Published Research on Line Drawings from 3D Data

The following list contains papers describing algorithms for producing line drawings from 3D data, as well as research on the perception of line drawings. Papers marked with an asterisk (*) are the most closely related to this course, and are recommended reading. Detailed bibliographical information follows this annotated list.

Before 1990

- [Appel 1967] Introduces an efficient algorithm for discovering hidden lines in drawings of 3D shapes by propagation of quantitative invisibility.
- [Waltz 1975] Applies the technique of constraint satisfaction to search for consistent labelings of lines in line drawings of polyhedral scenes. It works from exhaustive catalogs of all possible configurations of line junctions.
- [Stevens 1981] A description of how repeated arrangements of lines in line drawings can give rise to shape percepts. Parallel lines (cutting lines), geodesics and lines of curvature are investigated.
- [Barrow 1981] Describes algorithms for the reconstruction of surfaces from line drawings by making a range of assumptions (i.e. about surface smoothness).
- [Koenderink 1982] A discussion of what lines artists might be drawing. It includes a proof that ending contours must terminate in a concave way, yet points out that artists often draw convex endings.
- * [Koenderink 1984] Seminal paper establishing the relationship between the curvature of the contour in the image (the apparent curvature) and the Gaussian curvature of the corresponding point on the surface.
- [Malik 1987] The generalization of line labeling [Waltz 1975] to curved surfaces. It also includes an algorithm for pruning away unlikely interpretations.

1990

- [Dooley 1990] Describes automatic generation of boundary, silhouette, discontinuity, and iso-parametric lines to depict 3D objects. Main focus is on stylization with an importance, line type, and hiddenness matrix.
- [Elber 1990] Defines boundary, silhouette, discontinuity, and iso-parametric curves mathematically. Describes curve extraction, intersection, and visibility methods for B-spline surfaces. Visibility propagates quantitative invisibility.
- [Koenderink 1990] Well-known and well-respected book on geometric and perceptual aspects of shape.
- * [Saito 1990] Uses 2D image processing algorithms to draw discontinuities, edges, and iso-parametric lines over 2D renderings of 3D models.

1992

- [Knill 1992] Describes perceptual experiments that suggest our perceptual systems assume that surface markings (i.e. reflectance boundaries) line along geodesics on the surface.
- [Rossignac 1992] Introduces a method of hidden-line removal for contours using the hardware z-buffer.

1994

- [Hsu 1994] Introduces a comprehensive framework for describing and rendering heavily stylized complex 2D strokes.
- [Saito 1994] Proposes interactive visualization of volumetric data by hierarchically sampling areas of interest from the data and rendering oriented lines.
- * [Salisbury 1994] Presents interactive user-driven methods for creating line drawings by painting texture and tone over a 2D reference image, with optional extracted edges.
- * [Winkenbach 1994] Describes general principles for creating computer generated line drawings from 3D models. Introduces stroke textures to apply resolution-dependent texture and tone to 3D polygonal surfaces. Describes *indication*, a technique for elision of detail in drawn textures to enhance comprehensibility of line drawings.

1995

- [Elber 1995a] Describes generation of line-art drawings using iso-parametric curves to cover freeform surfaces. A lighting model affects the density of curves and noise is added to avoid a synthetic look.
- [Elber 1995b] Presents several ideas for the improvement of line drawings from 3D surfaces. Suggests performing depth cuing by modulating line width and intensity, drawing thin light strokes for background lines. Trimming of background lines near intersections is also suggested.
- [Interrante 1995] Suggests using ridge and valley lines as an aide to transparent isosurface visualization. Lines are extracted from an isosurface and opacity is modulated by principal curvature.

1996

- [Interrante 1996] Describes rendering of transparent isosurfaces using short strokes directed along principal curvature with length modulated by principal curvature magnitude.
- [Koenderink 1996] A psychophysical study that measures and compares shape percepts from (external) silhouettes, line drawings and shaded images. It uses the same psychophysical tasks as [Koenderink 2001].

- [Salisbury 1996] Suggests representing pen-and-ink drawings with a grayscale image, a set of discontinuity segments, and associated stroke textures for the purposes of producing consistent drawings at any scale and resolution. A novel edgereconstruction algorithm allows low-resolution grayscale images to be up-sampled while maintaining sharp discontinuities. Line drawings are created by rendering the stroke textures on the grayscale image.
- [Thirion 1996] Introduces the marching lines algorithm for extraction of line loops along intersections of two closed surfaces in 3D space. Describes drawing crest lines as an aide to visualizing isosurfaces by intersecting a maximal curvature surface with the isosurface.
- [Winkenbach 1996] Describes rendering line-art drawings from parametric freeform surfaces. Details controlled-density hatching to modulate line width based on proximity to other lines. Also introduces a method to construct a planar map for a parametric surface and a method of rendering shadows with strokes.

