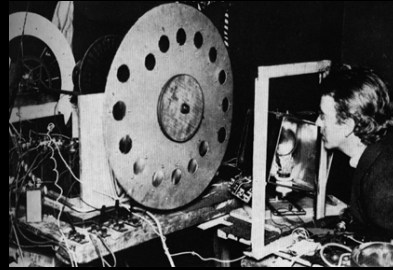


dual

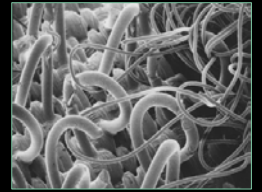
Related Techniques



- “Flying-spot” TV camera [Baird 1926]
- scanning electron microscope

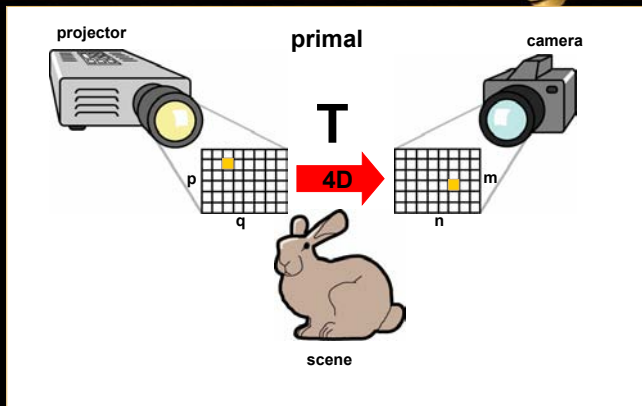


[Baird 1926]

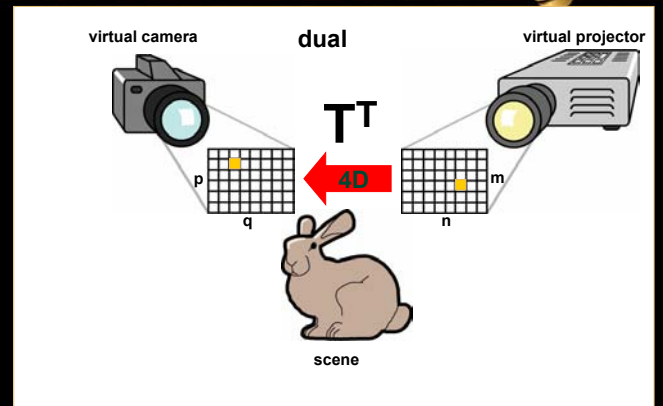


35x magnification
[Museum of Science, Boston]