1997

- [Ma 1997] Argues for the benefit of extracting feature lines (contours, ridges and valleys) from unstructured triangular meshes. Presents some results in the context of augmenting fluid flow visualization.
- * [Markosian 1997] Introduces a fast randomized algorithm for finding and tracing contours on polygonal surfaces. Exploits frame-to-frame temporal coherence and uses random probes to locate contour seed points and trace contours along the surface. Uses an accelerated quantitative invisibility propagation method to differentiate hidden lines.
- [Masuch 1997] Describes a system for creating animated linedrawings from 3D polygonal objects.

1998

- [Belyaev 1998] Details and derives formulas for ridges and valleys on implicit surfaces. Uses these to generate ridges and valleys on an implicit surface as the intersection curves of a ridge and valley surface with the implicit surface.
- [Bremer 1998] Describes a method of extracting silhouettes from implicit surfaces using a seed-and-traverse method.
 Seeding is performed by ray-surface intersection and walking along the surface to a silhouette. Traversal is done by Euler integration with a penalty to avoid iterative drift.
- [Elber 1998] Describes a method for creating line art renderings from freeform parametric surfaces based on a uniform point sampling of the surface that is independent of the surface parameterization.
- [Gooch 1998] Proposes an NPR color shading model to augment line drawings in technical illustrations.
- [Hamel 1998] Introduces transparency in line drawings by modifying line width, density, or style for occluded surfaces. Uses several static 2D renderings of a scene with transparency enabled and disabled as input to a line drawing algorithm.
- [Koenderink 1998] A comprehensive overview of the structure of relief (i.e. images, height fields, etc...) that covers everything from the historical development of the concepts of

- ridges and valleys, to differential structure, to linear features such as the occluding contour and cliff curves (closely related to suggestive contours). Note: this was written for physicists, so expect math.
- [Masuch 1998a] Extends the daLi! system for creating animated line-drawings from 3D objects with frame-to-frame coherence.
- [Masuch 1998b] Describes an application of the daLi! linedrawing system in visualizing ancient architecture.

1999

- [Barequet 1999] Introduces a method for efficiently detecting silhouette edges in 3D meshes by solving a dual problem of intersecting a plane with line segments.
- [Belhumeur 1999] A theoretical development of the ambiguity present in shaded imagery. The generalized bas-relief transformation also preserves contours and shadow boundaries.
- [Benichou 1999] Details a method that allows for real-time selection and rendering of a complete set of silhouette edges from a 3D mesh after a preprocessing of the mesh.
- [Elber 1999] Introduces an interactive method for rendering of silhouette strokes from freeform models. Generates silhouette-oriented strokes in a preprocessing step and uses an accelerated data structure to selectively render them in real-time.
- [Gooch 1999] Outlines aspects of an interactive technical illustration system for 3D polygonal models. Describes hardware and software methods of drawing silhouettes as well as NPR shading models and shadows.
- [Raskar 1999] Describes a hardware-accelerated method of rendering silhouette edges. Renders back-facing polygons offset towards the camera to show through front-facing polygons.

2000

- [Deussen 2000] Details an algorithm for the creation of penand-ink drawings of trees. Uses silhouettes and hatching to render trunks and branches. Combines individual leaves into larger groups represented by abstract shapes to render foliage.
- [Ebert 2000] Introduces NPR rendering techniques for volume illustration. Topics covered include boundary and silhouette enhancement, feature halos, and tone shading.
- [Girshick 2000] Argues for the merit of using lines along principal directions for conveying 3D shape. Presents psychological evidence to support the importance of principal direction in perception. Describes the creation of principal direction vector fields on surfaces and the tracing of strokes through the vector field to create line drawings.
- * [Hertzmann 2000] Describes line drawing rendering techniques for smooth mesh surfaces. Includes algorithms for fast deterministic detection of silhouettes using a dual surface intersection, cusp detection, visibility, and computation of smooth direction fields suitable for hatching strokes.

- [Northrup 2000] Details a set of rendering methods for lines extracted from 3D geometry. Describes how to smooth selfintersecting silhouette edges in image space and create longer, cleaner silhouette paths using an ID reference image. Suggests rendering line paths as texture-mapped triangle strips to achieve various artistic brush stroke effects.
- [Rossl 2000] Creates a specific style of line-art drawings from 3D models using hatching along principal directions. The object is rendered with surface information (normal, curvature) to image space where user-guided segmentation is performed. Hatching is applied to segmented components along their principal directions.
- [Sander 2000] Contains a section on efficient silhouette detection using a hierarchical cone structure.
- [Treavett 2000] Introduces 3D and multi-pass 2D methods for pen-and-ink rendering of volumes using procedural textures in a standard volume rendering pipeline. Discusses integration of the NPR rendering steps with traditional rendering steps to generate images that are mixed photorealistic and NPR.

2001

- [Csébfalvi 2001] Presents a fast, automatic algorithm for visualization of contours in volumes by rendering areas of high gradient magnitude modulated by a view-dependent term. Details optimizations required to achieve interactive rendering.
- [Gooch 2001] Book describing a variety of non-photorealistic rendering techniques and effects.
- [Knill 2001] Connects the information provided by geodesics on surfaces with homogenous texture "flow".
- [Koenderink 2001] A fantastic development that connects the bas-relief ambiguity [Belhumeur 1999] in shaded imagery with a series of psychophysical experiments that demonstrated that percepts arising from photographs of simply shaded objects respect this ambiguity. The psychophysical tasks described here could be used to measure percepts of NPR imagery.
- [Page 2001] Extracts ridge and valley lines from 3D objects using curvature estimated with a normal voting approach.
- [Praun 2001] Describes a hardware-accelerated method of rendering 3D polygonal models with light-dependent hatched shading in real-time. Generates multi-resolution tonal art maps in an automatic preprocess and renders them using mipmapped texture mapping. Textures are oriented along principal directions such that hatching marks convey surface shape.
- [Raskar 2001] Adapts previous two-pass hardware-assisted rendering techniques to single-pass rendering of silhouettes and creases using modern graphics hardware.
- [Watanabe 2001] Detects ridge and valley triangles on meshes by looking for curvature extrema on the "focal surface." The extreme regions are thresholded and thinned.

- [Isenberg 2002] Describes an algorithm that simplifies selfintersecting silhouette edges from 3D meshes to create longer, cleaner paths suitable for stylized rendering. Differs from previous approaches by using z-buffer techniques and avoiding the use of an ID reference image.
- [Kalnins 2002] Details an interactive NPR rendering system for 3D meshes which allows for artist annotated strokes and brush styles to be consistently rendered across multiple frames and viewpoints. Artist input from one viewpoint is synthesized and propagated for other viewpoints and several models of scale-varying hatching are introduced.
- [Lu 2002] Presents an interactive NPR volume rendering technique using stippling. Includes provisions for enhancement of silhouette and boundary regions and a method of sketching silhouette curves.
- [Lum 2002] Describes a hardware-accelerated parallelized NPR volume rendering method for large volumes. Renders with tone shading, silhouettes and depth cuing at interactive frame-rates on computer clusters.
- [Martin 2002] Introduces a method for creating flat silhouettes from 3D meshes suitable for stylized rendering. Results in an ordered stack of 2D filled polygons which together compose a line drawing of the 3D model.
- [Strothotte 2002] Provides an introduction and overview of NPR rendering methods and areas of application. Explains 2D and 3D algorithms for pen-and-ink, pencil-sketch, painterlyeffects, and other NPR effects.

2003

- * [DeCarlo 2003] Describes a class of lines defined on a surface, suggestive contours, which complement the set of surface contours in depicting shape. Suggestive contours provide interior detail to line drawings and are defined at points with radial curvature of zero. Both object-space and image-space extraction algorithms are provided.
- [Dong 2003] Introduces new non-interactive silhouette and hatching algorithms for volumetric data sets. Hatching strokes for a surface are generated from the surface as well as from data throughout the volume enclosed by the surface.
- * [Isenberg 2003] Surveys a wide variety of silhouette extraction algorithms for polygonal models.
- * [Kalnins 2003] Describes a method for maintaining frame-toframe temporal coherency for stylized silhouettes by propagating line stroke parameterizations between frames.
- [Kindlmann 2003] Transfer function-based rendering of contour and ridge and valley lines in volume data. Contour thickness is controlled using estimated curvatures, and ridges and valleys are emphasized by thresholding principal curvatures.
- * [Pauly 2003] Extracts ridge and valley lines from unstructured 3D point clouds. Performs a scale-space analysis to keep the most important lines at multiple scales.
- [Phillips 2003] Demonstrates that people can consistently mark ridges and valleys in shaded images. Also includes discussion on the presence of ridges and valleys in line drawings.

- [Sousa 2003a] Details a fast but non-interactive method for creating precise ink drawings from highly tessellated 3D models. A fraction of mesh edges are selected to become strokes and are drawn with width modulated by surface curvature.
- [Sousa 2003b] Describes a complete system for generating artistic line drawings from 3D meshes. Extracts silhouettes, boundaries, ridges, and valleys, chains lines together, fits curves to paths, and renders paths sparsely with varying line width.