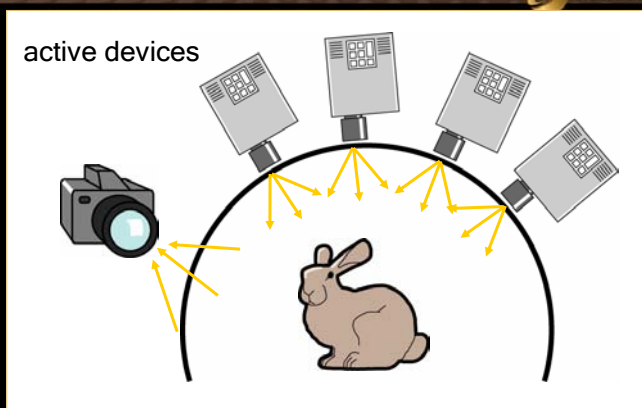
Relighting with Dual Photography



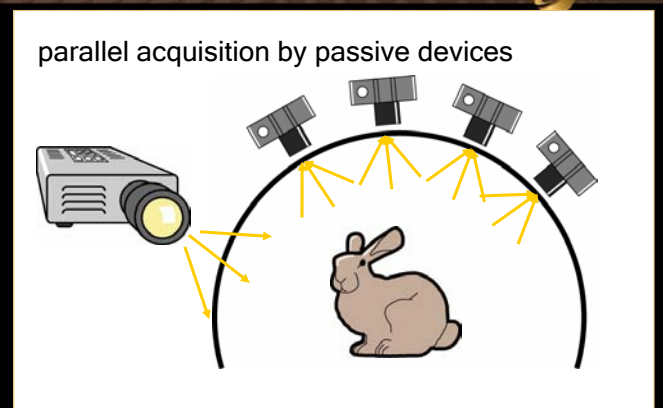
Relighting with Dual Photography



Acquisition of 6D Reflectance Fields

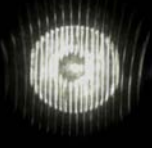


Dual Acquisition Process



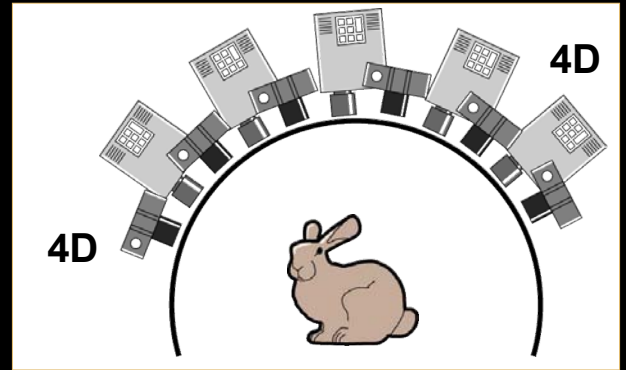
Smooth Interpolation

100.000 images, 26 hours → model - 4.5GB



[Chen, Lensch - VMV2005]

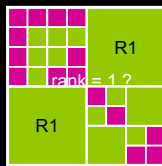
8D Reflectance Fields



arbitrary view point + arbitrary illumination

H-Matrices

[Hackbusch2000]



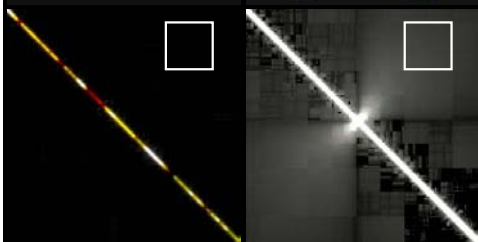
efficient representation of dense but *data-sparse* matrices

- subdivision hierarchy
- local low-rank approximation
- efficient evaluation

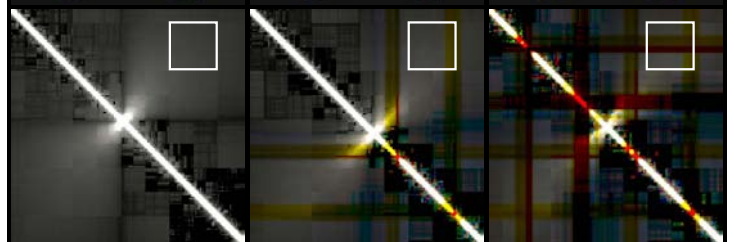
Direct vs. Indirect Reflections



Direct vs. Indirect Reflections



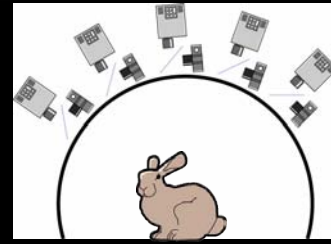
Direct vs. Indirect Reflections



2D Slices through a Reflectance Field



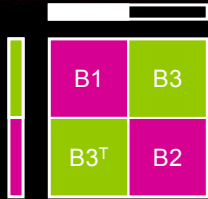
Symmetric Acquisition



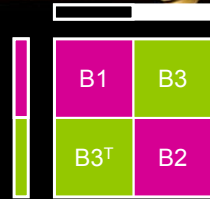
- symmetric 8th order tensor
- rank-1 approximation from two images only
- parallel acquisition of dense matrices

[Garg, Talvala, Levoy, Lensch – EGSR06]

Symmetric Exploration

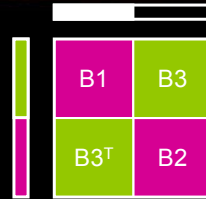


B3 – row sums
B2 – rows+columns

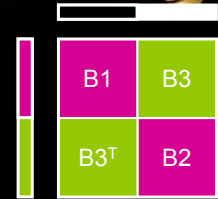


B3 – column sums
B1 – rows+columns

Symmetric Exploration



B3 – row sums
B2 – rows+columns



B3 – column sums
B1 – rows+columns

rank-1 approximation?