2004

- [Ashikhmin 2004] Presents a simple image-based approach to rendering silhouettes from 3D meshes without any preprocessing of the mesh surface.
- [Brosz 2004] Introduces an improved method of silhouette selection by considering the stability of silhouettes over potential silhouette edges. Resulting silhouettes can be stylized and drawn with frame-to-frame coherence.
- * [DeCarlo 2004] Discusses the motion and stability of suggestive contours on surfaces and describes an algorithm for interactive suggestive contour extraction and rendering.
- [Gooch 2004] An evaluation of methods for facial illustrations and caricatures that compares photographs and drawings. It turns out that illustrations are learned faster than photographs in recognition tasks.
- [Grabli 2004a] Describes a Python-based programmable architecture for the creation of NPR line drawings. Includes capabilities for line-type selection, line chaining, and stylization as well as descriptions of the requisite data structures and support algorithms.
- [Grabli 2004b] Introduces a method for measuring density in line drawings and a simplification method based on such density information. Differentiates between density measured in a completed drawing versus density measured during the drawing process. Discusses indication as well as stroke prioritization.
- [Kalnins 2004] Discusses the previously introduced WYSI-WYG NPR system in more depth, with sections about stroke representation, visibility, media simulation, temporally-coherent line stylization, and annotated hatching.
- [McGuire 2004] Describes GPU hardware methods for extracting and rendering stylized silhouettes from 3D meshes.
 Creates an edge mesh with edge information stored at its vertices, allowing for the vertex shader to operate on edge information
- [Nagy 2004] Describes a GPU hardware method for rendering silhouettes on volumes. Uses texturing hardware and the fragment shader to generate thin image-space lines, which are then broadened and rendered.
- * [Ohtake 2004] Estimates curvature and curvature derivative of 3D objects using implicit function fits, then extracts high-quality ridge and valley lines using these estimates. Curvature-based filtering is used to keep the most significant lines.
- [Raskar 2004] Introduces a camera and multi-flash setup for acquisition of silhouettes of real-world objects.

- [Schein 2004] Presents a method for extracting silhouettes from volume data by modeling the data with trivariate tensor product B-spline functions and extracting silhouettes from the implicit function representation.
- [Wilson 2004] Introduces a method for rendering line drawings from complex 3D geometry in a comprehensible expressive manner. Areas of high complexity are rendered with abstraction by using a hybrid 2D/3D rendering approach.
- [Xu 2004] Presents an algorithm for real-time rendering of silhouettes from unstructured 3D point clouds.
- [Zakaria 2004] Introduces an algorithm for interactive extraction of stylized silhouettes from unstructured 3D point clouds.
- [Zander 2004] Describes an algorithm for high-quality rendering of hatching on 3D meshes by selectively rendering streamlines derived from surface curvature.

2005

 [Burns 2005] Introduces an interactive method for extracting and rendering contours and suggestive contours from volume data.

References

- AGRAWALA, M., AND STOLTE, C. 2001. Rendering Effective Route Maps: Improving Usability Through Generalization. In *Proceedings of ACM SIGGRAPH 2001*, Computer Graphics Proceedings, Annual Conference Series, 241–250.
- APPEL, A. 1967. The notion of quantitative invisibility and the machine rendering of solids. In *Proceedings of the 1967 22nd national conference*, ACM Press, New York, NY, USA, 387–393.
- ASHIKHMIN, M. 2004. Image-space silhouettes for unprocessed models. In GI '04: Proceedings of the 2004 conference on Graphics interface, Canadian Human-Computer Communications Society, School of Computer Science, University of Waterloo, Waterloo, Ontario, Canada, 195–202.
- BAREQUET, G., DUNCAN, C. A., GOODRICH, M. T., KUMAR, S., AND POP, M. 1999. Efficient perspective-accurate silhouette computation. In SCG '99: Proceedings of the fifteenth annual symposium on Computational geometry, ACM Press, New York, NY, USA, 417–418.
- BARROW, H., AND TENENBAUM, J. 1981. Interpreting Line Drawings as Three-Dimensional Surfaces. *Artificial Intelligence* 17, 75–116.
- BELHUMEUR, P. N., KRIEGMAN, D. J., AND YUILLE, A. L. 1999. The Bas-Relief Ambiguity. *International Journal of Computer Vision 35*, 1, 33.44
- BELYAEV, A., PASKO, A., AND KUNII, T. 1998. Ridges and ravines on implicit surfaces. In *Computer Graphics International* 98, 530–535.
- BENICHOU, F., AND ELBER, G. 1999. Output Sensitive Extraction of Silhouettes from Polygonal Geometry. In PG '99: Proceedings of the 7th Pacific Conference on Computer Graphics and Applications, IEEE Computer Society, Washington, DC, USA, 60.
- Bremer, D., and Hughes, J. 1998. Rapid approximate silhouette rendering of implicit surfaces. In *Implicit Surfaces* 98, 155–164.
- BROSZ, J., SAMAVATI, F., AND SOUSA, M. C. 2004. Silhouette rendering based on stability measurement. In SCCG '04: Proceedings of the 20th spring conference on Computer graphics, ACM Press, New York, NY, USA, 157–167.
- BURNS, M., KLAWE, J., RUSINKIEWICZ, S., FINKELSTEIN, A., AND DECARLO, D. 2005. Line Drawings from Volume Data. In SIGGRAPH '05: Proceedings of the 32nd annual conference on Computer graphics and interactive techniques, ACM Press, New York, NY, USA. To appear.

- CSÉBFALVI, B., MROZ, L., HAUSER, H., KÖNIG, A., AND GRÖLLER, E. 2001. Fast Visualization of Object Contours by Non-Photorealistic Volume Rendering. In *Eurographics 01*.
- DECARLO, D., AND SANTELLA, A. 2002. Stylization and Abstraction of Photographs. *ACM Transactions on Graphics* 21, 3 (July), 769–776.
- DECARLO, D., FINKELSTEIN, A., RUSINKIEWICZ, S., AND SANTELLA, A. 2003. Suggestive contours for conveying shape. *ACM Trans. Graph.* 22, 3, 848–855.
- DECARLO, D., FINKELSTEIN, A., AND RUSINKIEWICZ, S. 2004. Interactive rendering of suggestive contours with temporal coherence. In NPAR '04: Proceedings of the 3rd international symposium on Non-photorealistic animation and rendering, ACM Press, New York, NY, USA, 15–145.
- DEUSSEN, O., AND STROTHOTTE, T. 2000. Computer-generated pen-and-ink illustration of trees. In *SIGGRAPH '00: Proceedings of the 27th annual conference on Computer graphics and interactive techniques*, ACM Press/Addison-Wesley Publishing Co., New York, NY, USA, 13–18.
- DONG, F., CLAPWORTHY, G. J., LIN, H., AND KROKOS, M. A. 2003. Nonphotorealistic Rendering of Medical Volume Data. *IEEE Comput. Graph. Appl.* 23, 4, 44–52.
- DOOLEY, D., AND COHEN, M. F. 1990. Automatic illustration of 3D geometric models: lines. In S13D '90: Proceedings of the 1990 symposium on Interactive 3D graphics, ACM Press, New York, NY, USA, 77–82.
- DURAND, F., OSTROMOUKHOV, V., MILLER, M., DURANLEAU, F., AND DORSEY, J. 2001. Decoupling Strokes and High-Level Attributes for Interactive Traditional Drawing. In *Rendering Techniques 2001: 12th Eurographics Workshop on Rendering*, 71–82.
- EBERT, D., AND RHEINGANS, P. 2000. Volume illustration: non-photorealistic rendering of volume models. In VIS '00: Proceedings of the conference on Visualization '00, IEEE Computer Society Press, Los Alamitos, CA, USA, 195–202.
- ELBER, G., AND COHEN, E. 1990. Hidden curve removal for free form surfaces. In SIGGRAPH '90: Proceedings of the 17th annual conference on Computer graphics and interactive techniques, ACM Press, New York, NY, USA, 95–104.
- ELBER, G. 1995. Line Art Rendering via a Coverage of Isoparametric Curves. *IEEE Transactions on Visualization and Computer Graphics 1*, 3, 231–239.
- ELBER, G. 1995. Line illustrations in computer graphics. *The Visual Computer* 11, 6, 290–296.
- ELBER, G. 1998. Line Art Illustrations of Parametric and Implicit Forms. IEEE Transactions on Visualization and Computer Graphics 4, 1, 71–81.
- ELBER, G. 1999. Interactive Line Art Rendering of Freeform Surfaces. Computer Graphics Forum 18, 3, 1–1.
- GIRSHICK, A., INTERRANTE, V., HAKER, S., AND LEMOINE, T. 2000. Line direction matters: an argument for the use of principal directions in 3D line drawings. In NPAR '00: Proceedings of the 1st international symposium on Non-photorealistic animation and rendering, ACM Press, New York, NY, USA, 43–52.
- GOOCH, A., GOOCH, B., SHIRLEY, P., AND COHEN, E. 1998. A non-photorealistic lighting model for automatic technical illustration. In SIG-GRAPH '98: Proceedings of the 25th annual conference on Computer graphics and interactive techniques, ACM Press, New York, NY, USA, 447–452
- GOOCH, B., SLOAN, P.-P. J., GOOCH, A., SHIRLEY, P., AND RIESEN-FELD, R. 1999. Interactive technical illustration. In *SI3D '99: Proceedings of the 1999 symposium on Interactive 3D graphics*, ACM Press, New York, NY, USA, 31–38.
- GOOCH, B., AND GOOCH, A. 2001. Non-Photorealistic Rendering. A K Peters.
- GOOCH, B., REINHARD, E., AND GOOCH, A. 2004. Human facial illustrations: Creation and psychophysical evaluation. *ACM Trans. Graph.* 23, 1, 27–44.