Hierarchical Rank-1 Decomposition

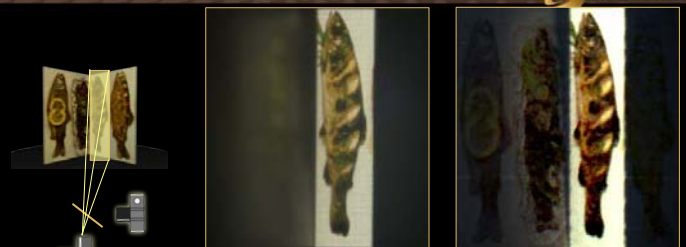


$$\begin{bmatrix} B1 & R1 \\ R1 & B2 \end{bmatrix} = \begin{bmatrix} & B3 \\ B3^T & \end{bmatrix} + \begin{bmatrix} B1 & \\ & B2 \end{bmatrix} = \dots$$

already determined radiometrically independent

B1 and B2 are investigated in parallel.
parallel acquisition even for dense matrices

Dual vs. Symmetric Photography



Dual Photography

Symmetric Photography

- increased SNR because regions are determined at large block sizes

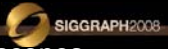
An 8D Reflectance Field



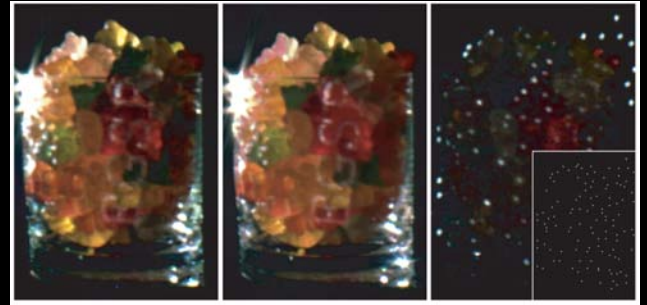
3.300 images, 6 hours → model - 1.4 GB



Virtual Photography



- reflectance fields of arbitrarily complex scenes



novel illumination

original

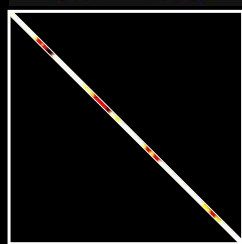
acquisition pattern

[Garg, Talvala, Levoy, Lensch – EGSR 2006]

Application of Near-field Reflectance Fields



- getting rid of global effects



compare [Nayar2006]

Application to 3D Scanning

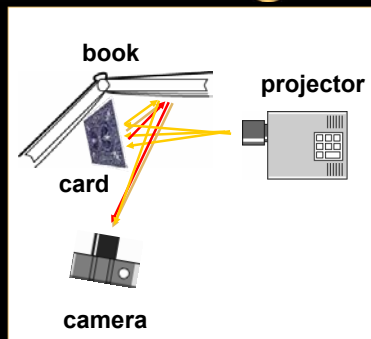


[Chen, Fuchs, Lensch, Seidel – CVPR 2007]

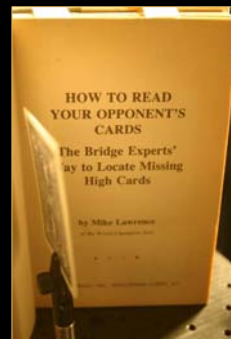
Card Experiment



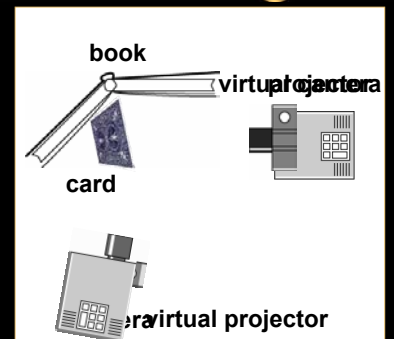
primal



Card Experiment



primal



Card Experiment



primal



dual

Near-Field Reflectance Fields



- Sequential Sampling
- Dual Photography
- Symmetric Photography based on \mathcal{H} -matrices

- first methods for acquiring the global light transport in arbitrary scenes

Challenges



- densely sampled 8D reflectance fields
- upsampling / interpolation
- dynamic near-field reflectance fields
- interactive relighting
- global illumination with reflectance fields
- theory on the complexity of reflectance fields