- GRABLI, S., TURQUIN, E., DURAND, F., AND SILLION, F. 2004. Programmable Style for NPR Line Drawing. In Eurographics Symposium on Rendering '04.
- GRABLI, S., DURAND, F., AND SILLION, F. 2004. Density Measure for Line-Drawing Simplification. In *Proceedings of Pacific Graphics*.
- HAMEL, J., SCHLECHTWEG, S., AND STROTHOTTE, T. 1998. An Approach to Visualizing Transparency in Computer-Generated Line Drawings. In IV '98: Proceedings of the International Conference on Information Visualisation, IEEE Computer Society, Washington, DC, USA, 151.
- HERTZMANN, A., AND ZORIN, D. 2000. Illustrating smooth surfaces. In SIGGRAPH '00: Proceedings of the 27th annual conference on Computer graphics and interactive techniques, ACM Press/Addison-Wesley Publishing Co., New York, NY, USA, 517–526.
- HERTZMANN, A. 2001. Paint by relaxation. In Computer Graphics International 2001, 47–54.
- HSU, S. C., AND LEE, I. H. H. 1994. Drawing and animation using skeletal strokes. In SIGGRAPH '94: Proceedings of the 21st annual conference on Computer graphics and interactive techniques, ACM Press, New York, NY, USA, 109–118.
- INTERRANTE, V., FUCHS, H., AND PIZER, S. 1995. Enhancing Transparent Skin Surfaces with Ridge and Valley Lines. In VIS '95: Proceedings of the 6th conference on Visualization '95, IEEE Computer Society, Washington, DC, USA, 52.
- INTERRANTE, V., FUCHS, H., AND PIZER, S. 1996. Illustrating transparent surfaces with curvature-directed strokes. In VIS '96: Proceedings of the 7th conference on Visualization '96, IEEE Computer Society Press, Los Alamitos, CA, USA, 211–ff.
- ISENBERG, T., HALPER, N., AND STROTHOTTE, T. 2002. Stylizing Silhouettes at Interactive Rates: From Silhouette Edges to Silhouette Strokes. *Computer Graphics Forum* 21, 3, 249–249.
- ISENBERG, T., FREUDENBERG, B., HALPER, N., SCHLECHTWEG, S., AND STROTHOTTE, T. 2003. A Developer's Guide to Silhouette Algorithms for Polygonal Models. *IEEE Comput. Graph. Appl.* 23, 4, 28–37.
- ITTI, L., AND KOCH, C. 2000. A Saliency-based search mechanism for overt and covert shifts of visual attention. Vision Research 40, 1489– 1506
- KALNINS, R. D., MARKOSIAN, L., MEIER, B. J., KOWALSKI, M. A., LEE, J. C., DAVIDSON, P. L., WEBB, M., HUGHES, J. F., AND FINKELSTEIN, A. 2002. WYSIWYG NPR: drawing strokes directly on 3D models. In SIGGRAPH '02: Proceedings of the 29th annual conference on Computer graphics and interactive techniques, ACM Press, New York, NY, USA, 755–762.
- KALNINS, R. D., DAVIDSON, P. L., MARKOSIAN, L., AND FINKEL-STEIN, A. 2003. Coherent stylized silhouettes. ACM Trans. Graph. 22, 3, 856–861.
- KALNINS, R. D. 2004. WYSIWYG NPR: Interactive Stylization for Stroke-Based Rendering of 3D Animation. PhD thesis, Princeton University.
- KINDLMANN, G., WHITAKER, R., TASDIZEN, T., AND MOLLER, T. 2003. Curvature-based transfer functions for direct volume rendering: methods and applications. In *IEEE Visualization 2003*, 513–520.
- KNILL, D. C. 1992. Perception of surface contours and surface shape: from computation to psychophysics. *Journal of the Optical Society of America A* 9, 9, 1449–1464.
- KNILL, D. C. 2001. Contour into texture: information content of surface contours and texture flow. *Journal of the Optical Society of America A* 18, 1, 12–35.
- KOENDERINK, J. J., AND VAN DOORN, A. J. 1982. The Shape of Smooth Objects and the Way Contours End. *Perception 11*, 129–137.
- KOENDERINK, J. J. 1984. What does the occluding contour tell us about solid shape? *Perception* 13, 321–330.
- KOENDERINK, J. J. 1990. Solid Shape. MIT press.

- KOENDERINK, J. J., VAN DOORN, A., CHRISTOU, C., AND LAPPIN, J. 1996. Shape constancy in pictorial relief. *Perception* 25, 155–164.
- KOENDERINK, J. J., AND VAN DOORN, A. 1998. The Structure of Relief. Advances in Imaging and Electron Physics 103, 65–150.
- KOENDERINK, J. J., VAN DOORN, A. J., KAPPERS, A. M., AND TODD, J. T. 2001. Ambiguity and the 'mental eye' in pictorial relief. *Perception* 30, 431–448.
- LU, A., MORRIS, C. J., EBERT, D. S., RHEINGANS, P., AND HANSEN, C. 2002. Non-photorealistic volume rendering using stippling techniques. In VIS '02: Proceedings of the conference on Visualization '02, IEEE Computer Society, Washington, DC, USA, 211–218.
- LUM, E. B., AND MA, K.-L. 2002. Hardware-accelerated parallel nonphotorealistic volume rendering. In NPAR '02: Proceedings of the 2nd international symposium on Non-photorealistic animation and rendering, ACM Press, New York, NY, USA, 67–ff.
- MA, K.-L., AND INTERRANTE, V. 1997. Extracting feature lines from 3D unstructured grids. In VIS '97: Proceedings of the 8th conference on Visualization '97, IEEE Computer Society Press, Los Alamitos, CA, USA, 285–ff.
- MALIK, J. 1987. Interpreting Line Drawings of Curved Objects. *International Journal of Computer Vision* 1, 1, 73–103.
- MARKOSIAN, L., KOWALSKI, M. A., GOLDSTEIN, D., TRYCHIN, S. J., HUGHES, J. F., AND BOURDEV, L. D. 1997. Real-time nonphoto-realistic rendering. In SIGGRAPH '97: Proceedings of the 24th annual conference on Computer graphics and interactive techniques, ACM Press/Addison-Wesley Publishing Co., New York, NY, USA, 415–420.
- MARTIN, D., FEKETE, J., AND TORRES, J. C. 2002. Flattening 3D objects using silhouettes. *Computer Graphics Forum 21*, 3, 239–239.
- MASUCH, M., SCHLECHTWEG, S., AND SCHNWLDER, B. 1997. dali! Drawing Animated Lines! In Simulation and Animation 97, 87–96.
- MASUCH, M., SCHUHMANN, L., AND SCHLECHTWEG, S. 1998. Animating Frame-To-Frame-Coherent Line Drawings for Illustrated Purposes. In *Simulation and Animation 98*, 101–112.
- MASUCH, M., AND STROTHOTTE, T. 1998. Visualising Ancient Architecture using Animating Line Drawings. In *IV '98: Proceedings of the International Conference on Information Visualisation*, IEEE Computer Society, Washington, DC, USA, 261.
- McGuire, M., and Hughes, J. F. 2004. Hardware-determined feature edges. In NPAR '04: Proceedings of the 3rd international symposium on Non-photorealistic animation and rendering, ACM Press, New York, NY, USA, 35–147.
- NAGY, Z., AND KLEIN, R. 2004. High-Quality Silhouette Illustration for Texture-Based Volume Rendering. In WSCG '04.
- NORTHRUP, J. D., AND MARKOSIAN, L. 2000. Artistic silhouettes: a hybrid approach. In *NPAR '00: Proceedings of the 1st international symposium on Non-photorealistic animation and rendering*, ACM Press, New York, NY, USA, 31–37.
- OHTAKE, Y., BELYAEV, A., AND SEIDEL, H.-P. 2004. Ridge-valley lines on meshes via implicit surface fitting. *ACM Trans. Graph.* 23, 3.
- PAGE, D. L., KOSCHAN, A., SUN, Y., PAIK, J., AND ABIDI, A. 2001. Robust Crease Detection and Curvature Estimation of Piecewise Smooth Surfaces from Triangle Mesh Approximations Using Normal Voting. In Proc. Conference on Computer Vision and Pattern Recognition.
- PAULY, M., KEISER, R., AND GROSS, M. 2003. Multi-Scale Feature Extraction on Point-Sampled Models. In *Proc. Eurographics*.
- PHILLIPS, F., TODD, J. T., KOENDERINK, J. J., AND KAPPERS, A. M. 2003. Perceptual representation of visible surfaces. *Perception and Psy-chophysics* 65, 5, 747–762.
- PRAUN, E., HOPPE, H., WEBB, M., AND FINKELSTEIN, A. 2001. Realtime hatching. In SIGGRAPH '01: Proceedings of the 28th annual conference on Computer graphics and interactive techniques, ACM Press, New York, NY, USA, 581.