Thanks



- BMBF (FKC011MC01)
- DFG - Emmy Noether Program



<http://mpi-inf.mpg.de/~lensch>

The Human Face Scanner Project

Tim Weyrich
Princeton University

Facial Appearance Acquisition

“Grand challenge” in appearance acquisition:

- Complex reflectance and scattering properties
- *In vivo* measurements required
- High expectation by the observer
- Appearance editing desirable



Analysis of Human Faces

*Analysis of Human Faces
Using a Measurement-Based
Skin Reflectance Model*
[Weyrich et al. 2006]

joint work at
ETH Zurich, Switzerland,
and Mitsubishi Electric Research
Laboratories, Cambridge, MA

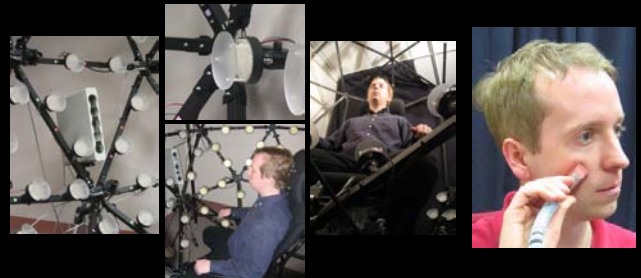


Photograph

Rendered

Objectives

- Capture facial appearance



Objectives

- Capture facial appearance
- Reconstruct realistic face models



Photograph

Rendered

Objectives

- Capture facial appearance
- Reconstruct realistic face models
- High-level controls to alter appearance



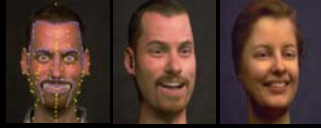
Target Skin

Altered Appearance

Capturing Face Appearance



- Explicit Modeling
 - Geometry + texture
[PIGHIN ET AL. 1998]



[PIGHIN ET AL. 1998]

- Image-based Methods
 - Reflectance fields
[DEBEVEC ET AL. 2000],
[HAWKINS ET AL. 2004]

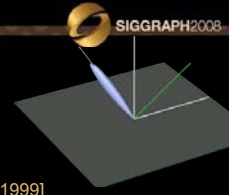


[HAWKINS ET AL. 2004]

Skin Reflectance Models



- BRDF (*bi-directional reflectance distribution function*)
 - BRDF approximation of scattering
[HANRAHAN AND KRUEGER 1993], [STAM 2001]
 - Image-based BRDF [MARSCHNER ET AL. 1999]
- BSSRDF (*bi-directional surface scattering reflectance distribution function*)
 - Single-layered skin model [JENSEN ET AL. 2001]
 - Multi-layered skin model [DONNER AND JENSEN 2005/2006]
- BTF (*bi-directional texture function*)
 - Spatially varying reflectance of skin patches
[CULA AND DANA 2002]



Appearance Editing



- Image-based editing
 - Manual editing by skilled artists
 - Melanin/hemoglobin model
[TSUMURA ET AL. 2003]



[TSUMURA ET AL. 2003]

- Morphable face model
[BLANZ AND VETTER 1999],
[FUCHS ET AL. 2005]



[BLANZ AND VETTER 1999]

Production Environment



- Gemini Man
[WILLIAMS ET AL. 2005]
- Hulk, Harry Potter II
[HERY 2003/2005]
- Matrix
[BORSHUKOV 2003]
- Spider Man II
[SAGAR ET AL. 2004]



© ILM [HERY 2003]



[BORSHUKOV 2003]

Project Contributions



- Acquisition hardware for the facial BSSRDF
 - Translucency measurements
 - Facial reflectance fields
- Practical skin model to be fitted
 - Simple, but realistic
 - Suited for production environments
- Analysis of physiological parameters
- Intuitive appearance editing framework

Outline



- Skin appearance acquisition
- Face data processing
- Reflectance Model Fit
- Reflectance Analysis
- Appearance Transfer

Skin Appearance



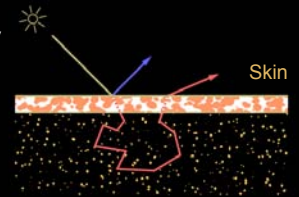
- Skin most important for facial appearance
- Main effects due to skin's translucent layers



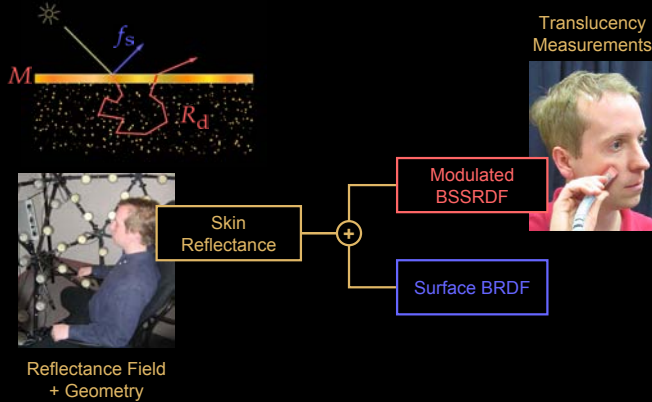
Skin Appearance



- Skin most important for facial appearance
- Main effects due to skin's translucent layers
- Light transport affected by
 - Air/skin interface (reflectance/refraction)
 - Epidermis, Dermis (scattering/absorption)



Reflectance Acquisition



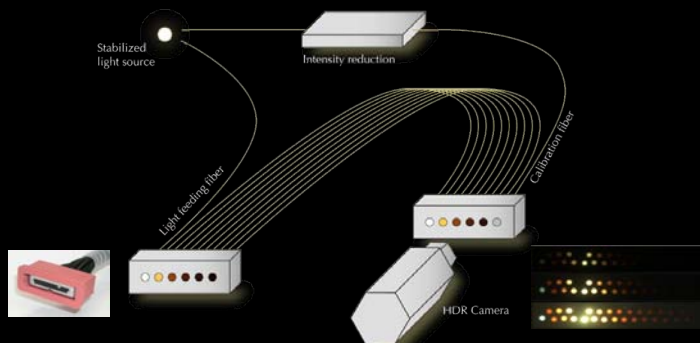
"BSSRDF Gun"



- Subcutaneous light transport measurements
- Measures translucency (mean free path ℓ)
 - Contact measurements
 - Light transport through optical fibers
- Suction pump ensures contact



"BSSRDF Gun"



Reflectance Field Acquisition



- Spherical acquisition dome
 - 16 cameras @ 1300 x 1030
 - 150 LED light sources
 - Commercial 3D scanner



Reflectance Field Acquisition



- Spherical acquisition dome
 - 16 cameras @ 1300 x 1030
 - 150 LED light sources
 - Commercial 3D scanner
- Dual-exposure HDR



Reflectance Field Acquisition



- Spherical acquisition dome
 - 16 cameras @ 1300 x 1030
 - 150 LED light sources
 - Commercial 3D scanner
- Dual-exposure HDR
- 25 seconds



Sample Reflectance Field

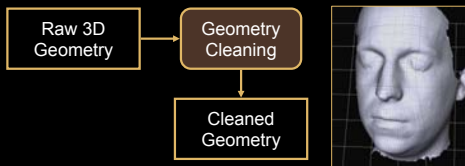


Outline

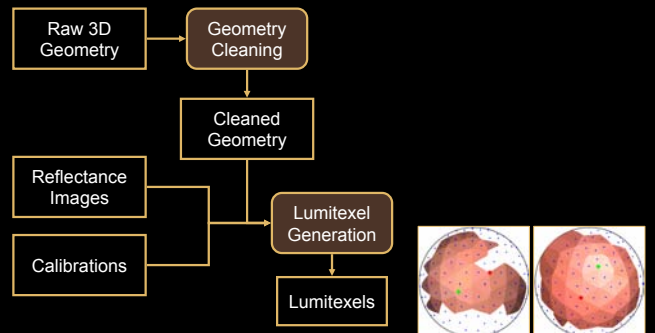


- Skin appearance acquisition
- Face data processing
- Reflectance Model Fit
- Reflectance Analysis
- Appearance Transfer