- RASKAR, R., AND COHEN, M. 1999. Image precision silhouette edges. In SI3D '99: Proceedings of the 1999 symposium on Interactive 3D graphics, ACM Press, New York, NY, USA, 135–140.
- RASKAR, R. 2001. Hardware Support for Non-photorealistic Rendering. In Proc. Graphics Hardware.
- RASKAR, R., HAN TAN, K., FERIS, R., YU, J., AND TURK, M. 2004. Non-photorealistic Camera: Depth Edge Detection and Stylized Rendering using Multi-Flash Imaging. ACM Trans. Graph. 23, 3.
- ROSSIGNAC, J., AND VAN EMMERIK, M. 1992. Hidden Contours on a Framebuffer. *Proc. of 7th Workshop on Computer Graphics Hardware*.
- ROSSL, C., AND KOBBELT, L. 2000. Line-art rendering of 3D-models. In Pacific Graphics 00, 87–96.
- SAITO, T., AND TAKAHASHI, T. 1990. Comprehensible rendering of 3-D shapes. In SIGGRAPH '90: Proceedings of the 17th annual conference on Computer graphics and interactive techniques, ACM Press, New York, NY, USA, 197–206.
- SAITO, T. 1994. Real-time previewing for volume visualization. In VVS '94: Proceedings of the 1994 symposium on Volume visualization, ACM Press, New York, NY, USA, 99–106.
- SALISBURY, M. P., ANDERSON, S. E., BARZEL, R., AND SALESIN, D. H. 1994. Interactive pen-and-ink illustration. In SIGGRAPH '94: Proceedings of the 21st annual conference on Computer graphics and interactive techniques, ACM Press, New York, NY, USA, 101–108.
- SALISBURY, M., ANDERSON, C., LISCHINSKI, D., AND SALESIN, D. H. 1996. Scale-dependent reproduction of pen-and-ink illustrations. In SIG-GRAPH '96: Proceedings of the 23rd annual conference on Computer graphics and interactive techniques, ACM Press, New York, NY, USA, 461–468.
- SANDER, P. V., GU, X., GORTLER, S. J., HOPPE, H., AND SNYDER, J. 2000. Silhouette clipping. In SIGGRAPH '00: Proceedings of the 27th annual conference on Computer graphics and interactive techniques, ACM Press/Addison-Wesley Publishing Co., New York, NY, USA, 327– 334.
- SANTELLA, A., AND DECARLO, D. 2004. Visual interest and NPR: an evaluation and manifesto. In NPAR 2004, 71–78.
- SCHEIN, S., AND ELBER, G. 2004. Adaptive extraction and visualization of silhouette curves from volumetric datasets. Vis. Comput. 20, 4, 243– 252
- SOUSA, M. C., FOSTER, K., WYVILL, B., AND SAMAVATI, F. 2003. Precise Ink Drawing of 3D Models. Computer Graphics Forum 22, 3, 369–369.
- SOUSA, M. C., AND PRUSINKIEWICZ, P. 2003. A Few Good Lines: Suggestive Drawing of 3D Models. Computer Graphics Forum 22, 3, 381–381.
- STEVENS, K. A. 1981. The Visual Interpretation of Surface Contours. Artificial Intelligence 17, 47–73.
- STROTHOTTE, T., AND SCHLECHTWEG, S. 2002. Non-Photorealistic Computer Graphics. Morgan Kaufmann.
- THIRION, J.-P., AND GOURDON, A. 1996. The 3D Marching Lines Algorithm. *Graphical Models and Image Processing* 58, 6 (Nov.), 503–509.
- TREAVETT, S. M. F., AND CHEN, M. 2000. Pen-and-Ink rendering in volume visualisation. In VIS '00: Proceedings of the conference on Visualization '00, IEEE Computer Society Press, Los Alamitos, CA, USA, 203–210.
- WALTZ, D. L. 1975. Understanding Line Drawings of Scenes with Shadows. In *The Psychology of Computer Vision*, P. Winston, Ed. McGraw-Hill. 19–92.
- WATANABE, K., AND BELYAEV, A. G. 2001. Detection of Salient Curvature Features on Polygonal Surfaces. *Computer Graphics Forum (Proc. Eurographics 2001)* 20, 3.
- WILSON, B., AND MA, K.-L. 2004. Rendering complexity in computergenerated pen-and-ink illustrations. In NPAR '04: Proceedings of the 3rd international symposium on Non-photorealistic animation and rendering, ACM Press, New York, NY, USA, 129–137.

- WINKENBACH, G., AND SALESIN, D. H. 1994. Computer-generated penand-ink illustration. In SIGGRAPH '94: Proceedings of the 21st annual conference on Computer graphics and interactive techniques, ACM Press, New York, NY, USA, 91–100.
- WINKENBACH, G., AND SALESIN, D. H. 1996. Rendering parametric surfaces in pen and ink. In *SIGGRAPH* '96: Proceedings of the 23rd annual conference on Computer graphics and interactive techniques, ACM Press, New York, NY, USA, 469–476.
- XU, H., NGUEN, M., YUAN, X., AND CHEN, B. 2004. Interactive Silhouette Rendering for Point-Based Models. In Proc. Eurographics Symposium on Point-Based Graphics.
- ZAKARIA, N., AND SEIDEL, H.-P. 2004. Interactive stylized silhouette for point-sampled geometry. In *GRAPHITE '04: Proceedings of the 2nd international conference on Computer graphics and interactive techniques in Australasia and Southe East Asia*, ACM Press, New York, NY, USA, 242–249.
- ZANDER, J., ISENBERG, T., SCHLECHTWEG, S., AND STROTHOTTE, T. 2004. High Quality Hatching. *Computer Graphics Forum 23*, 3, 421–421.