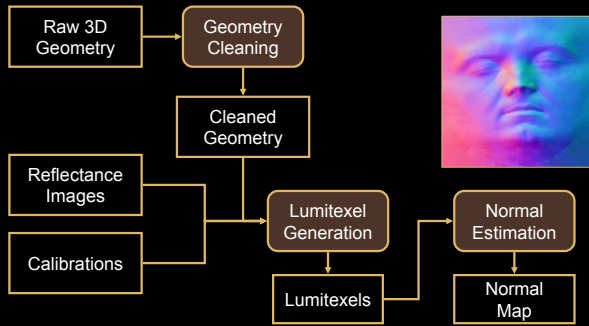
Overview



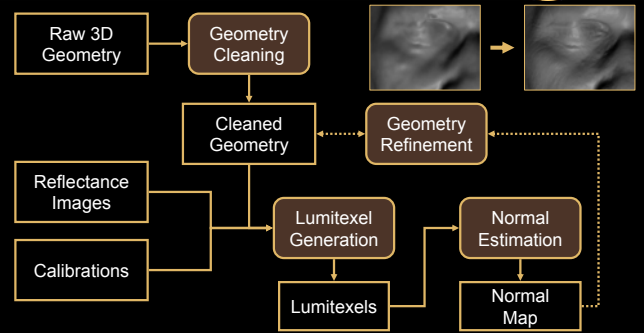
Overview



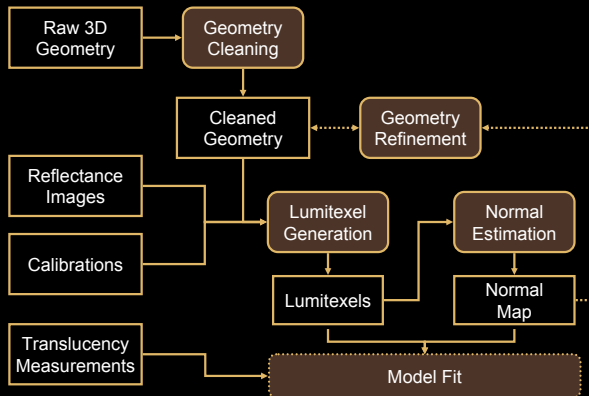
Overview



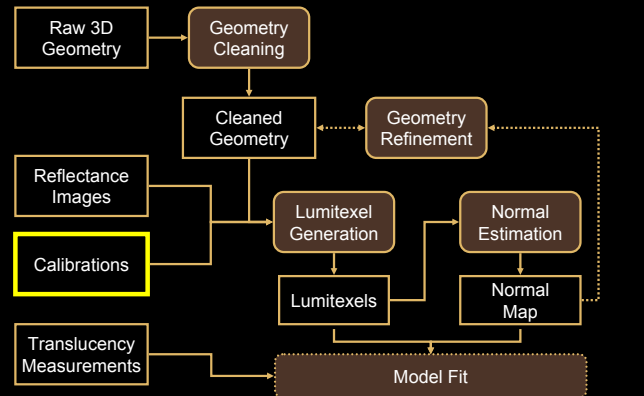
Overview



Overview



Overview



Camera Calibration



- Intrinsic
 - Using Intel OpenCV library
 - Based on checker-board images
- Extrinsic
 - n -camera calibration ($n = 16$)
 - Euclidian bundle optimization
 - Correspondences from LED swept through volume



Camera Calibration



- Vignetting & color calibration
 - Radial image intensity fall-off
 - Relative sensor calibration of all cameras
 - Affine color correction model [FUNT 2000]
 - Equalizes images taken under identical conditions
- Radiometric calibration
 - Implicitly through light source calibration

Light Source Calibration



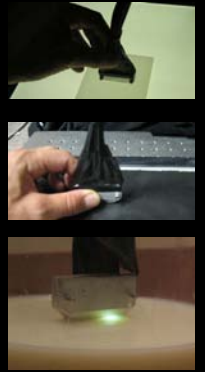
- Desired parameters
 - Light source color
 - Light cone fall-off
- Fluorilon™ reflectance target
 - Perfect diffuse reflector
 - Reflects 99.9% of incident radiance
- Reflectance fields of different orientations
- Fitting 2nd-order polynomial to spot cross-section



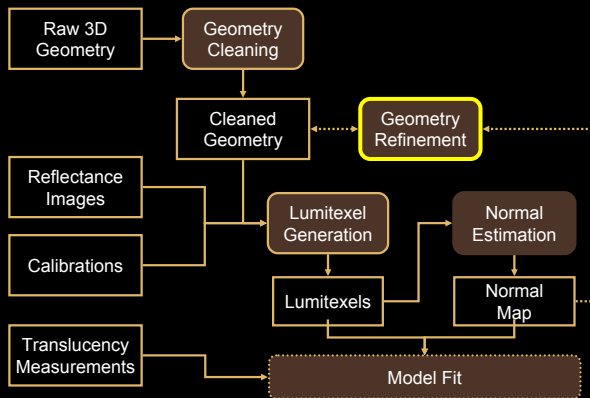
“BSSRDF Gun” Calibration



- Relative fiber transmittance
 - Light table with opal glass diffuser
- Black image calibration
- Irradiance calibration
 - Skim milk as secondary standard
 - Values as measured by [JENSEN ET AL. 2001]



Overview

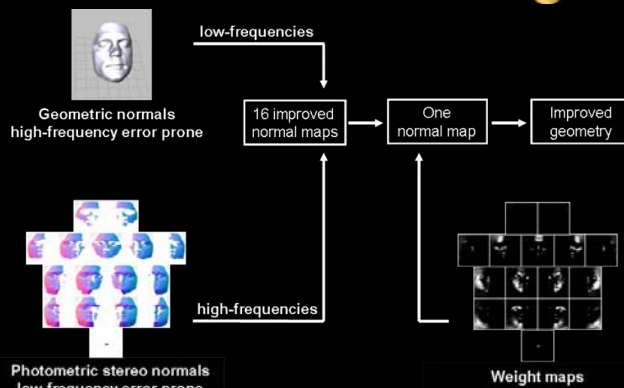


Geometry Refinement

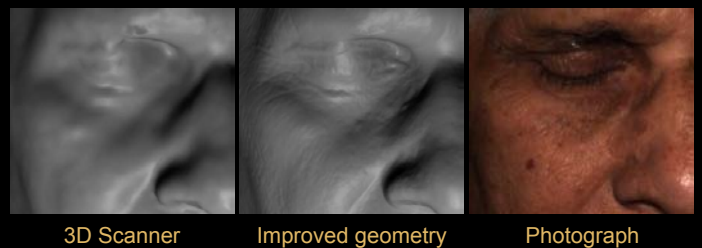


- Geometry and normal information crucial
- Normal estimation
 - Photometric stereo
 - Lambertian assumption
 - Problem: bias, discontinuities
- Normal and geometry improvement adapting [NEHAB ET AL. 2005]

Geometry Refinement



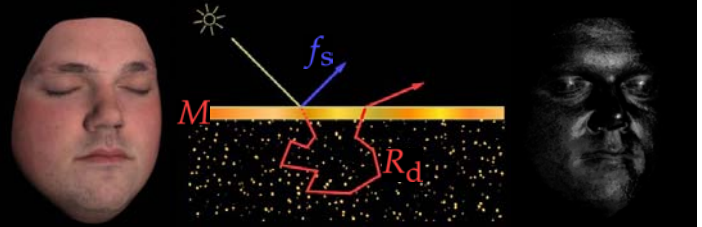
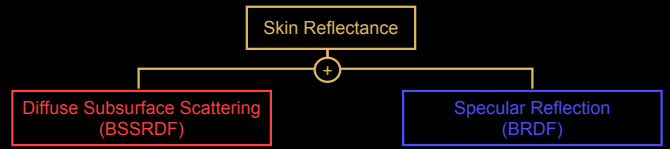
Geometry Refinement



Outline

- Skin appearance acquisition
- Face data processing
- Reflectance Model Fit
- Reflectance Analysis
- Appearance Transfer

Skin Reflectance Model



Skin Reflectance Model



Dipole Approximation
[JENSEN ET AL. 2001]

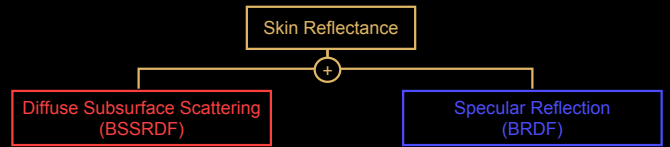
- Analytic model
- Isotropic scattering in homogeneous materials
- Modulation texture M
[GOESELE ET AL. 2004]



Torrance-Sparrow BRDF

- Physically based
- Micro-facets

Model Fit



Face Reconstruction



Photograph

Reconstruction

Reconstruction



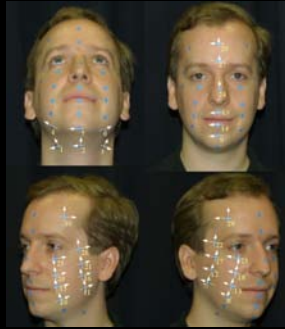
Photograph

Reconstruction

Translucency Variance



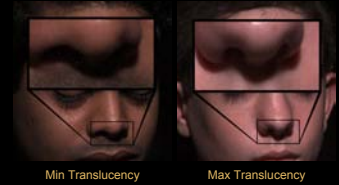
- Model validation
 - Facial scattering is isotropic
- Spatial translucency variance minute



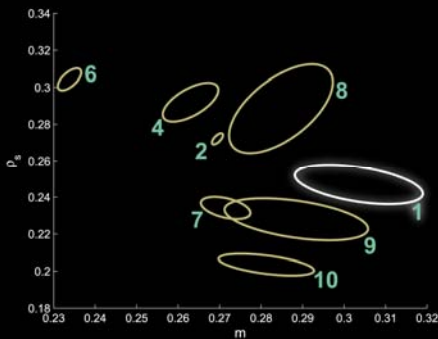
Translucency Variance



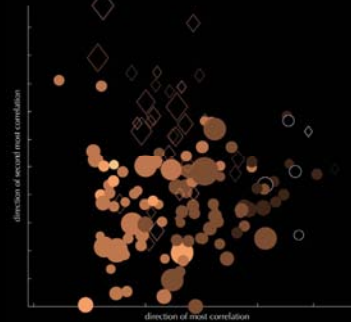
- Model validation
 - Facial scattering is isotropic
- Spatial translucency variance minute
- Inter-subject variance negligible
 - Small variance between males and females



Spatial BRDF Variance



Skin Trait Variations



- Canonical Correlation Analysis (CCA)
 - Directions of maximal correlation in BRDF parameter space
- BRDF: correlates with *skin type* and *gender*
- Albedo: highly correlated with *skin type*

Outline



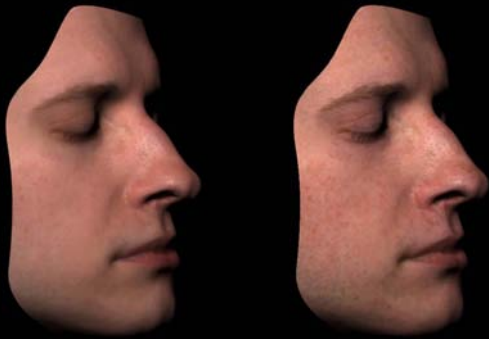
- Skin appearance acquisition
- Face data processing
- Reflectance Model Fit
- Reflectance Analysis
- Appearance Transfer

Appearance Editing



- From parameter observations derive intuitive user controls
 - Main tool: texture synthesis [HEEGER AND BERGEN 1995], [MATUSIK ET AL. 2005]
 - Applicable to all model parameter types
 - Add freckles, moles, gloss variations, ...
- General appearance editing framework

Results Appearance Transfer



Target face

Freckles applied

Results Appearance Transfer



Target face

Changed skin type

Results Appearance Transfer



Target face

Lotion applied, Stubbles reduced

Contributions



- Acquisition hardware for the facial BSSRDF
 - Translucency measurements
 - Facial reflectance fields
- Practical skin model to be fitted
 - Simple, but realistic
 - Suited for production environments
- Analysis of physiological parameters
- Intuitive data-driven appearance editing framework
- Published appearance database of human faces

Potential Extensions



- Facial hair
 - Eye-brows, eye-lashes
 - Beard, stubbles
 - Velvety hair
- Spectral measurements
- Multi-layered model using additional model assumptions (e.g. [DONNER AND JENSEN 2006])
- *Will increasing measurement accuracy increase the perceived degree of realism?*



Q & A

Appearance database online at:
<http://www.merl.com/facescanning/>